Type-based Object Immutability with Flexible Initialization

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Abstract. We present a type system for checking object immutability, read-only references, and class immutability in an open or closed world. To allow object initialization outside object constructors (which is often needed in practice), immutable objects are initialized in lexically scoped regions. The system is simple and direct; its only type qualifiers specify immutability properties. No auxiliary annotations, e.g., ownership types, are needed, yet good support for deep immutability is provided. To express object confinement, as required for class immutability in an open world, we use qualifier polymorphism. The system has two versions: one with explicit specification commands that delimit the object initialization phase, and one where such commands are implicit and inferred. In the latter version, all annotations are compatible with Java's extended annotation syntax, as proposed in JSR 308.

1 Introduction

1.1 Motivation

Immutable data structures greatly simplify programming, program maintenance, and reasoning about programs. Immutable structures can be freely shared, even between concurrent threads and with untrusted code, without the need to worry about modifications, even temporary ones, that could result in inconsistent states or broken invariants. In a nutshell, immutable data structures are simple. It is therefore not surprising that favoring immutability is a recommended coding practice for Java [3].

Unfortunately, statically checking object immutability in Java-like languages is not easy, unless one settles for supporting only a restricted programming style that can be enforced through final fields. Clearly, objects are immutable if all their fields are final and of primitive type. Additionally, one can allow final fields of immutable types, this way supporting immutable recursive data structures. Thus, Java's final fields support a style of programming immutable objects that mimics datatypes in functional languages and is advocated, for instance, by Felleisen and Friedman [15].

Many immutable objects, however, do not follow this style. A prominent example are Java's immutable strings. An immutable string is a wrapper around a character array. While final fields can prevent that a string's internal character array is replaced by another character array, final fields cannot prevent that the array elements themselves are mutated. Moreover, Java's type system provides no means for preventing representation exposure of the character array, which would allow indirect mutation of a string through aliases to its (supposedly) internal character array. Preventing this, not just for

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arrays but for any internal mutable data structures, requires a richer type system with support for object confinement.

It is also quite common to have immutable data structures that are not instances of immutable classes. Examples include immutable arrays, immutable collections that are implemented in terms of Java's mutable collection classes (but are never mutated after initialization), and immutable cyclic data structures, e.g., doubly linked lists, graphs or trees with parent references. Concrete examples are given on pages 8, 10 and Figure 3.

This article presents the design of a pluggable type system for Java to specify and statically check various immutability properties. A pluggable type checker operates on Java's abstract syntax trees and is optionally invoked after the standard type checker, to ensure additional properties. A pluggable checker for object immutability guarantees that immutable objects never mutate.

Syntactically, our immutability type system can be handled with Java's extended annotation syntax as proposed by JSR 308 [19], to be included in Java 7, which allows annotations on all occurrences of types. While in this paper we slightly deviate from legal annotation syntax (for explanatory reasons), all proposed annotations are in syntactic positions allowed by JSR 308.

1.2 Kinds of Immutability

The following classification of immutability properties has been used in various places in the literature [34,22]:

- Object immutability: An object is immutable if its state cannot be modified.
- Class immutability: A class is immutable if all its instances in all programs are immutable objects.
- Read-only references: A reference is read-only if the state of the object it refers to cannot be modified through this reference.

Examples of *immutable classes* are Java's String class and the wrapper classes for primitive types, e.g., Integer and Boolean. All instances of immutable classes are immutable objects.

Conversely, *immutable objects* need not be instances of immutable classes. For example, immutable arrays are not instances of an immutable class, and neither are immutable collections that are implemented in terms of Java's mutable collection libraries. Immutable objects that are not instances of immutable classes typically have public, non-final fields or public mutator methods, but the pluggable type system disallows assignments to these fields and calls to these methods.

An example for a *read-only reference* is the reference created by Java's static method Collection unmodifiableCollection(Collection c), which generates a wrapper around collection c. This wrapper refers to c through a read-only reference.

For class immutability, we further distinguish between an open and a closed world [25]:

- Class immutability in a closed world assumes that all program components follow the rules of the pluggable type system.
- Class immutability in an open world assumes that immutable classes and the classes
 they depend on follow the rules of the pluggable type system, but clients of immutable classes are unchecked (i.e., they only follow Java's standard typing rules).

Unchecked class clients may for instance be untrusted applets. Note that the closed world assumption only makes sense if *all* code is checked with the additional type rules. Java's classes String, Integer and Boolean are immutable in an open world. For class immutability in an open world it is essential that instances of immutable classes encapsulate their representation objects. Open-world-immutable classes necessarily have to initialize their instances inside constructors or factory methods, and they should not provide accessible mutator methods or fields. Note also that, in an open world, object immutability without class immutability can only be achieved for objects that are never exposed to unchecked clients, because unchecked clients cannot be prevented from calling mutator methods or assigning to accessible fields if these exist. Similarly, in an open world, read-only references can only be achieved for references that are never exposed to unchecked clients.

1.3 Specifying Immutability with Type Qualifiers

Following our earlier work [18], we support the distinction between mutable and immutable objects through *access qualifiers* on types:

Objects of type Rd *C* are called Rd-objects, and have immutable fields. Our type system is designed to guarantee the following soundness property (see Theorem 2):

Well-typed programs never write to fields of Rd-objects.

For instance, the method bad() attempts an illegal write to a Rd-object and is forbidden by our type system. On the other hand, good() legally writes to a RdWr-object:

```
class C { int f; }
static void bad(Rd C x) {
    x.f = 42; // TYPE ERROR
}
static void good(RdWr C x) {
    x.f = 42; // OK
}
```

An additional type qualifier, Any, represents the least upper bound of Rd and RdWr:

```
p,q:=\cdots Any "either Rd or RdWr" Subtyping: \frac{p<:q\quad C<:D}{p\ C<:q\ D} Rd <: Any RdWr <: Any
```

A reference of a type Any C may refer to a Rd-object or a RdWr-object, so writes through Any-references are forbidden. Beware of the difference between Rd and Any. A reference of type Any C is a *read-only reference*, meaning you cannot write to the object through this particular reference. A reference of type Rd C is a reference to a read-only object, i.e. to an object that *nobody* has write-access to. C

¹ IGJ [34] uses the same three qualifiers, calling them @Mutable, @Immutable, and @ReadOnly instead of Rd, RdWr and Any.

The following example shows how Any-references can be useful. The method m() creates a RdWr-array and then applies the method foo() to the array. From the type of foo() we can tell that foo() does not mutate the array: ²

```
interface Util {
    void foo(int Any [] a);
}

void foo(int Any [] a);

int[] a = new int RdWr [] {42,43,44};

util.foo(a);

assert a[0] == 42;
}
```

In this example, we assume a closed world. In an open world, where there may be unchecked classes that do not play by the additional rules our type system imposes, there is still the possibility that foo() writes a to some heap location of type Any, so that unchecked class could modify a[0] concurrently. Preventing foo() from writing its parameter to the heap can be achieved by a more general method type that uses qualifier polymorphism, as will be discussed in Section 2.3.

1.4 Flexible Object Initialization With Stack-local Regions

A common problem of type systems for object immutability [4,18,34,22] and for non-nullness (more generally, object invariants) [13,14,28] is object initialization. Whereas in traditional type systems, values have the same types throughout program execution, this is not quite true for these systems. Type systems for non-nullness face the difficulty that all fields are initially null; type systems for object immutability face the difficulty that even immutable objects mutate while being initialized. In these systems, each object starts out in an uninitialized state and only obtains its true type at the end of its initialization phase. Thus, objects go through a *typestate transition* from "uninitialized" to "initialized".

Object initialization is often the most complicated aspect of otherwise simple type systems, see for instance Fähndrich and Leino's non-nullness type system [13]. Some of the above type systems require that initialization takes place inside object constructors [13,18,34]. Unfortunately, this does not really simplify matters because object constructors in Java-like languages can contain arbitrary code (which may, for instance, leak self-references or call dynamically dispatched methods). Moreover, initialization inside constructors is often too restrictive in practice. For instance, cyclic data structures often get initialized outside constructors, and array objects do not even have constructors.

One contribution of this paper is a simple but flexible object initialization technique for immutability, using stack-local memory regions. Object initialization with stack-local regions supports a programming style that is natural for programmers in main-stream OO languages. In particular, programmers do not have to mimic destructive reads, as required by type systems where object initialization is based on unique references [4,22]. Statically checking object initialization with stack-local regions is simple, as it does not require tracking aliasing on the heap, which is needed in more general typestate-like systems based on static capabilities [10,29,6,11,5,7,2]. In order to facilitate modular static checking, these systems use additional program annotations in the form of constraints, effects, or pre/postconditions. Our system, on the other hand, only uses standard type annotations, largely hiding the typestate change from "uninitialized"

² Following JSR 308 syntax, the qualifier of an array type C[] is written before the [].

to "initialized" from programmers. To this end, we have designed an inference algorithm that automatically infers the end of object initialization phases (see Section 3.4).

1.5 Object Confinement with Qualifier-polymorphic Methods

A type system for class immutability in an open world must enforce several confinement properties [3]. Specifically, it must guarantee that instances of immutable classes encapsulate their representation objects and that their object constructors do not leak self-references. In our earlier paper [18], we enforced these properties using two type-based confinement techniques (in addition to the access qualifiers Rd and RdWr), namely a dedicated ownership type system for enforcing encapsulation of representation objects, and so-called anonymous methods [32] for confining self-references during object construction. Unfortunately, the resulting type system was more complex than one would desire. One of the insights of this article is that, when combined with flexible object initialization, the various confinement properties for class immutability can be expressed in terms of methods that are polymorphic in access qualifiers.

