

# Concealing KETJE

## A Lightweight PUF-based Privacy Preserving Authentication Protocol

*Master's Thesis*

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*Abstract*

We enroll more and more personal pervasive devices because these simplify our everyday lives. In order to verify the identity of these devices we use authentication protocols. Although simple authentication often suffices, users would like to remain anonymous during these authentications. Many privacy-preserving authentication protocols have been proposed that claim security and privacy. However, most of them are vulnerable in either their design or their proof of concept.

In this research, we focus on the design of a novel authentication protocol that preserves the privacy of embedded devices. A Physically Unclonable Function (PUF) generates challenge-response pairs that form the source of authenticity between a server and multiple devices. We rely on Authenticated Encryption (AE) for confidentiality, integrity and authenticity of the messages. A challenge updating mechanism combined with an authenticate-before-identify strategy is used to provide privacy. The major advantage of the proposed method is that no shared secrets need to be stored into the device's non-volatile memory. We design a protocol that supports server authenticity, device authenticity, device privacy, and memory disclosure. Following, we prove that the protocol is secure, and forward and backward privacy-preserving via game transformations. Moreover, a proof of concept is presented that uses a 3-1 Double Arbiter PUF, a concatenation of repetition and BCH error-correcting codes, and the AE-scheme KETJE. We show that our device implementation utilizes 8,305 LUTs on a 28 nm Xilinx Zynq XC7Z020 System on Chip (SoC) and takes only 0.63 ms to perform an authentication operation.



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Before you lies the hard work of not only one person but many. As you read it, you will find a wide range of topics, techniques and evaluation methods all boiling down to one authentication protocol. I am content with the way it turned out, I had a steep learning curve tackling all the problems. I would like to take this opportunity now to thank everyone involved.

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CHAPTER

**ONE**

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INTRODUCTION

## 1.1 Introduction

Nowadays, RFID-technology and the Internet of Things (IoT) are hot topics due to the increasing desire to simplify our everyday lives via pervasive devices. Hence, we see a shift from simple identification of devices towards complex authentication protocols, in which a challenging feature to implement is the protection of the entity's privacy. Because these entities belong to individuals who may want to preserve their privacy, we notice a shift on focusing more on privacy-preserving authentication protocols [17]. With the use of state-of-the-art cryptographic techniques, device-to-server authentication can be implemented while protecting the privacy with respect to outsiders.

One solution is to use Symmetric Key Cryptography (SKC), with a pre-shared key (PSK) and a key-updating mechanism in order to randomize device credentials at each successful authentication [33]. However, storing these PSKs requires Non-Volatile Memory (NVM) which, in the field of Hardware Security, is considered to be easily compromised by an attacker. Another option is to use Physically Unclonable Functions (PUFs), physical entities that are similar to algorithmic one-way functions. PUFs act on challenges, returning noisy PUF responses that are close enough between equal PUF instances, but far enough between different PUF instances. Using PUFs, one can refrain from storing a PSK in the device's NVM. Instead, one only needs to store a challenge which, similar to the aforementioned construction, is updated on a successful authentication. The strength of this construction is that these challenges are not secret and can safely be stored in NVM. By using a PUF, one needs to implement a Fuzzy Extractor (FE) that can produce an unpredictable key from the non-uniform and noisy PUF responses. On top of that, the FE provides for the recovery of old PUF responses from fresh PUF responses using error-correcting codes.

In order to cover the need for anonymous authentication in the IoT, research has to be done into lightweight privacy-preserving authentication protocols. A PUF-based privacy-preserving authentication protocol might be the solution. However, no such protocol exists yet that both claims security and privacy, and presents a secure proof of concept.

## 1.2 Related Work

PUFs were first introduced as *physical random functions* by Pappu et al. [52]. Since then, many PUF constructions have been proposed [27, 30, 36, 22, 62]. Maes researched PUFs for his PhD thesis, in which he gives a thorough explanation of PUF constructions, properties and applications [42]. More recent, Machida et al. proposed a 3-1 Double Arbiter PUF (DAPUF) which substantially decreases the prediction rate of delay-based Strong<sup>1</sup> PUF responses [39].

---

<sup>1</sup>In contrast to a Weak PUF that can only generate a limited amount of responses, a Strong PUF can generate  $2^l$  Challenge-Response Pairs (CRPs), where  $l$  is the number of bits in the challenge.

Many PUF based protocols have been proposed [44, 29, 48, 3]. Majzoobi et al. propose the Slender PUF protocol, an efficient and secure method to authenticate the responses generated from a Strong PUF [44]. Their protocol does not rely on FEs and error-correcting codes because response fragments are authenticated using statistical methods. However, as Delvaux et al. pointed out, the implementation of the Slender protocol is subjected to Pseudo-Random Number Generator (PRNG) exploitation [17]. Herrewewege et al. propose a reversed FE, putting the computationally less complex generation procedure in the device, and the more complex reproduction procedure on the server [29]. However less severe than the exploit in the Slender protocol, their proof of concept is also subjected to a PRNG issue [17]. Moriyama et al. propose a provably secure privacy-preserving authentication protocol that uses a different PUF response at every authentication, and thus changing the device credential after every successful authentication [48]. Aysu et al. [3] propose a provably secure protocol based on the protocols by Herrewewege et al. and Moriyama et al.. Their protocol is optimized for resource-constrained platforms like Radio-Frequency Identification (RFID) devices. The authors evaluate the design using a PUF and True Random Number Generator (TRNG) based on Static Random-Access Memory (SRAM), a Pseudo-Random Function (PRF) using the SIMON block-cipher and a Reverse FE (RFE) based on Bose-Chaudhuri-Hocquenghem (BCH) codes. While this is the first effort to describe an end-to-end design and evaluation of a provable secure privacy-preserving PUF-based authentication protocol, their interleaved FE construction is vulnerable to linear equation analysis [3, p. 12]. Moreover, the authors use an additional PSK that does not increase the entropy of the communicated messages. Thus, this additional PSK can be considered overhead.

### 1.3 Scope and Contributions

This research focusses on improving the results of the most recent, aforementioned PUF-based privacy-preserving authentication protocol as proposed by Aysu et al. [3]. We do this by integrating a single, compact cryptographic primitive, namely Authenticated Encryption (AE), into a PUF-based privacy-preserving authentication protocol. In contrast to the protocol by Aysu et al., we aim to construct a secure FE and aim to abstain from using a PSK between server and devices. With this, we hope to improve the overall efficiency of the protocol. Therefore, our main research question is:

*How does the integration of Authenticated Encryption in a PUF-based privacy-preserving authentication protocol affect its performance in relation to other similar, existing authentication protocols?*

For this, we design, prove and implement a novel PUF-based privacy-preserving authentication protocol using AE. We summarize our contributions as follows:

- We present the theoretical design of a novel PUF-based privacy-preserving authentication protocol using AE. By doing this we present a generic approach to create any implementation of the protocol provided the quality of PUF responses.