To get an idea how polymorphism helps with confinement, consider the following qualifier-polymorphic method signature:

where <q> denotes universal quantification of the qualifier variable q, making the method polymorphic in q. For a qualifier hierarchy without greatest element, this signature tells us that foo() does not write its parameter to a heap location, because the type of such a location would need a single qualifier annotation that is greater than all other qualifiers. This observation can be exploited to confine representation objects of immutable objects and to confine self-references to constructors of immutable objects.

To support *deep immutability* we treat the access qualifier as an implicit class parameter. It is interesting that this single class parameter in combination with qualifier-polymorphic methods and flexible object initialization suffices for satisfactorily encoding class immutability. In particular, we do not need separate ownership annotations, because the required confinement properties can be expressed in terms of these primitives, in a similar way as in ownership type systems. Flexible initialization is a crucial ingredient, as it allows us, for instance, to treat the internal character array of a string as an *immutable* object (rather than as a *mutable* object that is owned by an immutable one). This would not be possible if object initialization was tied to object constructors, because then all arrays would necessarily be mutable. As a result of treating the character array inside a string as immutable, our type system can, for instance, easily support different strings sharing the same, immutable, character array for their representation, which is often problematic with ownership types.

³ Any is actually not the greatest element of our qualifier hierarchy, but the greatest qualifier for *initialized* objects. We still name this qualifier Any (rather than Initialized). Fortunately, qualifiers for uninitialized objects are inferred and never need to be written by programmers.

⁴ Supporting immutable arrays initialized by array initializers is not enough for the constructor String(char[] c) of Java's String class, because the length of c is not known statically.

1.6 Summary of Contributions

Based on the ideas sketched in this introduction, we have designed a pluggable immutability type system for Java-like languages. The primitives of the type language are the type qualifiers Rd, RdWr and Any for specifying object access rights. The features of the system are:

- expressiveness: the system supports object immutability, read-only references, and class immutability in a closed and open world;
- simplicity and directness: the system only needs the type qualifiers Rd, RdWr and Any plus qualifier polymorphism; its formal typing rules are simple; annotations are only required on field types and in method signatures; no annotations are required inside method bodies;
- flexible initialization: object initialization is not tied to object constructors; while
 the type system is necessarily flow-sensitive in order to support object initialization,
 it works for concurrency, too, because it enforces that threads only share initialized
 objects and because types of initialized objects are persistent.

On the technical side, our contributions are:

- type system formalization and proof of soundness for object immutability: we formalize a subset of the type system for a small model language; this subset focuses on what we believe is the most critical part of the system, namely, the initialization phase; we prove that the system is sound for object immutability: well-typed programs never write to Rd-objects;
- a local annotation inference algorithm: we present a local annotation inference
 algorithm that automatically infers the end of object initialization phases; we have
 formalized this algorithm for our model language and proven it sound.

Outline. The rest of the paper has two parts. Section 2 informally discusses the type system design. Section 3 contains the technical contributions: it formalizes the type system for a small model language, presents the annotation inference algorithm, and states soundness theorems, whose detailed proofs are contained in the companion report [17]. Section 4 compares to related work and Section 5 concludes.

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2 Informal Presentation

We carry on with the informal presentation, as started in Section 1.3.

2.1 Access Qualifier as Class Parameter

For aggregate object structures, it is desirable to associate a single access qualifier with the entire aggregate, especially if the internal structure of the aggregate is hidden from object clients. In order to support access control for aggregates through single access qualifiers, we treat the access qualifier as an implicit class parameter. We have already proposed this in [18] and so has IGJ [34]. Technically, we introduce a special access variable myaccess that refers to the access qualifier of this. The scope of this variable is the entire class body. In particular, the myaccess variable can be used in field types

and signatures of methods and constructors. In the Square class below, myaccess annotates the type Point of its fields. Method m() takes an Any-square, so can neither write to the Point-fields of the square, nor to the int-fields of its points.

```
class Point { int x; int y; }
class Square { myaccess Point upperleft; myaccess Point lowerright; }
static void m(Any Square s) {
    s.upperleft = s.lowerright; // TYPE ERROR
    s.upperleft.x = 42; // TYPE ERROR
}
```

It is also possible to assign a single access right to a cyclic structure. For instance:

```
class Person { myaccess Person partner; }
class Couple { myaccess Person husband; myaccess Person wife; }
```

Old-fashioned couples stick with each other forever: they have type Rd Couple. Modern couples can divorce and the partners can re-marry: they have type RdWr Couple.

The access qualifier is a *covariant class parameter*. Generally, covariant class parameters are unsound, because upcasting a class parameter allows ill-typed writes to fields whose types depend on this class parameter. Here, treating the access qualifier covariantly is sound, because access qualifiers that permit write-access are minimal elements of the qualifier hierarchy. Thus, *upcasting access qualifiers makes object references read-only*.

2.2 Flexible Initialization

For sound object initialization, we adapt a technique from region-based memory management [30], allowing initialization of immutable objects inside *stack-local memory regions* (closely related to *lexically scoped regions*). A stack-local region is a part of the heap that cannot be reached from the rest of the heap. All references into a stack-local region are on the stack. Each stack-local region is *owned* by a method (or a constructor), namely, the lowest method on the call stack that holds references into this region. All objects inside a stack-local region have the same special type qualifier. The method that owns the region (and only this method) is permitted to change this type qualifier to some other qualifier, uniformly for all objects in the same region. When this typestate change is performed, the owning method is on the top of the call stack, so all references into the stack-local region come from local variables of this owning method. This means that all references into the stack-local region at the time of the typestate change are statically known: the static type system can easily modify the type qualifiers of these references.

Technically, to support flexible initialization, we add Fresh-qualifiers. These have a name as an argument, which we call an *initialization token*.

```
p,q ::= \cdots
Fresh(n) fresh object under initialization
n \in \text{Name} token for initializing a set of related objects
```

An initialization token can be viewed as an identifier for a stack-local region that contains Fresh(n)-objects. The token n is secret to the method that owns the associated region and grants permission to commit Fresh(n) to q, for any q. To syntactically capture this semantics, we introduce two *specification commands*:

```
newtoken n create a new initialization token commit Fresh(n) as q globally convert Fresh(n) to q
```

These are specification commands, i.e., they operate on auxiliary state ("ghost state") and have no runtime effect on concrete state or control flow. Our inference algorithm can infer all specification commands, so they need not be written by the programmer. In fact, all annotations inside method bodies can be inferred, so that programmers only have to write qualifiers in field declarations and method signatures. In the examples below, all inferred annotations are shaded gray.

The following method, for instance, creates an immutable array; it uses the flexible initialization technique, to initialize the array \mathbf{r} outside a constructor.

```
static char Rd [] copy (char Any [] a) {
   newtoken n;
   char[] r = new char Fresh(n) [a.length];
   for (int i=0; i++; i < a.length) r[i] = a[i];
   commit Fresh(n) as Rd;
   return r;
}</pre>
```

To initialize immutable cyclic data structures, we use the same initialization token for all members of the structure. Using the flexible initialization technique, we can set cross-references (here husband and wife) *after* the constructors have been called:⁵

```
newtoken n;
Person alice = new <Fresh(n)>Person();
Person bob = new <Fresh(n)>Person();
alice.partner = bob; bob.partner = alice;
Couple couple = new <Fresh(n)>Couple();
couple.husband = bob; couple.wife = alice;
commit Fresh(n) as Rd;
```

Note that field types and method signatures cannot contain Fresh(n)-annotations, because n is out-of-scope in field types and method signatures:

```
class C {
   Fresh(n) D x; // TYPE ERROR: n out of scope
   static Rd C commit(Fresh(n) C x) { // TYPE ERROR: n out of scope
        commit Fresh(n) as Rd; return x; }
}
```

Because we do not allow methods that are parametrized by initialization tokens, each initialization token is confined to a single method. As a result, only the method that "owns" a Fresh(n)-region can commit it, which is crucial for the soundness of commit.

Figure 1 sketches a runtime configuration before a commit-statement. In this configuration, the heap has three regions: a region of initialized objects, and two Fresh regions with associated initialization tokens n1 and n2. The picture shows possible inter-region references. Importantly, the type system ensures that there are no incoming references from the heap into Fresh regions. Furthermore, when the top of the stack

⁵ Person() is a qualifier-polymorphic constructor, hence the angle brackets. See Section 2.4.

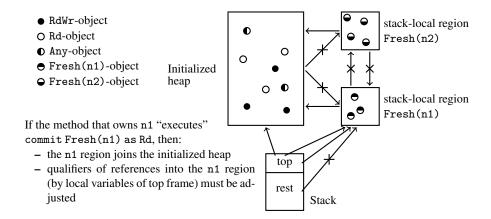


Fig. 1. Committing the fresh region owned by the top stack frame.

owns region n1, there are no references from the rest of the stack into this region. When the commit-statement is executed, region n1 is merged with the initialized region. The type system then has to adjust the qualifiers of all references into region n1. Fortunately, this can be done statically, because all references into this region come from local variables in its owning method.

2.3 Qualifier Polymorphism for Methods

Consider the following method:

```
static void copy(Point src, Point dst) {
    dst.x = src.x; dst.y = src.y;
}
```

This method could accept both RdWr-points and Fresh-points as dst-parameters. To facilitate this, we introduce *bounded qualifier polymorphism for methods*. The Hasse diagram in Figure 2.3 depicts the qualifier hierarchy, including qualifier bounds. The syntax for qualifier-polymorphic methods is as in Java Generics:

```
\langle \bar{\alpha} \text{ extends } \bar{B} \rangle T m(\bar{T} \bar{x}) q \{ \dots \} (method declaration)
```

We usually omit the qualifier bound Qual, writing <a extends Qual> as <a>. The qualifier q is associated with the receiver parameter, that is, e.m() can only be called if e's access qualifier is a subqualifier of q. Receiver qualifiers are not present in static methods. For subclassing, method types are treated contravariantly in the qualifiers on input types (including the receiver qualifier) and covariantly in the qualifier on the output type. These variances are as in IGJ [34]. We can now type copy() as follows:

```
static <a, b extends Writeable> void copy(a Point src, b Point dst) {
   dst.x = src.x; dst.y = src.y;
}
```

Note that Writeable can only be used as a qualifier bound, but not as a qualifier. Allowing Writeable as qualifier would lead to unsoundness for two reasons: Firstly,

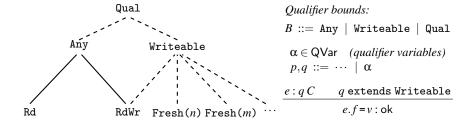


Fig. 2. The qualifier hierarchy. Qual and Writable are qualifier *bounds*, not qualifiers, so they cannot be used as type qualifiers, only in extends-clauses.

Writeable would be a *non-minimal qualifier that allows writes*, which would make covariance of the myaccess class parameter unsound. Secondly, Writeable could be used as an annotation on field types. This would open the door for violating stack locality of Fresh-regions, which would make the typestate transition at commits unsound.

Signatures of qualifier-polymorphic methods tell us which method parameters are potentially mutated by the method. In addition, they also provide information about which method parameters are potentially written to the heap. For instance:

```
static <a> void foo(int a [] x);
does not write to object x through reference x
does not write object x to the heap
static void faa(int Any [] x);
does not write to object x through reference x
may write object x to the heap (into Any-fields)
static <a extends Writeable> void fee(int a [] x);
may write to object x through reference x
```

• does not write object x to the heap

The method foo(x) cannot write x to the heap, because the qualifier hierarchy does not have a greatest element, which would be needed as the type of a location that x can be written to. Similarly, fee(x) cannot write x to the heap, because there is no qualifier that bounds all writeable qualifiers.

In the following example, we use the qualifier for the receiver parameter to distinguish between inspector and mutator methods. Inspectors can be called on any receivers, whereas mutators can only be called on writeable receivers:

```
class Hashtable<K,V> {
     <a> V get(K key) a { ... } // inspector
     <a extends Writeable> V put(K key, V value) a { ... } // mutator
}
```

To create an immutable hash table we can use flexible initialization outside the constructor:

```
newtoken n;
Hashtable<String,String> t = new <Fresh(n)>Hashtable<String,String>();
t.put("Alice", "Female"); t.put("Bob", "Male");
commit Fresh(n) as Rd;
t.get("Alice"); // OK
t.put("Charly", "Male"); // TYPE ERROR
```

2.4 Constructors

Constructor declarations have one of the following two forms:

```
<\bar{\alpha} extends \bar{B}> q C(\bar{T}\ \bar{x}) p { body } (caller-commit constructor) <\bar{\alpha} extends \bar{B}> q C(\bar{T}\ \bar{x}) { newtoken n; body } (constructor-commit constructor)
```

Caller-commit constructors are more common. In their signature, p represents the qualifier of this when the constructor body starts executing. The typechecker assumes this qualifier initially when checking the constructor body, and enforces that constructor callers, through super() or this(), establish this precondition. The postcondition q represents the qualifier of this when the constructor terminates.

A typical instance of caller-commit constructors looks like this:

```
<\alpha extends Writeable>\alpha C(\bar{T}\bar{x}) \alpha \{ \dots \}
```

In particular, the default no-arg constructors have this form. Note that, if in the above constructor signature α does not occur in any of the parameter types \bar{T} , then we know that the constructor does not leak references to this⁶. This is often desired for constructors. Constructors that deliberately leak this could have the following form (which prevents the creation of immutable class instances):

$$RdWr C(\bar{T} \bar{x}) RdWr \{ \dots \}$$

Constructor-commit constructors enforce that the object is committed inside the constructor. This is useful in an open world to prevent object clients from ever seeing an uninitialized object. In constructor-commit constructors, the precondition is omitted. Instead, the constructor begins by generating a fresh token n. The body then initially assumes that this has qualifier Fresh(n). The scope of n is the constructor body, and therefore n cannot be mentioned in the constructor postcondition. To establish the postcondition, the body is forced to commit Fresh(n) before it terminates. The type system disallows calling constructor-commit constructors through fresh(n) this (). Therefore, constructor-commit constructors are particularly suited for fresh(n) classes.

Figure 3 shows an example with a caller-commit constructor. An immutable tree with parent pointers is constructed from the bottom up. A single initialization token is used for all nodes and is committed only after the root node has been initialized. This example is interesting because Qi and Myers [28] identify it as a problematic initialization pattern for other type systems [14]. It causes no problems for our system.

2.5 Class Immutability in an Open World

In his book "Effective Java" [3], Bloch presents rules that ensure class immutability. These rules require that fields of immutable classes are private and final, that public methods are inspectors, that methods and constructors do not leak representation objects, that public constructors do not leak this, and that the behaviour of instances of immutable classes does not depend on overridable methods. Some of these rules (e.g., that all fields are private and final) can very easily be checked automatically. The conditions that methods of immutable classes are inspectors, that instances of immutable

⁶ If α occurs in \bar{T} , the constructor could for instance leak this to a field x.f of a constructor parameter α Dx, in case f's type in C is annotated with myaccess.

```
class Tree {
    myaccess Tree parent, left, right;
    <a extends Writeable> a Tree (a Tree left, a Tree right) a {
        this.left = left; this.right = right;
        if (left != null) left.parent = this;
        if (right != null) right.parent = this;
    }
}
newtoken n;
Tree left_leaf = new <Fresh(n)>Tree(null, null);
Tree right_leaf = new <Fresh(n)>Tree(null, null);
Tree root = new <Fresh(n)>Tree(left_leaf, right_leaf);
root.parent = root;
commit Fresh(n) as Rd;
```

Fig. 3. Bottom-up initialization of a tree with parent pointers

classes do not leak representation, and that constructors of immutable classes do not leak this can be expressed and checked by our type system.

If we specify class immutability with a class annotation Immutable, we could for instance declare an immutable String class like this:

```
Immutable final class String {
    private final char myaccess [] value;
    ...
}
```

Semantically, the Immutable annotation is meant to specify that String is an immutable class in an open world, i.e., that all instances of String are Rd-objects that cannot be mutated by possibly unchecked clients. In order to tie the access modifier for the value array to the access modifier for the enclosing string, it is important that we annotate the value field with myaccess instead of Rd. In combination with the requirements on method and constructor signatures below, this prevents representation exposure of the character array.

The following rules guarantee class immutability:

- immutable classes must be final and direct subclasses of Object
- methods and constructors may only call static or final methods or methods of final classes (transitively)
- all fields must be final
- public constructors must have the following form:

```
< $\tilde{\alpha}$ extends $\bar{B} > \text{Rd}$ $C(\bar{T},\bar{x})$ { newtoken $n$; ...; commit Fresh($n$) as Rd; } where myaccess does not occur in $\bar{T}$
```

- types of public methods must have the following form:

```
\langle \alpha, \bar{\beta} \text{ extends } \bar{B} \rangle U m(\bar{T} \bar{x}) \alpha \{ \dots \}
```

```
static <a, b extends Writeable>
void arraycopy(a Object src, int srcPos, b Object dst, int dstPos, int 1);
public <a> Rd String(char a value[]) {
    newtoken n;
    int size = value.length;
    char[] v = new char Fresh(n) [size];
    System.arraycopy(value, 0, v, 0, size);
    this.offset = 0; this.count = size; this.value = v;
    commit Fresh(n) as Rd;
}
```

Fig. 4. A constructor of Java's immutable String class

We use the String example to explain the constructor rule: The rule ensures that public constructors do not assign previously existing character arrays to the string's value field. This would only be possible, if the class parameter myaccess occurred in one of the parameter types \bar{T} , which is forbidden. For instance, the constructor String(char value[]) is forced to make a defensive copy of its input parameter, as shown in Figure 4. Furthermore, constructors can not assign this or this.value to heap locations outside the stack-local Fresh(n)-region. This would only be possible if one of the parameter types \bar{T} mentioned myaccess, or if the commit-statement were executed somewhere in the middle of the constructor, in which case the constructor could write this.value or this to the heap as a Rd-object after the commit.

As for the method rule, we have already argued that the above method type enforces that m is an inspector. Furthermore, the type forbids that m assigns the value array to the heap, because the qualifier hierarchy does not have a greatest element. Note that method types of the form U $m(\bar{T}\ \bar{x})$ Any $\{\ldots\}$ do not prevent representation exposure, because they enable writing the value array to Any-fields, which is dangerous in an open-world. Similarly, if the value field were annotated with Rd instead of myaccess, the value array could be written to Rd-fields or Any-fields.