- We prove that the proposed protocol is mathematically secure, and forward and backward privacy-preserving, under the condition on the security of the AE-scheme and the quality of the PUF responses. For this we define a new type of Strong Extractor (SE), the Entropy Accumulator (EA), which is part of the FE.
- We present a proof of concept of the device on a development board and the server on a PC such that we can elaborate on the performance of the end-to-end design of the protocol. By doing this we present one of the first use-cases of the lightweight AEAD-scheme KETJE, which is part of the running Competition for Authenticated Encryption: Security, Applicability and Robustness (CAESAR).
- We make a comparison of the proposed protocol's performance with other similar, existing authentication protocols.
- We argue about the applicability of the proposed protocol in RFID-technology and the IoT.

## 1.4 Research Methodology

In order to answer our research question, we use the following research methodology:

- *Literature study.* We carry out a literature study towards authentication protocols in general, and the techniques used in the PUF-based privacy-preserving authentication protocol by Aysu et al. [3] in particular. Moreover, we study techniques that might improve the performance and security of the protocol.
- *Theoretical design.* Based on the literature study, we design a PUF-based privacy-preserving authentication protocol using AE. The aim is to replace the Symmetric Key Encryption (SKE) and the PRF from Aysu et al. [3] with a single, compact cryptographic primitive (Authenticated Encryption with Associated Data (AEAD)) that provides for confidentiality of the PUF responses, authenticity of the devices and the server, and integrity of the transmitted data. Moreover, a secure PUF needs to be selected that forms the basis for the design of a FE in particular and the protocol in general.
- *Mathematical proof.* We think that a novel protocol should be provably secure and privacy-preserving. Hence, we give mathematical proof for both the security as well as forward and backward privacy.
- *Proof of concept.* In order to evaluate the performance of the proposed protocol, we physically implement the device on a development board. On top of that, we implement the server on a PC such that we create an end-to-end design.

## 1.5 Relevance

As mentioned before, RFID-technology and the IoT is emerging. While the technology often is not new, by interconnecting devices and entities in the World Wide Web (WWW), we create a new type of web, the World-Sized Web (WSW) [60]. In this WSW devices and entities are moving through the network, roaming from access point to access point. One might consider that without proper privacy-preserving authentication protocols, data gets leaked about the specific devices and their locations in time. This traceability is a concern that affects everyone. To illustrate this, the Open Web Application Security Project (OWASP) has introduced a Top 10 IoT vulnerabilities, in which in the fifth place, there is “Privacy Concerns” and in the second place, there is “Insufficient Authentication/Authorization” [51]. This shows that the online community realizes effort should be devoted to both aspects of lightweight privacy-preserving authentication protocols, namely privacy and authentication.

On the other hand, one might consider conventional use-cases for RFID-technology, e.g. in supply chains or in access control. In these scenarios, the amount of devices is substantially reduced in comparison with the IoT. However, a company might want to disclose articles that wear RFID tags and their locations to competitors. Also, in access control, organizations might want to disclose to outsiders what key figures entered where at what times. This demands for a lightweight privacy-preserving authentication protocol.

In addition, this thesis is written in the partial fulfillment of the requirements for the degree Master of Computing Science in Software Science. With this work the author shows his skills in writing, reasoning, specifying, building and managing a project.

## 1.6 External Validity

As mentioned, since the introduction of PUFs, many authentication protocols have been proposed that rely on key generation by PUFs. However, many of them were either not provably secure or were insecure in their proof of concept. Depending on how successful this research proves to be, the protocol can be implemented in nodes in the IoT, or on a smaller scale in RFID devices in conventional use-cases. With the protocol, a generic approach is presented to construct any instance of the protocol provided the quality of the PUF responses, the desired maximum failure rate for the authentications and the desired security level. A designer can choose which PUF to use, which error-correcting codes and which AEAD-scheme. This way, the protocol might prove useful for a variety of applications.

In order to validate this research externally, a 20-page paper is submitted to the Fifth International Workshop on Lightweight Cryptography for Security & Privacy (LightSec 2016, Aksaray University, Cappadocia, Turkey).

## 1.7 Outline

In Chapter 2 we describe the theoretical foundation for further chapters. This chapter starts by giving notation and preliminaries before describing and defining PUFs, error-correcting codes, FEs and AE. In Chapter 3 we describe the proposed privacy-preserving authentication protocol, which we call the Concealing KETJE Protocol (CKP), named after the lightweight AEAD-scheme KETJE. This chapter starts by defining the security considerations before presenting the CKP with all of its elements. In Chapter 4 we first describe the security model and formal security definitions before presenting the security and privacy proof of the proposed protocol. In Chapter 5 we describe a proof of concept of the CKP. Chapter 6 both describes the results from the protocol as supported by the mathematical foundation as well as the results from the protocol supported by the proof of concept. Finally, in Chapter 7 we present the conclusions, discussion and future work.



## BACKGROUND

In this chapter we describe the theoretical foundation for further chapters. The information includes notation and preliminaries as well as theoretical background on the topics addressed in this thesis.

We start by describing the notation that is used throughout this thesis in Section 2.1. Section 2.2 describes the preliminaries. Following, in Section 2.3 we describe Physically Unclonable Functions (PUFs), which is the component that forms the basis of our privacy-preserving authentication protocol. Section 2.4 describes repetition codes and Bose-Chaudhuri-Hocquenghem (BCH) codes, two error-correcting codes that are being used in the Fuzzy Extractor (FE), which is one of the main components in our protocol. FEs are being described in Section 2.5. The chapter concludes in Section 2.6 by describing Authenticated Encryption (AE) in general and Authenticated Encryption with Associated Data (AEAD) in particular.

## 2.1 Notation

In this section we describe the general notation that is used throughout this thesis. For a detailed description of the specific notation used, please consult the Nomenclature starting at page 95. We use notation from Cryptography [33, 56], Coding Theory [47, 63, 41, 28] and Information Theory [61, 55], the three theoretical foundations our protocol is mainly based on. In general, we use the following notation:

- Classes and sets are denoted by calligraphic letters, e.g.  $\mathcal{A}, \mathcal{B}, \dots, \mathcal{Z}$ .
- Vectors and (binary) variables/strings are denoted by capitalized roman letters, e.g.  $A \in \mathcal{A}, B \in \mathcal{B}, \dots, Z \in \mathcal{Z}$ .
  - Varying instances of variable  $A$  are identified using superscript (e.g.  $A', A^1$  or  $A^{\text{old}}$ )
  - $A = [1, 1, 0]$  denotes a binary string with characters  $A_0 = 0, A_1 = 1$  and  $A_3 = 1$  with  $\mathbf{a}(x) = x^2 + x$  its polynomial.
  - $B_{2 \rightarrow 0}$  denotes the substring of  $B$  with characters  $B_2, B_1$  and  $B_0$ .
  - $E = C \parallel D$  denotes the concatenation of strings  $C$  and  $D$ .
  - $|F| = n$  denotes the length  $n$ , or the amount of bits of  $F$ .
  - $I = G \oplus H$  denotes the bitwise exclusive-OR (XOR) of strings  $G$  and  $H$ .
  - $\langle J, K \rangle$  denotes a tuple of strings  $J$  and  $K$ .
- Functions are either denoted by **function**( $\cdot, \dots, \cdot$ ), where  $\cdot$  denotes an input to the function, or by calligraphic letters similar to sets<sup>1</sup>.

## 2.2 Preliminaries

In this section we give the preliminary definitions that are being used throughout this thesis. Again, we use definitions from Cryptography [33, 56], Coding Theory [47, 63, 41, 28] and Information Theory [61, 55]. We define the Hamming distance and Hamming weight, Shannon entropy, min-entropy and statistical distance.

### 2.2.1 Hamming Distance and Hamming Weight

The Hamming distance, introduced by Hamming [28] is defined as follows:

**Definition 2.1** (Hamming distance). *The Hamming distance  $\mathbf{HD}(Y, Y')$  between two binary vectors  $Y, Y' \leftarrow \mathcal{Y}$  of the same length is the number of positions in both vectors with differing values:*

$$\mathbf{HD}(Y, Y') = |\{i : Y_i \neq Y'_i\}|$$

---

<sup>1</sup>The context in which calligraphic letters are used clearly reveals the denotation.

The distance metric  $\mathbf{dist}(Y, Y')$  over two binary vectors  $Y, Y' \leftarrow \mathcal{Y}$  is defined by the Hamming distance. Similarly, the *Hamming weight* is defined as [28]:

**Definition 2.2** (Hamming weight). *The Hamming weight  $\mathbf{HW}(Y)$  of a vector  $Y \leftarrow \mathcal{Y}$  is the number of positions with non-zero values:*

$$\mathbf{HW}(Y) = |\{i : Y_i \neq 0\}|$$

Note that  $\mathbf{HW}(Y \oplus Y') = \mathbf{HD}(Y, Y')$ .

### 2.2.2 Shannon Entropy

The measurement of entropy we use is *Shannon entropy*, introduced by Shannon [61]:

**Definition 2.3** (Shannon entropy). *The Shannon entropy  $\mathbf{H}(Y)$  of a discrete random variable  $Y \leftarrow \mathcal{Y}$  is defined as:*

$$\mathbf{H}(Y) = - \sum_{Y_i \in \mathcal{Y}} \mathbf{Pr}(Y_i) * \log_2 \mathbf{Pr}(Y_i)$$

The entropy of a binary variable  $Y \leftarrow \{0, 1\}^l$  with probabilities  $\mathbf{Pr}(Y_i = 1) = p$  and  $\mathbf{Pr}(Y_i = 0) = 1 - p$  ( $0 \leq i < l$ ) is defined in the binary entropy function  $\mathbf{h}(p)$ :

$$\mathbf{h}(p) = -p \log_2(p) - (1 - p) \log_2(1 - p) \quad (2.2.1)$$

Sometimes we use an approach that expects the worst outcome to Shannon entropy, which is the min-entropy introduced by Rényi [55]. If  $Y \in \mathcal{Y}$  is uniformly distributed, the Shannon Entropy and min-entropy are equal. However, if this is not the case, the ‘worst-case’ scenario is taken for the min-entropy.

We define the min-entropy as follows [42, p. 206]:

**Definition 2.4** (Min-entropy). *The min-entropy  $\tilde{\mathbf{H}}_\infty(Y)$  of a random variable  $Y \in \mathcal{Y}$  is defined as:*

$$\tilde{\mathbf{H}}_\infty(Y) = -\log_2 \max_{Y_i \in \mathcal{Y}} \mathbf{Pr}(Y_i)$$

### 2.2.3 Statistical Distance

The statistical distance is a measure of distinguishability between two probability distributions (e.g. random variables/vectors/strings).

We define the statistical distance as follows [19, p. 528]:

**Definition 2.5** (Statistical distance). *The statistical distance  $\mathbf{SD}(A, B)$  between two probability distributions  $A$  and  $B$  is:*

$$\mathbf{SD}(A, B) = \frac{1}{2} \sum_{V \in \mathcal{V}} |\Pr(A = V) - \Pr(B = V)|,$$

where  $\Pr(x)$  denotes the probability that  $x$  occurs and  $\mathcal{V}$  denotes the set from which the statistical distance is sampled using  $V$ .

## 2.3 Physically Unclonable Functions

PUFs are entities that are intrinsically embodied in physical structures. The main characteristic of a PUF is that it should be easy to evaluate but hard to predict, moreover, it should be practically impossible to duplicate. Because of its equivalence to algorithmic one-way-functions, PUFs might be ideal for cryptographic purposes.

Although the following definition is somewhat decrepit, we can still use it to illustrate the general idea of a PUF [21, p. 2]:

**Definition 2.6** (Physical Unclonable Function). *A Physical Unclonable Function is a function that maps challenges to responses and that is embodied in a physical object. It satisfies the following properties:*

1. *Easy to evaluate: the physical object can be evaluated in a short amount of time.*
2. *Hard to characterize: from a number of measurements performed in polynomial time, an attacker who no longer has the device and who only has a limited (polynomial) amount of resources can only obtain a negligible amount of knowledge about the response to a challenge that is chosen uniformly at random.*

This definition was superseded by numerous broader and often more complex definitions of which Armknecht et al. [1] try to unify them all. For this thesis, we follow Maes [42] as he covers the main characteristics we need to describe a PUF.

A PUF is mainly characterized by its reproducibility, uniqueness, identifiability, unclonability and unpredictability, which are defined by the intra- and inter-distance of the PUF responses [42, p. 20-23, 61-64].

Before we give these definitions, we first introduce the notion of a PUF class, denoted as  $\mathcal{P}$ , which is the set of PUFs that share the same PUF construction type

(see Section 2.3.5). The set of all possible challenges  $X$  which can be applied to an instance of  $\mathcal{P}$  is denoted as  $\mathcal{X}_{\mathcal{P}}$ .

### 2.3.1 Intra-distance and Reproducibility

When challenging a single PUF multiple times with the same challenge, there is a chance that the response bits are different in both responses. We call the probability that a single bit is different between measurements the bit-error probability  $p_e$ . This is one of the characteristics of a PUF and is defined by its intra-distance, which is defined as follows [42, p. 20]:

**Definition 2.7** (Intra-distance). *A PUF response intra-distance is modeled as a random variable describing the distance between two PUF responses from the same PUF instance using the same challenge:*

$$\mathcal{D}_{\mathbf{puf}_i}^{\text{intra}}(X) = \text{dist}(Y^i \leftarrow \mathbf{puf}_i(X), Y^{i'} \leftarrow \mathbf{puf}_i(X)),$$

with  $Y^i$  and  $Y^{i'}$  two distinct and random evaluations of PUF instance  $\mathbf{puf}_i$  on the same challenge  $X$ . Additionally, the PUF response intra-distance for a random PUF instance and a random challenge is defined as the random variable:

$$\mathcal{D}_{\mathcal{P}}^{\text{intra}} = \mathcal{D}_{\mathbf{puf} \leftarrow \mathcal{P}}^{\text{intra}}(X \leftarrow \mathcal{X}_{\mathcal{P}})$$

The intra-distance provides reproducibility of any unique PUF instance  $\mathbf{puf}_{0 \leq i < n} \in \mathcal{P}$  (where  $n$  is the total number of PUFs in the PUF class  $\mathcal{P}$ ), which means that if two measurements are performed on the same PUF, then these responses are with high probability close to each other. More precisely, reproducibility is defined as follows [42, p. 61]:

**Definition 2.8** (Reproducibility). *A PUF class  $\mathcal{P}$  exhibits reproducibility if:*

$$\Pr(\mathcal{D}_{\mathcal{P}}^{\text{intra}} \text{ is small}) \text{ is high}$$

Note that Maes does not introduce a theoretical or experimental bound. For now, an unbounded perspective suffices. We introduce a theoretical bound  $\epsilon$  in the formal security definitions in Section 4.2 needed for the security and privacy proofs in Section 4.3.