2.6 Threads

For type soundness in multi-threaded programs, we must ensure that thread-shared objects are initialized, i.e., they must have types Rd, RdWr or Any, but not Fresh. This suffices for soundness, because types of initialized objects never change. As all thread-shared objects are reachable from the sharing Thread-objects and as the initialized region is closed under reachability⁷, it suffices to require that Thread-objects are initialized when threads get started. Furthermore, we must assume this fact as the precondition for verifying the body of Thread.run():

```
class Thread {
    void run() RdWr { }
    void start(); // Treated specially. Type system uses run()'s type.
}
```

⁷ In this discussion, we ignore Java Generics. See [17] for a discussion of generics.

Subclasses of Thread may override run() with receiver qualifier RdWr or Any (by contravariance)⁸. Calling start() on a receiver o, whose static type is a subtype MyThread of Thread, requires that o has run()'s receiver qualifier from MyThread. Note that treating Thread.start() specially is not a random special case, because conceptually Thread.start() is a concurrency primitive for dynamic thread creation (a.k.a. fork or spawn), which is always treated specially in verification systems for concurrency.

3 The Formal Model

We formalize our system for a model language that is deliberately simple. The main objective is to prove soundness of the flexible initialization technique in a very simple setting, to describe the local inference algorithm in the small as a high-level blueprint for an implementation, and to prove soundness of the inference algorithm. Our simple language is based on recursively defined records with nominal types, recursive function definitions, and a simple command language. We include conditionals and while-loops, because the type system and the associated inference algorithm are flow-sensitive, and so branching and repetition are interesting.

Mathematical Notation. Let $X \to Y$ be the set of functions from X to Y, and $X \rightharpoonup Y$ the set of partial functions, and $\mathsf{SetOf}(X)$ the set of all subsets of X. Functions $f \in X \rightharpoonup Y$ induce functions in $\hat{f} \in \mathsf{SetOf}(X) \to \mathsf{SetOf}(Y)$: $\hat{f}(X') = \{f(x) \mid x \in X' \cap \mathsf{dom}(f)\}$. We usually omit the hat when the context resolves ambiguities. For $f \in X \rightharpoonup Y$ and Z some set, let $f \mid Z$ be the restriction of f to Z: $f \mid Z = \{(x,y) \in f \mid x \in Z\}$. For $f \in X \rightharpoonup Y$ and $g \in Y \to Z$, let $g \circ f = \{(x,g(f(x))) \mid x \in \mathsf{dom}(f)\}$. Note that $g \circ f \in X \rightharpoonup Z$. For $f,g \in X \rightharpoonup Y$, let $f[g] = g \cup (f \mid \{x \mid x \not\in \mathsf{dom}(g)\})$. Let $x \mapsto y = \{(x,y)\}$. We write $f,x \mapsto y$ instead of $f[x \mapsto y]$ when we want to indicate that $x \not\in \mathsf{dom}(f)$. If f is a type environment, we write f[x:y] and f,x:y instead of $f[x \mapsto y]$ and $f,x \mapsto y$. We write π_1 and π_2 for the first and second projection that map pairs to their components.

3.1 A Model Programming Language with Access Qualifiers

Our model is based on records. We refer to named record types as classes, and to records as objects. Record types are of the form qC, where q is an access qualifier and C a class identifier. The void-type has only one element, namely null. We define a mapping that erases qualifiers from types: |qC| = C and |void| = void. Subqualifying is the least partial order such that Rd <: Any and RdWr <: Any. Subtyping is the least partial order such that pC <: qC for all p <: q. A class table is a set of class declarations for distinct class identifiers. Class declarations may be (mutually) recursive. A method table is a set of (mutually) recursive function declarations for distinct identifiers. The syntax of the model language is shown below. The identifiers x and x in the forms x and x in the forms x and x in the forms of bound identifiers. The judgment in Figure 5 formalizes boundedness (writing x for extends) and ensures that arguments x of Fresh x represent initialization tokens.

⁸ It would also be sound to use Rd as the receiver qualifier for Thread.run(). However, this would be too restrictive, because it would globally enforce that threads never write to fields of their Thread-objects.

⁹ See also the remark on the operational semantics of newtoken at the end of Section 3.2.

Fig. 5. Qualifier typing, $\Delta \vdash q \triangleleft B$ and $\Delta \vdash n$: Token

```
n, o \in \mathsf{Name} (names)
                                                 \alpha, \beta \in \mathsf{QVar} (qualifier variables, including myaccess)
 p,q \in Qual ::= Rd \mid RdWr \mid Any \mid Fresh(n) \mid \alpha \quad (access qualifiers)
 f,g \in \mathsf{FieldId} (field identifiers)
                                                              C,D \in \mathsf{ClassId} (class identifiers)
 class ::= class C \{ \bar{T} \bar{f} \} (class declarations)
                                                                                     T \in \mathsf{Ty} ::= q C \mid \mathsf{void} \mid (types)
 B \in \mathsf{QualBound} ::= \mathsf{Writeable} \mid \mathsf{Any} \mid \mathsf{Qual} \quad (qualifier\ bounds)
 m \in MethodId (method identifiers)
                                                                    x \in Var \quad (local \ variables)
 method ::= \langle \bar{\alpha} \triangleleft \bar{B} \rangle T m(\bar{T} \bar{x}) \{e\} (method declarations)
v \in \mathsf{OpenVal} ::= \mathtt{null} \mid n \mid x
                                                                                                             (open values)
e \in \mathsf{Exp} ::= v \mid C x; e \mid \mathsf{newtoken} \, n; e \mid h; e
                                                                                                             (expressions)
h \in \mathsf{HdExp} ::= x = v \mid x = v.f \mid v.f = v \mid x = \langle \bar{q} \rangle m(\bar{v}) \mid x = \mathsf{new} \ q \ C \mid
                                                                                                            (head expressions)
                        if v e e \mid while v e \mid commit Fresh(n) as q
Derived form, e;e': v;e \stackrel{\Delta}{=} e (h;e);e' \stackrel{\Delta}{=} h;(e;e') (C x;e);e' \stackrel{\Delta}{=} C x;(e;e') if x not free in e'
                                (\text{newtoken } n; e); e' \stackrel{\Delta}{=} \text{newtoken } n; (e; e') \text{ if } n \text{ not free in } e'
Derived form, e; e; \stackrel{\Delta}{=} e; null
```

Note that declarations of local variables associate a class C with the variable, but no access qualifier q. The reason for this design choice is that local variables may change their qualifier at commit-statements. We would find it misleading if our system fixed an access qualifier for a local variable at its declaration site, even though later the variable refers to objects with incompatible access qualifiers.

Our system also permits qualifier changes at assignments to local variables. This seems a natural design choice, given that we have flexible qualifiers for local variables anyway. When a local variable *x* is used, the type system assumes the access qualifier of the object that most recently got assigned to *x*. For instance, assuming a context where local variables **r** and **w** have types Rd Point and RdWr Point, respectively:

```
Point p; p=w; // now p has type RdWr Point
p.x=42; // this typechecks
p=r; // now p has type Rd Point
p.x=42; // type error: illegal write to Rd-object
```

3.2 Operational Semantics

Heaps are functions from names to objects. Each object is tagged with an access qualifier. These tags are auxiliary state in the sense that they have no effect on concrete program state or control flow, that is, they are erasable. The operational semantics also tracks the pool of tokens that have so far been generated. Token pools are erasable.

```
\mathbf{v} \in \mathsf{Val} ::= \mathtt{null} \mid n \qquad obj \in \mathsf{Object} \stackrel{\triangle}{=} \mathsf{Qual} \times (\mathsf{FieldId} \rightharpoonup \mathsf{Val}) ::= q \{ \bar{f} = \bar{\mathbf{v}} \}
h \in \mathsf{Heap} \stackrel{\triangle}{=} \mathsf{Name} \rightharpoonup \mathsf{Object} \qquad t \in \mathsf{TokenPool} \stackrel{\triangle}{=} \mathsf{SetOf}(\mathsf{Name})
```