### 2.3.2 Inter-distance and Uniqueness

The inter-distance is defined as follows [42, p. 22]:

**Definition 2.9** (Inter-distance). *A PUF response inter-distance is modeled as a random variable describing the distance between two PUF responses from different PUF instances using the same challenge:*

$$\mathcal{D}_{\mathcal{P}}^{\text{inter}}(X) = \text{dist}(Y \leftarrow \mathbf{puf}(X), Y' \leftarrow \mathbf{puf}'(X)),$$

with  $Y$  and  $Y'$  evaluations of the same challenge  $X$  on two random but distinct PUF instances  $\mathbf{puf} \in \mathcal{P}$  and  $\mathbf{puf}' (\neq \mathbf{puf}) \in \mathcal{P}$ . Additionally, the PUF response inter-distance for a random challenge is defined as the random variable:

$$\mathcal{D}_{\mathcal{P}}^{\text{inter}} = \mathcal{D}_{\mathcal{P}}^{\text{inter}}(X \leftarrow \mathcal{X}_{\mathcal{P}})$$

The inter-distance provides uniqueness of any PUF instance  $\mathbf{puf}_{0 \leq i < n}$  in the PUF class  $\mathcal{P}$  (where  $n$  is the total number of PUFs in the PUF class  $\mathcal{P}$ ), which implies that responses of measurements performed on different PUFs (taking into account that one of the PUFs might be fake) are with high probability far apart. More precisely, uniqueness is defined as follows [42, p. 62]:

**Definition 2.10** (Uniqueness). *A PUF class  $\mathcal{P}$  exhibits uniqueness if:*

$$\Pr(\mathcal{D}_{\mathcal{P}}^{\text{inter}} \text{ is large}) \text{ is high}$$

### 2.3.3 Identifiability

Reproducibility of a PUF instance  $\mathbf{puf}_i \in \mathcal{P}$  and uniqueness between PUF instances  $\mathbf{puf}_i, \mathbf{puf}_j \in \mathcal{P}$  (where  $i \neq j$ ) provides identifiability of PUF instance  $\mathbf{puf}_i \in \mathcal{P}$ . More precisely, identifiability is defined as follows [42, p. 62]:

**Definition 2.11** (Identifiability). *A PUF class  $\mathcal{P}$  exhibits identifiability if it is reproducible and unique, and in particular if:*

$$\Pr(\mathcal{D}_{\mathcal{P}}^{\text{intra}} < \mathcal{D}_{\mathcal{P}}^{\text{inter}}) \text{ is high}$$

### 2.3.4 Unclonability and Unpredictability

For cryptographic applications, unclonability and unpredictability are essential. The characteristic of unclonability assures that physically and technically, a PUF instance  $\mathbf{puf}_{i'} \in \mathcal{P}$  is difficult (or even impossible) to create from an other PUF instance  $\mathbf{puf}_i \in \mathcal{P}$ . More precisely, unclonability is defined as follows [42, p. 63]:

**Definition 2.12** (Unclonability). *A PUF class  $\mathcal{P}$  exhibits unclonability it is hard to apply and/or influence the creation procedure in such a way as to produce two distinct PUF instances  $\mathbf{puf}, \mathbf{puf}' \in \mathcal{P}$  for which it holds that:*

$$\Pr(\text{dist}(Y \leftarrow \mathbf{puf}(X), Y' \leftarrow \mathbf{puf}'(X)) < \mathcal{D}_{\mathcal{P}}^{\text{inter}}(X)) \text{ is high,}$$

for  $X \leftarrow \mathcal{X}_{\mathcal{P}}$ . Ultimately, it should be hard to produce two PUF instances for which it holds that:

$$\Pr(\text{dist}(Y \leftarrow \mathbf{puf}(X), Y' \leftarrow \mathbf{puf}'(X)) > \mathcal{D}_{\mathcal{P}}^{\text{intra}}(X)) \text{ is low}$$

The characteristic of unpredictability ensures that unobserved responses remain sufficiently random, even after observing responses to other challenges on the same PUF instance. More precisely, unpredictability is defined as follows [42, p. 64]:

**Definition 2.13** (Unpredictability). *A PUF class  $\mathcal{P}$  exhibits unpredictability if it is hard to win the following game for a random PUF instance  $\mathbf{puf} \in \mathcal{P}$ :*

- In a learning phase, one is allowed to evaluate  $\mathbf{puf}$  on a limited number of challenges and observe the responses. The set of evaluated challenges is  $\mathcal{X}'_{\mathcal{P}}$  and the challenges are either randomly selected (weak unpredictability) or adaptively chosen (strong unpredictability).
- In a challenging phase, one is presented with a random challenge  $\mathcal{X} \leftarrow \mathcal{X}_{\mathcal{P}} \setminus \mathcal{X}'_{\mathcal{P}}$ . One is required to make a prediction  $Y^{\text{pred}}$  for the response to this challenge when evaluated on  $\mathbf{puf}$ . One does not have access to  $\mathbf{puf}$ , but the prediction is made by an algorithm  $\mathbf{predict}$  which is trained with the knowledge obtained in the learning phase:  $Y^{\text{pred}} \leftarrow \mathbf{predict}(X)$ .
- The game is won if:

$$\Pr(\text{dist}(Y^{\text{pred}} \leftarrow \mathbf{predict}(X), Y \leftarrow \mathbf{puf}(X)) < \mathcal{D}_{\mathcal{P}}^{\text{inter}}(X)) \text{ is high}$$

One way of carrying out this experiment is by using Machine Learning (ML) attacks. Recent studies have shown that PUF responses can be predicted in some practical scenarios [58, 57]. It is evident that a PUF should be designed carefully, taking this risk into account.

### 2.3.5 PUF Construction Types

Various PUF construction types have been proposed, a few of them are being discussed in this section: Static RAM (SRAM) PUFs, Arbiter PUFs, Ring Oscillator PUFs (ROPUFs) and Non-Intrinsic (PUF-like) PUFs [42].