Commit-environments are functions from names to access qualifiers. They are used to track Fresh-qualifiers that have been committed.

```
(Red Dcl)
                                                                                                                                                                                                                                                                                                                                                                                                                                                      (Red New Token) n \notin t
                    (\sigma, C \ x; e) :: s, h, t \rightarrow ((\sigma, x \mapsto \mathtt{null}), e) :: s, h, t
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           (\sigma, \texttt{newtoken} \ n; e) :: s, h, t \rightarrow (\sigma, e) :: s, h, t \cup \{n\}
  (Red Set Local)
                                                                                                                                                                                                                                                                                                                                                                                                                                          (\text{Red Get}) \quad \textit{v} \neq \texttt{null} \quad \sigma(\textit{v}) = \textit{n}
                                                                                                                                                                                                                                                                                                                                                                                                                                                          (\sigma, x = v.f; e) :: s, h, t \rightarrow (\sigma[x \mapsto \pi_2(h(n))(f)], e) :: s, h, t
                    (\sigma, x = v; e) :: s, h, t \rightarrow (\sigma[x \mapsto \sigma(v)], e) :: s, h, t
  (Red Set) v \neq \text{null} \quad \sigma(v) = n
                    (\sigma, v.f = w; e) :: s, h, t \rightarrow (\sigma, e) :: s, h[n \mapsto (\pi_1(h(n)), \pi_2(h(n))[f \mapsto \sigma(w)])], t
  (Red Call) \langle \bar{\alpha} \triangleleft \bar{B} \rangle U m(\bar{T} \bar{x}) \{e'\}
                    (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}), e'[\bar{q}/\bar{\alpha}]) :: (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}), e'[\bar{q}/\bar{\alpha}]) :: (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}), e'[\bar{q}/\bar{\alpha}]) :: (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}), e'[\bar{q}/\bar{\alpha}]) :: (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}), e'[\bar{q}/\bar{\alpha}]) :: (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}), e'[\bar{q}/\bar{\alpha}]) :: (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}), e'[\bar{q}/\bar{\alpha}]) :: (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}), e'[\bar{q}/\bar{\alpha}]) :: (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}), e'[\bar{q}/\bar{\alpha}]) :: (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}), e'[\bar{q}/\bar{\alpha}]) :: (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}), e'[\bar{q}/\bar{\alpha}]) :: (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}), e'[\bar{q}/\bar{\alpha}]) :: (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}), e'[\bar{q}/\bar{\alpha}]) :: (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}), e'[\bar{q}/\bar{\alpha}]) :: (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}), e'[\bar{q}/\bar{\alpha}]) :: (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}), e'[\bar{q}/\bar{\alpha}]) :: (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}), e'[\bar{q}/\bar{\alpha}]) :: (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}), e'[\bar{q}/\bar{\alpha}]) :: (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}), e'[\bar{q}/\bar{\alpha}]) :: (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}), e'[\bar{q}/\bar{\alpha}]) :: (\sigma, x \mapsto \sigma(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}), e'[\bar{q}/\bar{\alpha}]) :: (\sigma, x \mapsto \sigma(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto \sigma(\bar{v}); e) :: s, h, t \to (\bar{x} \mapsto
                    (\sigma, w) :: (\sigma', x = \langle \bar{q} \rangle m(\bar{v}); e) :: s, h, t \rightarrow (\sigma'[x \mapsto \sigma(w)], e) :: s, h, t
  (Red New) class C\{\bar{T}\bar{f}\} n \notin dom(h)
                    (\sigma, x \texttt{=} \mathtt{new} \ q \ C; e) :: s, h, t \to (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q \ \{\bar{f} \texttt{=} \mathtt{null}\}), t \mapsto (\sigma[x \mapsto n], e) :: s, (h, n \mapsto q
                                                                                                                                                                                                                                                                                                                                                                                                                                 (Red If False) \sigma(v) \neq \text{null}
(\sigma, (\text{if } v e e'); e'') :: s, h, t \rightarrow (\sigma, e'; e'') :: s, h, t
  (Red If True) \sigma(v) = \text{null}
                       (\sigma, (\text{if } v e e'); e'') :: s, h, t \rightarrow (\sigma, e; e'') :: s, h, t)
  (Red While True) \sigma(v) = \text{null}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            (Red While False) \sigma(v) \neq \text{null}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 (\sigma, (\mathtt{while}\ v\ e); e') :: s, h, t \rightarrow (\sigma, e') :: s, h, t
                    (\sigma, (\text{while } v \, e); e') :: s, h, t \rightarrow (\sigma, e; (\text{while } v \, e); e') :: s, h, t
  (Red Commit) \delta = (n \mapsto q)
                    (\sigma, \mathtt{commit} \, \mathtt{Fresh}(n) \, \mathtt{as} \, q; e) :: s, h, t \to (\sigma, e) :: s, (\delta \circ h), t
```

Fig. 6. Operational semantics

```
\delta \in \mathsf{CommitEnv} \stackrel{\vartriangle}{=} \mathsf{Name} \rightharpoonup \mathsf{Qual}
```

Commit-environments δ induce functions $\hat{\delta}$ in Qual \rightarrow Qual, Ty \rightarrow Ty and Object \rightarrow Object: $\hat{\delta}(\mathtt{Fresh}(n)) = q$ if $\delta(n) = q$, $\hat{\delta}(q) = q$ otherwise; $\hat{\delta}(q C) = \hat{\delta}(q) C$, $\hat{\delta}(\mathtt{void}) = \mathtt{void}$; $\hat{\delta}(q \{\bar{f} = \bar{v}\}) = \hat{\delta}(q) \{\bar{f} = \bar{v}\}$. If the context resolves ambiguities, we omit the hat. A *stack frame* is a pair of a local store σ and an expression e:

```
\sigma \in \mathsf{Var} \rightharpoonup \mathsf{Val} fr \in \mathsf{Frame} \stackrel{\Delta}{=} (\mathsf{Var} \rightharpoonup \mathsf{Val}) \times \mathsf{Exp} s \in \mathsf{Stack} ::= \mathsf{nil} \mid fr :: s
```

We extend the domain of functions σ to OpenVal, by setting $\sigma(v) = v$ for $v \in Val$. *Configurations* are triples of stacks, heaps and token pools.

$$cfg \in \mathsf{Configuration} \stackrel{\Delta}{=} \mathsf{Stack} \times \mathsf{Heap} \times \mathsf{TokenPool}$$

The rules in Figure 6 define the small-step operational semantics on configurations. In the rules (Red Dcl) and (Red New Token), we implicitly use a bound-variable convention that allows us to rename bound variables and names appropriately.

3.3 Type System

A type environment is a function from variables and names to types.

$$\iota \in \mathsf{Var} \cup \mathsf{Name} \qquad \Gamma \in \mathsf{TyEnv} \stackrel{\scriptscriptstyle \Delta}{=} (\mathsf{Var} \cup \mathsf{Name}) \rightharpoonup \mathsf{Ty}$$

Let $\Gamma <: \Gamma'$ whenever $\mathsf{dom}(\Gamma) = \mathsf{dom}(\Gamma')$ and $\Gamma(\iota) <: \Gamma'(\iota)$ for all ι in $\mathsf{dom}(\Gamma)$. We extend the domain of type environments to include null: $\Gamma(\mathsf{null}) = \mathsf{void}$.

We define: $\Delta \vdash q$: ok iff $\Delta \vdash q \triangleleft \mathtt{Qual}$; C: ok iff C is declared; $\Delta \vdash q$ C: ok iff $\Delta \vdash q$: ok and C: ok; $\Delta \vdash \mathtt{void}$: ok always; $\Delta \vdash \Gamma$: ok iff $\Delta \vdash \Gamma(\iota)$: ok for all ι in $\mathtt{dom}(\Gamma)$; $\Delta \vdash \delta$: ok iff $\Delta \vdash n$: Token and $\Delta \vdash \delta(n)$: ok for all x in $\mathtt{dom}(\delta)$.

Typing judgments for expressions have the following formats:

$$\Sigma \vdash \{\Gamma, \delta\}e : T\{\Gamma', \delta'\}$$
 $\Sigma \vdash \{\Gamma, \delta\}h\{\Gamma', \delta'\}$

 (Γ, δ) represents the configuration before executing the expression, and (Γ', δ') the one afterwards. We refer to (Γ, δ) as the precondition of the expression, and to (Γ', δ') as its postcondition. Recall that we permit local variables to change the qualifier components of their types. This is why we need to include type environments in postconditions. We write Δ ; $\Gamma \vdash \nu$: T to abbreviate $\Delta \vdash \{\Gamma, \emptyset\}\nu$: $T\{\Gamma, \emptyset\}$.

Now we can present the typing rules for expressions:

$$\frac{(\text{Null})}{\Delta \vdash \Gamma, \delta, T : \text{ok}} \frac{(\text{Id})}{\Delta \vdash \Gamma, \delta \vdash \text{ok}} \frac{(\text{Sub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma, \delta\}} \frac{(\text{Sub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma, \delta\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma, \delta\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\}} \frac{(S \text{ub})}{\Delta \vdash \{\Gamma, \delta\} \text{null} : T\{\Gamma', \delta'\} \text{null} : T\{\Gamma', \delta'\} \text{null} : T\{\Gamma',$$

In the rule (Dcl), we assume that the newly declared local variable initially has type q C, where q can be chosen appropriately. An automatic typechecker needs to delay the choice of an appropriate q until the new variable first gets assigned to. This delayed choice of q is subsumed by the inference algorithm in Section 3.4. The premise $\delta(q) = q$ ensures that q is not a previously committed Fresh-qualifier.

In the typing rules for head expressions, note that we update the qualifiers of local variables after assignments, implementing flexible qualifiers of local variables, as discussed earlier. Crucially, the rule (Set) checks that the object is writeable:

$$(Set \ Local) \qquad (Get) \ class \ C \ \{...T f ..\} \\ |\Gamma(v)| = |\Gamma(x)| \qquad \Gamma(v) = q \ C \quad U = T[q/\text{myaccess}] \quad |U| = |\Gamma(x)| \\ \Delta \vdash \{\Gamma, \delta\} x = v \{\Gamma[x : \Gamma(v)], \delta\} \qquad \Delta \vdash \{\Gamma, \delta\} x = v . f \{\Gamma[x : U], \delta\} \\ (Set) \ class \ C \ \{...T f ..\} \\ \underline{\Gamma(v) = q \ C \quad \Delta \vdash q \triangleleft \text{Writeable} \quad \Delta; \Gamma \vdash w : T[q/\text{myaccess}]} \\ \Delta \vdash \{\Gamma, \delta\} v = w \{\Gamma, \delta\}$$

$$(Call) \quad < \overline{\alpha} \triangleleft \overline{\beta} \gt U \ m(\overline{T} \ \overline{x}) \ \{e\} \\ \underline{\delta(\overline{q}) = \overline{q} \quad \Delta \vdash \overline{q} \triangleleft \overline{\beta} \quad \Delta; \Gamma \vdash \overline{v} : \overline{T}[\overline{q}/\overline{\alpha}] \quad V = U[\overline{q}/\overline{\alpha}] \quad |V| = |\Gamma(x)|} \\ \Delta \vdash \{\Gamma, \delta\} x = c \overline{q} \gt m(\overline{v}) \ \{\Gamma[x : V], \delta\} \qquad \Delta \vdash \{\Gamma, \delta\} x = \text{new } q \ C \{\Gamma[x : q \ C], \delta\}$$

$$(If) \\ \underline{\Delta; \Gamma \vdash v : T \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma', \delta'\} \quad \Delta \vdash \{\Gamma, \delta\} e' : \text{void} \{\Gamma', \delta'\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma, \delta\} \quad \Delta \vdash \{\Gamma, \delta\} e : \text{void} \{\Gamma$$

In the (While) rule, note that the environments are an invariant for the loop body. Consequently, it is disallowed to commit inside a loop body a token that was generated outside the loop body (as this would modify the commit-environment). On the other hand, it is allowed to commit tokens that were generated inside the loop body, because the rule (New Token) removes such tokens from pre- and postcondtions.