#### 2.3.5.1 SRAM PUFs

SRAM PUFs were first introduced by Guajardo et al. [27] and Holcomb et al. [30]. SRAM PUFs are based on the principle that upon power cycling an SRAM cell, its transient behavior either sets the value of the cell to 0 or 1. This transient behavior is intrinsically introduced due to the random process variations in the production of the cells. Hence, these variations are cell-specific and will (upon power cycling) determine the state of the cell with a high probability to a certain value. This value is called the preferred initial operating point and is introduced by a race condition in the electrical flow upon powering the SRAM. However, once in a while this value will be different from the preferred initial operating point because of the

race condition, which makes SRAM usable in a PUF construction. Challenges and responses can be created by adhering to memory addresses as challenges and the state of the SRAM as the PUF response. Before challenging the PUF with a same challenge (memory address), a power cycle needs to be executed. This construction is closely related to a One-Time Pad (OTP) where addresses are mapped to the state of the SRAM [33]. However, with each power cycle there is a chance that the pad changes from the previous measurement.

### 2.3.5.2 Arbiter PUFs

Figure 2.1 illustrates an Arbiter PUF, a type of delay-based PUF which was first introduced by Lee et al. [36]. Here, the multiplexers that act on the same challenge bit  $C_i$  ( $0 \leq i < n$ ,  $|C| = n$ ) are called a switch block, and the two negative-AND (NAND) ports are called an arbiter. An arbiter PUF is based on the idea that there exists a race condition between signals of two digital paths on an Integrated Circuit (IC). This race condition, or the delay of a path, is introduced by the random process variations in the production of the IC. This behavior makes the measurements of the delays usable in a PUF construction. An arbiter (usually a simple latch) either sets the response to 0 or 1, depending on what signal arrived first at the arbiter. Often, the paths are implemented using switch blocks (usually multiplexers) that act on a challenge bit. These switch blocks either let signals switch from digital paths or keep their paths. By concatenating a number of these switch blocks, a challenge can be sent to the PUF. In order for the response to have sufficient length, a number of these race conditions can be measured in parallel. For example, by measuring  $n$  arbiter PUFs in parallel using the same challenge, a  $n$ -bit response can be obtained. It is evident that this solution substantially increases the area of the IC. Another option is to measure responses sequentially using differing challenges. For example, one could append  $n$  bits to the challenge address space to measure  $2^n$  responses, obtaining a  $2^n$ -bit response. It is evident that this solution substantially increases the latency of PUF responses.

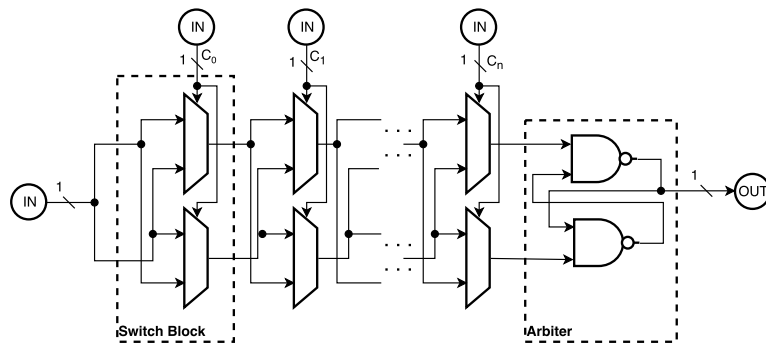


Figure 2.1: An arbiter PUF as introduced by Lee et al. [36].  $\textcircled{\text{IN}}$  denotes the input of the PUF,  $\textcircled{\text{OUT}}$  denotes the output of the PUF.

The responses of these PUFs can easily be predicted using ML-attacks. Machida et al. have shown that conventional arbiter PUFs have a prediction rate of 86%[40]. However, arbiter PUFs are used in various constructions that provide for a good



prediction rate (i.e. approximating 50%). One example is discussed in the next section, various others by Machida et al. [40].

### 2.3.5.3 Ring Oscillator PUFs

Figure 2.2 illustrates a ROPUF, another type of delay-based PUF which was first introduced by Gassend et al. [22]. In this figure, the configurable delay can (for example) be the delay introduced in the arbiter PUF from Section 2.3.5.2 or a series of inverters. This PUF is based on the measurements of the frequencies of digital oscillating circuits. Again, the differences in these measurements are introduced by the random process variations in the production of the IC. Usually, a ROPUF consists of a number of ring oscillators and an equal amount of frequency counters [43]. After measuring the frequencies of these oscillators, an ordering of these frequencies, and an encoding of this ordering reveals a PUF response. A challenge can be introduced by adding multiple oscillators in batches. This challenge, fed to a multiplexer can indicate from which oscillator in the batch the frequency needs to be measured.

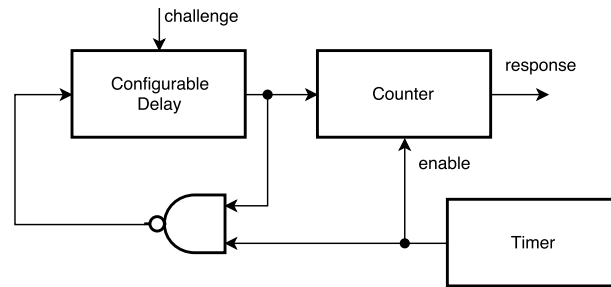


Figure 2.2: A ROPUF as introduced by Gassend et al. [22].

### 2.3.5.4 Non-Intrinsic (PUF-like) PUFs

Various non-intrinsic (PUF)-like PUFs have been proposed that have randomness that has been explicitly introduced. These PUFs are non-intrinsic because they are not completely integrated in an embedding device and/or they are not produced in the standard manufacturing process of their embedding device. Tuyls and Škorić [62] describe optical, coating and acoustic PUFs.

**2.3.5.4.1 Optical PUFs** An optical PUF is based on either absorption, transmission, reflection, scattering or a combination thereof, of a microstructural surface. The idea is that this surface has random variations in one of these characteristics introduced in the production of the surface. These random variations in the microstructural surface can be used in a PUF construction by challenging it at different locations on the surface. An example is to shoot a laser through a transparent material (e.g. glass) and observe the speckle pattern using a camera [62].

**2.3.5.4.2 Coating PUFs** A coating PUF is based on the dielectric variation of the coating of an IC. During manufacturing, the coating is doped with dielectric particles that respond with a different capacitance value on differing voltage inputs with varying frequencies. These differing capacitance values can be used in a PUF construction by challenging the PUF with different voltage inputs.

**2.3.5.4.3 Acoustic PUFs** An acoustic PUF is a PUF that is based on the response of sending an acoustic wave to an object. The acoustic wave propagates through the object and scatters on randomly distributed inhomogeneities that are introduced during manufacturing of the object. These differing wave responses can be used in a PUF construction by pointing the acoustic wave at different locations on the surface of the object as challenges.

## 2.4 Error-Correcting Codes

When sending data over a noisy channel, there is a chance that this data might be corrupted. For example, when sending a single bit, there is a probability  $\Pr(\text{“bit flipped”}) = p$  that this bit gets flipped. This is due to a Binary Symmetric Channel (BSC) [63, p. 2], as depicted in Figure 2.3.

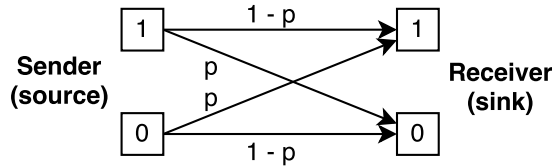


Figure 2.3: The BSC.

In this figure,

$$\Pr(\text{“1 received”} \mid \text{“0 transmitted”}) = \Pr(\text{“0 received”} \mid \text{“1 transmitted”}) = p, \text{ and}$$

$$\Pr(\text{“0 received”} \mid \text{“0 transmitted”}) = \Pr(\text{“1 received”} \mid \text{“1 transmitted”}) = 1 - p.$$

The BSC can be used to model various media, for example the aforementioned noisy channel (tele-communications, satellite communication), a storage medium or PUFs. In this thesis we only consider the BSC in a PUF scenario where multiple measurements on the same challenge return noisy responses. We require that the protocol’s channel is ideal (i.e. no errors occur during communication).

In order to recover the original data from the possibly corrupted data, error-correcting codes are used [41, p. 1]. Error-correcting codes have the ability to correct up to  $t$  bits of original data from the transmitted information.

Although error-correcting codes are often used for transmitted data, we can also use them for reconstructing PUF-responses.

**Example 2.4.1.** Take two of the same PUF challenges  $X$  on the same PUF  $\mathbf{puf}_i$ ,  $Y^i \leftarrow \mathbf{puf}_i(X)$  and  $Y^{i'} \leftarrow \mathbf{puf}'_i(X)$ , with  $Y^i = [0, 1, 0, 1, 0, 1, 1, 0]$  and  $Y^{i'} = [0, 1, 1, 1, 0, 0, 1, 0]$ . This can be seen as the transmission of PUF response  $Y^i$  using the PUF  $\mathbf{puf}_i$  under the influence of a BSC, receiving the PUF response  $Y^{i'}$ . We say that the error vector, indicating which bits have been ‘corrupted’, of these two response vectors is  $E = Y^i \oplus Y^{i'} = [0, 0, 1, 0, 0, 1, 0, 0]$ .  $\triangleleft$

One way of carrying out error correction to the errors that were introduced in the example is to encode the PUF response  $Y^i$  and decode the second PUF response  $Y^{i'}$ . Specific codes used in an encoding have the ability to carry out error detection to the error(s) introduced by a BSC. Error detection leads to error correction, which helps us obtain the PUF response  $Y^i$  in a decoding.

We describe binary repetition codes and binary BCH codes which are used in our proposed protocol to recover PUF responses.

### 2.4.1 Repetition Codes

One of the most basic error-correcting codes is the class of binary repetition codes, or repetition codes. As the name suggests, the codeword for a bit is the repetition of that bit such that probability indicates the original bit in a decoding.

We define binary repetition codes as follows:

**Definition 2.14** (Binary Repetition Code). *A binary linear code  $C_{REP}(n, 1, t)$  with codewords  $\mathbf{0} = [0, 0, \dots, 0]$  and  $\mathbf{1} = [1, 1, \dots, 1]$  is called a binary repetition code of length  $n$  and error correcting capability  $t = \lfloor \frac{n-1}{2} \rfloor$ .*

#### 2.4.1.1 Encoding

As we have mentioned before, the most basic form of encoding a string is by repeating its characters for a number of  $n$  times. There are more advanced techniques of using repetition codes, of which one will be described in Section 3.5.3.1.

**Example 2.4.2.** Take the binary repetition code  $C_{REP}(n, 1, t)$  with  $n = 3$  and  $t = \lfloor \frac{n-1}{2} \rfloor = 1$ . An encoding of the message  $M = [0, 1, 1, 0]$  of length  $l_M = 4$  results in the codeword  $W = [0, 0, 0] \parallel [1, 1, 1] \parallel [1, 1, 1] \parallel [0, 0, 0]$  of length  $l_W = 4 * n = 12$ .  $\triangleleft$

### 2.4.1.2 Decoding

Decoding of a received codeword  $W' = W \oplus E$  of length  $l_{W'}$  and error vector  $E$  is performed by measuring the Hamming weight of the  $n$ -bit substrings of  $W'$ .

Take the binary repetition code  $\mathcal{C}_{\text{REP}}(n, 1, t)$ . Let us say a message  $M$  of length  $l_M$  was encoded using this code. We can decode the received codeword  $W'$  as follows (for  $0 \leq i < l_M$ ):

$$\text{If } \mathbf{HW}(W'_{i \cdot n + (n-1) \rightarrow i \cdot n}) > t \text{ then we take } M_i = 1 \text{ and } M_i = 0 \text{ otherwise. } \quad (2.4.1)$$

This gives the highest probability that the decoding of the substrings represents the original message. There is a chance that the decoding will be faulty, as more than  $t$  bits in the  $n$ -bit string might be corrupted in the channel. The probabilistic foundation of repetition codes does not support detection of this faulty decoding. For this, the more complex BCH codes can be used which will be described in Section 2.4.2.

**Example 2.4.3.** Take the message  $M = [0, 1, 1, 0]$  and the codeword  $W = [0, 0, 0] \parallel [1, 1, 1] \parallel [1, 1, 1] \parallel [0, 0, 0]$  from Example 2.4.2 and an error vector  $E = [0, 0, 0] \parallel [0, 0, 1] \parallel [0, 1, 0] \parallel [1, 0, 1]$ . The received codeword results in  $W' = W \oplus E = [0, 0, 0] \parallel [1, 1, 0] \parallel [1, 0, 1] \parallel [1, 0, 1]$ . Using Formula 2.4.1, a decoding of the received codeword  $W'$  results in the received message  $M' = [0, 1, 1, 1]$ .  $\triangleleft$

As we can see  $M'_0 \neq M_0$  because  $\mathbf{HW}(W'_{2 \rightarrow 0}) > t$ , thus  $M_0 = 1$  whereas the original bit was 0. In this specific case, the number of errors in the error vector was higher than the error correcting capability  $t$ . In order to prevent this behavior, one can use a better coding technique, a different code with a higher error correcting capability (increasing the overhead on the channel), or one can use a concatenation of error-correcting codes, which is being described in Section 3.5.3.

## 2.4.2 BCH Codes

BCH codes are a class of cyclic error-correcting codes that are constructed using finite fields. The algebraic foundation of BCH codes makes them ideal for error correction.