For checking class and method declarations, we use the following rules:

$$\begin{array}{lll} & \text{(Class)} & \text{(Method)} \\ & \text{myaccess} \triangleleft \text{Qual} \vdash \bar{T} : \text{ok} & \bar{\alpha} \triangleleft \bar{B} \vdash \{\bar{x} : \bar{T}, \emptyset\} e : U\{\Gamma, \emptyset\} \\ & \text{class } C \ \{\bar{T} \ \bar{f} \ \} : \text{ok} & \text{c} \triangleleft \bar{B} \triangleright U \ m(\bar{T} \ \bar{x}) \ \{e\} : \text{ok} \\ & \text{c} \triangleleft \bar{B} \triangleright U \ m(\bar{T} \ \bar{x}) \ \{e\} : \text{ok} \\ \end{array}$$

```
Well-typed stack frames, \Delta; \Delta'; \Gamma; \Gamma' \vdash fr : T and \Delta; \Delta'; \Gamma; \Gamma' \vdash fr : T \rightarrow U:
 \Delta,\Delta';\Gamma,\Gamma'\vdash\sigma:\Gamma''\quad \Delta,\Delta'\vdash\{\Gamma'',\delta\}e:T\{\Gamma''',\delta'\}\quad \mathsf{dom}(\delta)\subseteq\mathsf{dom}(\Delta')\quad \delta\circ\Gamma''=\Gamma''
                                                                                                                                                                     \Delta; \Delta'; \Gamma; \Gamma' \vdash (\sigma, e) : T
 fr = (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) \quad \Delta; \Delta'; \Gamma; \Gamma' \vdash fr : U \quad \langle \bar{\alpha} \triangleleft \bar{B} \rangle \ T \ m(\bar{V} \ \bar{x}) \\ \{e'\} \qquad \Delta \vdash \Gamma : \mathsf{ok} \quad (\forall x \in \mathsf{dom}(\sigma))(\Delta; \Gamma \vdash \sigma(x) : \Gamma'(x)) \\ = (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) \quad \Delta; \Delta'; \Gamma; \Gamma' \vdash fr : U \quad \langle \bar{\alpha} \triangleleft \bar{B} \rangle \ T \ m(\bar{V} \ \bar{x}) \\ \{e'\} \qquad \Delta \vdash \Gamma : \mathsf{ok} \quad (\forall x \in \mathsf{dom}(\sigma))(\Delta; \Gamma \vdash \sigma(x) : \Gamma'(x)) \\ = (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) \quad \Delta; \Delta'; \Gamma; \Gamma' \vdash fr : U \quad \langle \bar{\alpha} \triangleleft \bar{B} \rangle \ T \ m(\bar{V} \ \bar{x}) \\ = (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) \quad \Delta; \Delta'; \Gamma; \Gamma' \vdash fr : U \quad \langle \bar{\alpha} \triangleleft \bar{B} \rangle \ T \ m(\bar{V} \ \bar{x}) \\ = (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) \quad \Delta; \Delta'; \Gamma; \Gamma' \vdash fr : U \quad \langle \bar{\alpha} \triangleleft \bar{B} \rangle \ T \ m(\bar{V} \ \bar{x}) \\ = (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) \quad \Delta; \Delta'; \Gamma; \Gamma' \vdash fr : U \quad \langle \bar{\alpha} \triangleleft \bar{B} \rangle \ T \ m(\bar{V} \ \bar{x}) \\ = (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) \quad \Delta; \Delta'; \Gamma; \Gamma' \vdash fr : U \quad \langle \bar{\alpha} \triangleleft \bar{B} \rangle \ T \ m(\bar{V} \ \bar{x}) \\ = (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) \quad \Delta; \Delta'; \Gamma; \Gamma' \vdash fr : U \quad \langle \bar{\alpha} \triangleleft \bar{B} \rangle \ T \ m(\bar{V} \ \bar{x}) \\ = (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) \quad \Delta; \Delta'; \Gamma; \Gamma' \vdash fr : U \quad \langle \bar{\alpha} \triangleleft \bar{B} \rangle \ T \ m(\bar{V} \ \bar{x}) \\ = (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) \quad \Delta; \Delta'; \Gamma; \Gamma' \vdash fr : U \quad \langle \bar{\alpha} \triangleleft \bar{B} \rangle \ T \ m(\bar{V} \ \bar{x}) \\ = (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) \quad \Delta; \Delta'; \Gamma; \Gamma' \vdash fr : U \quad \langle \bar{\alpha} \triangleleft \bar{B} \rangle \ T \ m(\bar{V} \ \bar{x}) \\ = (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) \quad \Delta; \Delta'; \Gamma; \Gamma' \vdash fr : U \quad \langle \bar{\alpha} \triangleleft \bar{B} \rangle \ T \ m(\bar{V} \ \bar{x}) \\ = (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) \quad \Delta; \Delta'; \Gamma; \Gamma' \vdash fr : U \quad \langle \bar{\alpha} \triangleleft \bar{B} \rangle \ T \ m(\bar{V} \ \bar{x}) \\ = (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) \quad \Delta; \Delta'; \Gamma; \Gamma' \vdash fr : U \quad \langle \bar{\alpha} \triangleleft \bar{B} \rangle \ T \ m(\bar{v} \ \bar{x}) \\ = (\sigma, x = \langle \bar{q} \rangle m(\bar{v}); e) \quad \Delta; \Delta'; \Gamma; \Gamma' \vdash fr : U \quad \langle \bar{\alpha} \triangleleft \bar{B} \rangle \ T \ m(\bar{v} \ \bar{x}) 
                                                                                                         \Delta; \Delta'; \Gamma; \Gamma' \vdash fr : T[\bar{q}/\bar{\alpha}] \rightarrow U
Well-typed stacks, \Delta; \Gamma \vdash s: ok and \Delta; \Gamma \vdash s: T \rightarrow ok:
                 \Delta \vdash \Gamma.T: ok
                                                                                                     \Delta;\Delta';\Gamma;\Gamma'\vdash fr:T\quad \Delta;\Gamma\vdash s:T\rightarrow \mathsf{ok}\qquad \Delta;\Delta';\Gamma;\Gamma'\vdash fr:T\rightarrow U\quad \Delta;\Gamma\vdash s:U\rightarrow \mathsf{ok}
 \Delta;\Gamma \vdash \mathsf{nil}:T \to \mathsf{ok}
                                                                                                                                                        \Delta, \Delta'; \Gamma, \Gamma' \vdash fr :: s : ok
                                                                                                                                                                                                                                                                                                                                                                                       \Delta, \Delta'; \Gamma, \Gamma' \vdash fr :: s : T \rightarrow \mathsf{ok}
Well-typed objects, \Delta; \Gamma \vdash obj : T:
                                                                                                                                                                                                                                                                                                                             Well-typed heaps, \Delta; \Gamma \vdash h: ok:
 {\tt class}\, C\, \{\,\bar{T}\,\bar{f}\,\} \quad \Delta; \Gamma \vdash \bar{{\tt v}}: \bar{T}[q/{\tt myaccess}]
                                                                                                                                                                                                                                                                                                                                \mathsf{dom}(\Gamma) = \mathsf{dom}(h) \quad (\forall n \in \mathsf{dom}(h))(\Delta; \Gamma \vdash h(n) : \Gamma(n))
                                                             \Delta;\Gamma \vdash q\,\{\bar{f}\,{=}\,\bar{\mathtt{v}}\}:q\,C
                                                                                                                                                                                                                                                                                                                                                                                                                                                 \Delta;\Gamma \vdash h: ok
Well-typed token pools, \Delta \vdash t: ok:
                                                                                                                                                                                                                                                                                                                               Well-typed configurations, cfg: ok:
 \mathsf{dom}(\Delta) = \mathsf{dom}(t) \quad (\forall n \in t) (\Delta \vdash n : \mathsf{Token})
                                                                                                                                                                                                                                                                                                                                \Delta; \Gamma \vdash s : \mathsf{ok} \quad \Delta; \Gamma \vdash h : \mathsf{ok} \quad \Delta \vdash t : \mathsf{ok}
                                                                                             \Delta \vdash t : \mathsf{ok}
                                                                                                                                                                                                                                                                                                                                                                                                             s, h, t: ok
```

Fig. 7. Typing rules for configurations

Soundness. We extend the type system to configurations, as shown in Figure 7. The judgment for stack frames has the format $\Delta; \Delta'; \Gamma; \Gamma' \vdash fr : T$. The type T is the type of the return value. Whereas Δ and Γ account for tokens and objects that are known to stack frames below fr, the environments Δ' and Γ' account for tokens and objects that have been generated in fr or in stack frames that were previously above fr and have been popped off the stack. The premise $dom(\delta) \subseteq dom(\Delta')$ in the first typing rule for stack frames captures formally that the commit-environment for the top frame never contains initialization tokens that have been generated in the rest of the stack. This is important for the soundness of (Commit). Another judgment for stack frames has the form $\Delta; \Delta'; \Gamma; \Gamma' \vdash fr : T \to U$. Intuitively, it holds when $\Delta; \Delta'; \Gamma; \Gamma' \vdash fr : U$ and in addition fr currently waits for the termination of a method call that returns a value of type T.

We can now prove the following preservation theorem:

Theorem 1 (**Preservation**). *If*
$$cfg$$
 : ok and $cfg \rightarrow cfg'$, then cfg' : ok.

The proof of the preservation theorem is mostly routine and contained in the companion report [17]. The following theorem says that the type system is sound for object immutability: *well-typed programs never write to fields of* Rd-*objects*. The theorem is a simple corollary of the preservation theorem and the fact that a configuration is ill-typed when the head expression of its top frame instructs to write to a field of a Rd-object.

Theorem 2 (Soundness for Object Immutability). *If*
$$cfg$$
 : ok, $cfg \rightarrow^* (\sigma, v. f = w; e) :: s, h, t \ and \ \sigma(v) = n, \ then \ \pi_1(h(n)) \neq \text{Rd}.$

3.4 Local Annotation Inference

Figure 8 presents the syntax for annotation-free expressions E, as obtained from the expression syntax by omitting the specification statements newtoken and commit, as

well as the qualifier arguments at call sites and the qualifier annotations at object creation sites. The function $e \mapsto |e|$ erases specification commands and annotations from annotated expressions. This section presents an algorithm that infers the erased information, deciding the following question: Given Δ, Γ, E, T such that $\Delta \vdash \Gamma, T$: ok. Are there e, Γ' such that |e| = E and $\Delta \vdash \{\Gamma, \emptyset\}e : T\{\Gamma', \emptyset\}$?

We have proven that our algorithm answers this question soundly: if the inference algorithm answers "yes", then the answer to this question is indeed "yes". We believe that the converse also holds (completeness), but cannot claim a rigorous proof. The algorithm constructs an annotated expression e whose erasure is E. An implementation does not have to really construct e, because knowing that e exists suffices. There are, of course, many annotated expressions that erase to the same annotation-free expression. So what is the strategy for inserting the specification commands without restricting generality? Conceptually, the algorithm parses the unannotated E from left to right, inserting specification commands newtoken and commit as needed.

Inserting Commits. For commits, we use a lazy strategy and only insert a commit if this is strictly necessary. For instance, we never insert commits in front of local variable assignment, because commits and local variable assignments can always be commuted without breaking well-typedness or changing the erasure. The spots where commits do get inserted are: (1) in front of field assignments when a value of type Fresh(n) is assigned to a field of type q where $q \neq Fresh(n)$, (2) in front of method calls when the method signature forces to commit types of arguments, (3) in front of the return value when the return type forces to commit the type of the return value, (4) at the end of conditional branches to match commits that have been performed in the other branch, (5) at the end of loop bodies (for tokens generated inside the loop) to establish the loop invariant, and (6) in front of loop entries (for tokens generated outside the loop) to establish the loop invariant. Consider the following example with a while-loop:

```
void r(Rd C x); void w(RdWr C x); <a < Writeable> f (a C x);
C x; x = new C; while x ( f(x); w(x); );
Generated annotated expression:
newtoken m; newtoken n; C x; x = new Fresh(n) C;
commit Fresh(n) as RdWr; while x ( <RdWr>f(x); w(x); );
commit Fresh(m) as Any;
```

In the above expression, the method call w(x) inside the loop body forces a commit in front of the loop.¹⁰ In contrast, the following expression does not typecheck, because the loop body forces x to have both a Writeable type and type Rd, which is impossible.

```
C x; x = new C; while x ( f(x); r(x); ); // TYPE ERROR
```

One could deal with while-loops by a fixed point computation that requires two iterations over the loop body, one to discover a candidate loop invariant and another one to check if the candidate grants the access permissions required by the loop body. Our algorithm is syntax-directed, because this is simpler to implement on top of the JSR 308 checkers framework [23].

¹⁰ Technically, the inference algorithm delays the generation of the prefix newtoken m; newtoken n; and the postfix commit Fresh(m) as Any. These get inserted at the top level, see Theorem 3.

```
\begin{split} E \in \mathsf{AfreeExp} &::= v \mid C \ x; E \mid H; E \qquad (annotation\text{-}free \ expressions) \\ H \in \mathsf{AfreeHdExp} &::= x = v \mid x = v, f \mid v, f = v \mid x = m(\bar{v}) \mid (annotation\text{-}free \ head \ expressions) \\ x = \mathsf{new} \ C \mid \mathsf{if} \ v \ E \ E \mid \mathsf{while} \ v \ E \\ |\cdot| : \mathsf{Exp} \to \mathsf{AfreeExp} \\ |v| \stackrel{\triangle}{=} v \mid C \ x; e | \stackrel{\triangle}{=} C \ x; |e| \quad |\mathsf{newtoken} \ n; e | \stackrel{\triangle}{=} |e| \quad |\mathsf{commitFresh}(n) \ \mathsf{as} \ q; e | \stackrel{\triangle}{=} |e| \\ |h; e| \stackrel{\triangle}{=} |h|; |e|, \ \mathsf{if} \ h \neq \mathsf{commitFresh}(.) \ \mathsf{as} \ . \\ |\cdot| : \mathsf{HdExp} \to \mathsf{AfreeHdExp} \\ |x = <\overline{q} > m(\bar{v}) \mid \stackrel{\triangle}{=} x = m(\bar{v}) \quad |x = \mathsf{new} \ q \ C | \stackrel{\triangle}{=} x = \mathsf{new} \ C \quad |\mathsf{if} \ v \ E \ | \stackrel{\triangle}{=} \mathsf{if} \ v \ |E| \ |E'| \\ |\mathsf{while} \ v \ E \mid \stackrel{\triangle}{=} \mathsf{while} \ v \ |E| \quad |h| \stackrel{\triangle}{=} h, \ \mathsf{otherwise} \end{split}
```

Fig. 8. Annotation-free expressions and erasure

Generating Tokens. Concerning the generation of initialization tokens, there are two questions to answer. Firstly, when does the algorithm generate new initialization tokens, and secondly, where does the algorithm insert the newtoken statements that bind the tokens. Generation happens (1) at variable declaration sites, (2) at object creation sites, and (3) at call sites for instantiation of qualifier parameters that occur in the method return type but not in the method parameter types. At such sites, the algorithm generates a new token n and uses Fresh(n) as the type of the newly declared variable, the newly created object or the method return value. In the above example, n and n are the tokens that were generated at the variable declaration site for n and at the object creation site that follows it. Note that tokens generated at variable creation sites often do not occur in the program text. Using Fresh(n) as the qualifier for newly created objects (and similarly for variable declarations and method returns) is no restriction, because the following type- and erasure-preserving transformation replaces qualifiers n at object creation sites by Fresh(n):

```
x=\text{new }q\ C\ 	o\ \text{newtoken }n; x=\text{new Fresh}(n)\ C; \text{commit Fresh}(n)\ \text{as }q
```

As for where to insert newtoken, observe that these can always be pulled out of conditional branches by the following type- and erasure-preserving transformation:

```
if v (newtoken n; e) e' \to \text{newtoken } n; \text{if } v \in (e'; \text{commit Fresh}(n) \text{ as } \delta(n);) where \delta is the commit environment in the postcondition of e (as found in the type derivation)
```

We cannot pull newtoken out of loops, though, because the typing rules prevent loop bodies to commit tokens that were generated outside the loop. Consider the following variation of the earlier example:

```
C x; while x (x = new C; f(x); r(x););
```

In contrast to the erroneous expression further up, this expression is well-typed. The inference algorithm generates the following annotated expression for it:

```
newtoken m; C x; commit Fresh(m) as Rd; while x (
  newtoken n; x = new Fresh(n) C; <Fresh(n)>f(x);
  commit Fresh(n) as Rd; r(x); );
```

The newtoken command commutes with all other commands, and therefore the inference algorithm generates newtoken at the beginning of loop bodies only (leaving token generation at the beginning of method bodies implicit).

Fig. 9. Helpers

Subqualifying Constraints. To deal with subqualifying the inference algorithm generates subqualifying constraints. We extend qualifiers by existential variables:

```
?\alpha \in ExVar (existential variables) p,q \in Qual ::= \cdots \mid ?\alpha \quad \Delta \vdash ?\alpha \triangleleft Qual
```

We partition the set of qualifiers into the sets PQual of *persistent qualifiers* and TQual of *transient qualifiers*:

$$\mathsf{TQual} \triangleq \{\mathsf{Fresh}(n) \mid n \in \mathsf{Name}\} \qquad \mathsf{PQual} \triangleq \mathsf{Qual} \setminus \mathsf{TQual}$$

A substitution is a function from existential variables to closed persistent qualifiers:

$$\rho \in \mathsf{Subst} \stackrel{\scriptscriptstyle\Delta}{=} \mathsf{ExVar} \rightharpoonup (\mathsf{PQual} \setminus \mathsf{ExVar})$$

Note that existential variables range over persistent qualifiers only. Substitutions ρ induce functions $\hat{\rho}$ in PQual \rightarrow PQual: $\hat{\rho}(?\alpha) = \rho(?\alpha)$ if $?\alpha \in \text{dom}(\rho)$; $\hat{\rho}(q) = q$ otherwise. Let $\hat{\rho}(T)$ (resp. $\hat{\rho}(e)$) denote the type (resp. expression) obtained by substituting all qualifier occurrences q by $\hat{\rho}(q)$. We omit the hat when no ambiguities arise.