For any positive integer  $m \geq 3$  and  $t < 2^m - 1$ , there exists a binary BCH code with the following parameters [45, 47, p. 99]:

- The block-length of a code is the amount of bits that the code acts on. When encoding a message larger than the block-length, the code is applied to a multiple of the block-length. The block-length of the code is given by:

$$n = 2^m - 1 \quad (2.4.2)$$

- The number of parity-check bits is the number of bits that are used to detect and correct errors in the code. The number of parity-check bits is given by:

$$n - k \leq m \cdot t \quad (2.4.3)$$

- The minimum distance is the minimum of  $\mathbf{HD}(U, V)$  over all distinct code-words  $U$  and  $V$ . If the following condition holds, the decoder will always decode correctly when there are  $t$  or fewer errors.

$$d_{\min} \geq 2t + 1 \quad (2.4.4)$$

We define a binary BCH code as follows:

**Definition 2.15** (Binary BCH Code). *A binary BCH code  $\mathcal{C}_{BCH}(n, k, t)$  is called a binary BCH code of order  $m$ , length  $n = 2^m - 1$ , distance  $d$ , error correcting capability  $t = \lfloor \frac{d-1}{2} \rfloor$  and primitive element  $\alpha \in \mathbf{GF}(2^m)$ :*

$$\mathcal{C}_{BCH}(n, k, t) = \{(W_0, \dots, W_{n-1}) \in \mathbf{GF}(2^m) \mid \mathbf{w}(x) = W_{n-1}x^{n-1} + \dots + W_1x + W_0 \\ \text{satisfies } \forall 1 \leq i \leq 2t : \mathbf{w}(\alpha^i) = \mathbf{w}(\alpha^{2i}) = \dots = \mathbf{w}(\alpha^{(n-1)i}) = 0\}$$

### 2.4.2.1 Encoding

In order to encode a message  $M$  of length  $k$  we first need to construct the generator polynomial.

Let  $\Phi_i(x)$  be the minimal polynomial of  $\alpha^i$ , the primitive element. Then the generator polynomial  $\mathbf{g}(x)$  must be the least common multiple of  $\Phi_1(x)$ ,  $\Phi_2(x)$ ,  $\dots$ ,  $\Phi_{d-1}(x)$ , i.e.,

$$\mathbf{g}(x) = \mathbf{LCM}(\Phi_1(x), \Phi_2(x), \dots, \Phi_{d-1}(x)) \quad (2.4.5)$$

The degree of the generator polynomial  $\mathbf{g}(x)$  is at most  $m \cdot t$ , hence, the number of parity-check bits  $(n - k)$  is at most  $m \cdot t$  (Formula 2.4.3).

**Example 2.4.4.** Let  $\alpha$  be a primitive element of  $\mathbf{GF}(2^4)$  generated by the primitive polynomial  $\mathbf{p}(x) = x^4 + x + 1$  [14]. The finite field table is given in Appendix B.1. The minimal polynomials  $\Phi_i(x)$  ( $1 \leq i \leq n$ ) of  $\alpha$  are<sup>2</sup>:

$$\begin{aligned} \Phi_1(x) &= (x + \alpha)(x + \alpha^2)(x + \alpha^4)(x + \alpha^8) \\ &= x^4 + x + 1 \\ \Phi_3(x) &= (x + \alpha^3)(x + \alpha^6)(x + \alpha^{12})(x + \alpha^9) \\ &= x^4 + x^3 + x^2 + x + 1 \\ \Phi_5(x) &= (x + \alpha^5)(x + \alpha^{10}) \\ &= x^2 + x + 1 \\ \Phi_7(x) &= (x + \alpha^7)(x + \alpha^{14})(x + \alpha^{13})(x + \alpha^{11}) \\ &= x^4 + x^3 + 1 \end{aligned}$$

<sup>2</sup>Note that conjugates are omitted. A conjugate is a minimal polynomial  $\Phi_j(x)$  that is equal to  $\Phi_i(x)$  ( $i < j$ ). For example, in Example 2.4.4,  $\Phi_1(x) = \Phi_2(x) = \Phi_4(x) = \Phi_8(x)$ .

Then, using Formula 2.4.5, the double-error-correcting ( $t = 2$ ,  $d = 5$ ) BCH code of length  $n = 2^4 - 1 = 15$  (Formula 2.4.2) is generated by:

$$\begin{aligned} \mathbf{g}(x) &= \mathbf{LCM}(\Phi_1(x), \Phi_3(x)) \\ &= (x^4 + x + 1)(x^4 + x^3 + x^2 + x + 1) \\ &= x^8 + x^7 + x^6 + x^4 + 1 \end{aligned}$$

Hence,  $n - k = 8$  such that this is a  $\mathcal{C}_{\text{BCH}}(n, k, t) = \mathcal{C}_{\text{ BCH}}(15, 7, 2)$  BCH code.  $\triangleleft$

The remainder polynomial  $\mathbf{r}(x)$  that contains the parity-check bits is obtained by:

$$\mathbf{r}(x) = x^{n-k} \cdot \mathbf{m}(x) \pmod{\mathbf{g}(x)} \quad (2.4.6)$$

**Example 2.4.5.** Take the message  $M = [1, 1, 0, 0, 1, 1, 0]$  with message polynomial  $\mathbf{m}(x) = x^6 + x^5 + x^2 + x$  and generator polynomial  $\mathbf{g}(x) = x^8 + x^7 + x^6 + x^4 + 1$  as calculated in Example 2.4.4, the remainder polynomial  $\mathbf{r}(x)$  is obtained by using Formula 2.4.6:

$$\begin{aligned} \mathbf{r}(x) &= x^8(x^6 + x^5 + x^2 + x) \pmod{x^8 + x^7 + x^6 + x^4 + 1} \\ &= x^{14} + x^{13} + x^{10} + x^9 \pmod{x^8 + x^7 + x^6 + x^4 + 1} \\ &= x^3 + 1 \end{aligned}$$

$\triangleleft$

Finally, the code polynomial  $\mathbf{w}(x)$  is obtained by:

$$\mathbf{w}(x) = x^{n-k}\mathbf{m}(x) + \mathbf{r}(x) \quad (2.4.7)$$

**Example 2.4.6.** Take the message polynomial  $\mathbf{m}(x) = x^6 + x^5 + x^2 + x$  and the remainder polynomial  $\mathbf{r}(x) = x^3 + 1$  as calculated in Example 2.4.5, the code polynomial  $\mathbf{w}(x)$  is obtained by using Formula 2.4.7:

$$\begin{aligned} \mathbf{w}(x) &= x^8(x^6 + x^5 + x^2 + x) + x^3 + 1 \\ &= x^{14} + x^{13} + x^{10} + x^9 + x^3 + 1 \end{aligned}$$

As a result, the codeword for the message  $M = [1, 1, 0, 0, 1, 1, 0]$  is given by  $W = [1, 1, 0, 0, 1, 1, 0, 0, 0, 0, 1, 0, 0, 1]$ .  $\triangleleft$

### 2.4.2.2 Decoding

As per Definition 2.15, the decoding is based on the following algebraic characteristic:

$$\forall 1 \leq i \leq 2t : \mathbf{w}(\alpha^i) = W_{n-1}\alpha^{(n-1)i} + \dots + W_2\alpha^{2i} + W_1\alpha^i + W_0 = 0 \quad (2.4.8)$$

The decoding of a received codeword  $W' = W \oplus E$  with codeword polynomial  $\mathbf{w}'(x) = W'_{n-1}x^{n-1} + \dots + W'_1x + W'_0$  and error polynomial  $\mathbf{e}(x) = E_{n-1}x^{n-1} + \dots + E_1x + E_0$  is performed in four steps:

1. Compute the syndromes  $\mathcal{S}_i$  ( $1 \leq i \leq 2t$ ).
2. Determine the error-locator polynomial  $\sigma(x)$ .
3. Find the error-locator polynomial coefficients  $\sigma_1, \sigma_0, \dots, \sigma_\tau$  ( $\tau \leq t$ ).
4. Carry out the error correction using the error correction polynomial  $\mathbf{e}'(x)$ .