A constraint set contains pairs of the forms (q, B) and (p, q):

```
C \in \mathsf{Constraints} \stackrel{\Delta}{=} \mathsf{SetOf}(\mathsf{PQual} \times \mathsf{QualBound} \cup \mathsf{PQual} \times \mathsf{PQual})
```

A Δ -solution of a constraint set C is substitution ρ such that $\Delta \vdash \rho(q) \triangleleft B$ and $\rho(p) <: \rho(q)$ for all (q, B), (p, q) in C.

Inference Algorithm. The inference judgment has the following format, where ts, Γ , δ_{pre} and T are inherited attributes, and the other attributes are synthesized.

$$ts; \Gamma \vdash E : T \Downarrow (\Gamma', \delta, ts', t, C)^{\mathsf{for}(\delta_{pre} \vdash e)}$$

The synthesized annotated expression e is such that |E| = e. An implementation does not need to compute e or track δ_{pre} , as the other attributes do not depend on them.

- (Γ, δ_{pre}) represents the precondition for e.
- $(\Gamma', (\delta_{pre}; \delta))$ represents the postcondition for *e*.
- ts contains the tokens in scope before e. ts has a stack structure that reflects the nesting of enclosing while loops.
- -ts' contains the tokens in scope after e.
- t contains all tokens n in rest(ts') such that the type derivation for e has a leaf of the form $\Delta \vdash Fresh(n) \triangleleft Writeable$. These tokens must be tracked because they cannot be committed to Rd in front of enclosing while-loops. (See the example on page 19.)
- C are the subqualifying constraints required for well-typedness of e.

For the details of the inference algorithm we refer to our report [17], where the following soundness theorem is proven:

Theorem 3 (Soundness of Inference). Suppose $\operatorname{ran}(\Delta) \subseteq \operatorname{QualBound}$, $(\Delta \vdash \Gamma, T : \operatorname{ok})$, Γ , T do not contain existential variables, \emptyset ; $\Gamma \vdash E : T \Downarrow (\Gamma', _, t, _, \mathcal{C})^{\operatorname{for}(\emptyset \vdash e)}$ and ρ Δ -solves \mathcal{C} . Then $(\Delta \vdash \{\Gamma,\emptyset\} \operatorname{newtokens}(t); \rho(e); \operatorname{commit}(\delta) : T\{(\delta;\rho) \circ \Gamma',\emptyset\})$ for $\delta = \{(n,\operatorname{Any}) \mid n \in t, \hat{\delta}(n) = \operatorname{Fresh}(n)\}$.

4 Related Work

Immutability. Our type system supports class immutability, object immutability, and read-only references, allows flexible object initialization, and is simple and direct (building only on the access qualifiers Rd, RdWr and Any). To the best of our knowledge, no existing type system for a Java-like language meets all these goals at once: Our earlier system Jimuva [18] supports object immutability and open-world class immutability, but requires immutable objects to be initialized inside constructors and does not meet the goal of simplicity and directness, as it requires ownership types, effect annotations and anonymity annotations in addition to access qualifiers. IGJ [34] is simple, direct and supports both object immutability and read-only references, but requires immutable objects to be initialized inside constructors and its support for deep immutability is limited. For instance, IGJ has no way of enforcing that the character array inside an immutable string is part of the string and should thus be immutable. This would either require immutable arrays or a special treatment of owned mutable subobjects, neither of which IGJ supports¹¹. SafeJava [4] and Joe₃ [22] are ownership type systems that support immutable objects with long initialization phases, where the transition from "uninitialized" to "initialized" is allowed through unique object references. In order to maintain uniqueness they use destructive reads, which is a rather unnatural programming style in Java-like languages. These systems build on top of expressive ownership type systems, thus violating our design goals of simplicity and directness. Frozen objects [20] support immutable objects with long initialization phases, but builds on the Boogie verification methodology [1], so is not suitable for an independent pluggable type system. The Universe type system [21] features read-only references. In particular, Generic Universe Types [12] support covariant class parameters if the main modifier of the supertype is Any (which is essentially what we and IGJ [34] do).

Unkel and Lam [31] automatically infer stationary fields, i.e., fields that may turn immutable outside constructors and after previous assignments, and thus are not necessarily final. Their fully automatic analysis requires the whole program. It only detects fields that turn stationary before their objects have been written to the heap, and is in this respect more restrictive than our system, which can deal with stack-local *regions*, as needed for initializing cyclic structures. On the other hand, our system only works at the granularity of objects. Interestingly, non-final stationary fields are reportedly much more common than final fields.

Our system does not address *temporary immutability*, which would require heavier techniques in order to track aliasing on the heap. On an experimental level, statically

¹¹ IGJ supports immutable arrays initialized by array initializers. This is not enough to check the String-constructor String(char[] c), because the length of c is not known statically.

checking temporary immutability has been addressed by Pechtchanski and Sarkar [24]. On a theoretical level, it is very nicely supported by fractional permissions [5].

Object confinement and ownership. For open-world class immutability, we use qualifier polymorphism to express several confinement properties. Firstly, we express a variant of so-called anonymous methods [32] in terms of qualifier polymorphism. Anonymous methods do not write this to the heap. Our variant of anonymity for constructors of immutable classes is slightly weaker and forbids that this is written to the heap outside the Fresh region in which the instance of the immutable class is constructed. Secondly, by combining the myaccess class parameter with conditions on method types, we can express that representation objects of immutable objects are encapsulated, thus avoiding the need to include both access qualifiers and ownership annotations in the system. To this end, we make use of qualifier-polymorphic methods, similar to owner-polymorphic methods in ownership type systems [9,4,33,27,18].

It is not clear if the myaccess parameter alone is enough to express tree-structured ownership hierarchies in general, as facilitated in parametric ownership type systems (e.g., [8], [4]) through instantiating the owner class parameter by rep or this, and in the Universe type system [21] through the rep-modifier. Potanin's system FGJ+c for package-level confinement [26] is based on a static set of owner constants (formally similar to Rd and RdWr but without the additional access semantics). It seems that very similar confinement properties as in FGJ+c could be expressed purely in terms of qualifier-polymorphic methods and without the owner constants. A subtle difference, however, is this: FGJ+c, as most ownership type systems, allows methods to return confined objects, ensuring safety by preventing "outside" class clients from calling such methods. Our system, on the other hand, prevents methods from returning confined objects in the first place. In an open world, where class clients may not follow the rules of the pluggable type system, the latter is the only safe choice.

Type systems for flexible object initialization. There are several articles on initialization techniques for non-nullness type systems [13,14,28]. Fähndrich and Xia's system of "delayed types" [14] is most closely related to our work, like us using lexically scoped regions for safe typestate changes, and using a class parameter representing a "delay time", similar to our myaccess parameter. Unlike us, Fähndrich and Xia do not address local annotation inference. Our system is considerably simpler than theirs, because the initialization problem for immutability seems inherently simpler than the initialization problem for object invariants. Intuitively, there are two reasons for this: Firstly, whereas for object immutability the end of the initialization phase is merely associated with the disposal of a write permission, for object invariants it is associated with an *obligation* to prove the invariant. Secondly, a major complication in [14] is the need to permit inserting uninitialized objects into initialized data structures. This is essential to satisfactorily support cyclic data structures, but requires the use of existential types. Fortunately, this complication does not arise for immutability, because no objects (whether uninitialized or not) ever get inserted into *immutable* data structures.

J\mask [28] is a type-and-effect system for reasoning about object initialization. It is based on a rich language for specifying partial object initialization, including primitives for expressing that fields may or must be uninitialized, as well as conditional assertions. It is designed to guarantee that well-typed programs never read uninitial-

ized fields. It is not designed for immutability, and consequently offers no support for specifying deep immutability or object confinement, as needed for object and class immutability. J\mask (based on a rich specification language for partial object initialization) is quite different in nature to Fähndrich and Xia's delayed types (based on a variant of lexically scoped regions combined with dependent types). Qi and Myers rightly claim that J\mask supports some initialization patterns that delayed types do not, giving bottom-up initialization of trees with parent pointers as an example where delayed types cannot establish object invariants in the required order. This example causes no problems for our immutability system, see Figure 3. In fact, our annotations for this example avoid conditional assertions and are thus simpler than J\mask's (but this comparison is not quite fair, as J\mask and our system have different goals).

Lexically scoped regions. Stack-local regions are closely related to lexically scoped regions [30] for region-based memory management (see also [16]). Whereas, in region-based memory management, lexical scoping is used to statically determine when memory regions can safely be deallocated, here we use it to statically determine when the types of memory regions can safely be changed. Lexically scoped regions do not have a separate commit-statement, but associate the end of region lifetimes with the end of region name scopes. We opted for a separate commit-statement, because it simplifies the description of our inference algorithm, which works by a left-to-right pass over the abstract syntax tree, inserting commits when field or method types enforce this.

5 Conclusion

We presented a pluggable type system for immutable classes, immutable objects, and read-only references. The system supports flexible initialization outside constructors by means of stack-local regions. Our system shows, for the first time, that support for the various forms of immutability, including open-world class immutability, is possible without building on top of an expressive ownership type system (though the class parameter myaccess effectively provides some notion of confinement) and without using effect annotations or unique references. A lesson we have learned is that parametric qualifier polymorphism is a very expressive tool, both for flexibility and confinement.

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