Here,  $\tau$  is the actual number of errors in the code. We describe these four steps in the following sections.

**2.4.2.2.1 Syndrome Computation** We can compute the syndromes  $\mathcal{S}_i$  ( $1 \leq i \leq 2t$ ) using:

$$\begin{aligned} \mathcal{S}_i &= \mathbf{w}'(\alpha^i) \\ &= W'_{n-1}\alpha^{(n-1)i} + \dots + W'_2\alpha^{2i} + W'_1\alpha^i + W'_0 \end{aligned} \quad (2.4.9)$$

**Example 2.4.7.** Take the message  $M = [1, 1, 0, 0, 1, 1, 0]$  and its codeword  $W = [1, 1, 0, 0, 1, 1, 0, 0, 0, 0, 1, 0, 0, 1]$  as calculated in Section 2.4.2.1. By applying the error vector  $E = [0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 1, 0, 0]$  on this message, we obtain the received codeword  $W' = [1, 1, 0, 0, 0, 1, 0, 0, 0, 0, 0, 1, 1, 0, 1]$ . Hence, the codeword polynomial is given by:  $\mathbf{w}'(x) = x^{14} + x^{13} + x^9 + x^3 + x^2 + 1$ .

The four syndromes are computed using Formula 2.4.9 and Table B.1 from Appendix B:

$$\begin{aligned} \mathcal{S}_1 &= \alpha^{14} + \alpha^{13} + \alpha^9 + \alpha^3 + \alpha^2 + 1 \\ &= \alpha + 1 = \alpha^4 \\ \mathcal{S}_2 &= \alpha^{28} + \alpha^{26} + \alpha^{18} + \alpha^6 + \alpha^4 + 1 \\ &= \alpha^2 + 1 = \alpha^8 \\ \mathcal{S}_3 &= \alpha^{42} + \alpha^{39} + \alpha^{27} + \alpha^9 + \alpha^6 + 1 \\ &= \alpha^3 + \alpha^2 + 1 = \alpha^{13} \\ \mathcal{S}_4 &= \alpha^{56} + \alpha^{52} + \alpha^{36} + \alpha^{12} + \alpha^8 + 1 \\ &= \alpha \end{aligned}$$

◁

**2.4.2.2.2 Error Locator Polynomial Coefficients** The error locator polynomial can be expressed as follows:

$$\begin{aligned} \sigma(x) &= (1 - \beta_\tau x) \dots (1 - \beta_2 x)(1 - \beta_1 x) \\ &= \sigma_\tau x^\tau + \dots + \sigma_1 x + \sigma_0, \end{aligned} \quad (2.4.10)$$

where  $\tau \leq t$  is the number of errors in the code.

In the case  $\tau \leq t$ , the number of roots (of which the calculation is given in Section 2.4.2.2.3) is equal to the degree of the error locator polynomial. If we find a higher degree of the error locator polynomial  $\sigma(x)$ , we can conclude that there were more errors in the code than its error correcting capability  $t$  (i.e.  $\tau > t$ ). In this case, no errors can be located. In order to prevent this behavior, one can use a better coding technique, a different code with a higher error correcting capability (increasing the overhead on the channel), or one can use a concatenation of error-correcting codes, which is being described in Section 3.5.3.

The coefficients of  $\sigma(x)$  are:

$$\begin{aligned}
 \sigma_0 &= 1 \\
 \sigma_1 &= \beta_\tau + \cdots + \beta_2 + \beta_1 \\
 \sigma_2 &= \beta_{\tau-1}\beta_\tau + \cdots + \beta_1\beta_3 + \beta_1\beta_2 \\
 \sigma_3 &= \beta_{\tau-2}\beta_{\tau-1}\beta_\tau + \cdots + \beta_1\beta_2\beta_4 + \beta_1\beta_2\beta_3 \\
 &\vdots \\
 \sigma_\tau &= \beta_1\beta_2 \dots \beta_\tau
 \end{aligned} \tag{2.4.11}$$

In order to solve the coefficients of the error locator polynomial, one has to solve the Newton's identities [47, p. 130]:

$$\begin{aligned}
 \mathcal{S}_1 + \sigma_1 &= 0 \\
 \mathcal{S}_2 + \sigma_1\mathcal{S}_1 &= 0 \\
 \mathcal{S}_3 + \sigma_1\mathcal{S}_2 + \sigma_2\mathcal{S}_1 + \sigma_3 &= 0 \\
 &\vdots \\
 \mathcal{S}_\tau + \sigma_1\mathcal{S}_{\tau-1} + \cdots + \sigma_{\tau-1}\mathcal{S}_2 + \sigma_\tau\mathcal{S}_1 &= 0
 \end{aligned} \tag{2.4.12}$$

The objective is to find the minimum degree polynomial  $\sigma(x)$  whose coefficients satisfy these Newton identities.

Various algorithms have been proposed to find these coefficients: the Peterson-Gorenstein-Zierler algorithm [24], the Berlekamp-Massey algorithm [6] and Euclid's algorithm [54]. For the purpose of this thesis and because of the complexity of these algorithms, we stop the description for finding the error-locator polynomial coefficients here. For a detailed description, we encourage the reader to consult Moreira and Farrell [47] or any of the papers these algorithms were introduced in [47, 24, 6, 54].

**Example 2.4.8.** Take the received codeword  $W' = [1, 1, 0, 0, 0, 1, 0, 0, 0, 0, 0, 1, 1, 0, 1]$  and its syndromes  $\mathcal{S}_1 = \alpha^4$ ,  $\mathcal{S}_2 = \alpha^8$ ,  $\mathcal{S}_3 = \alpha^{13}$  and  $\mathcal{S}_4 = \alpha$  from Example 2.4.7. Using the Berlekamp-Massey algorithm we obtain the error locator polynomial  $\sigma(x) = \alpha^{12}x^2 + \alpha^4x + 1$  with  $\sigma_0 = 1$ ,  $\sigma_1 = \alpha + 1 = \alpha^4$  and  $\sigma_2 = \alpha^3 + \alpha^2 + \alpha + 1 = \alpha^{12}$ .  $\triangleleft$



**2.4.2.2.3 Finding Roots of Error Locator Polynomial** The roots of the error locator polynomial  $\sigma(x)$  are  $\beta_\tau^{-1}, \dots, \beta_2^{-1}, \beta_1^{-1}$ , the inverse of the error location numbers.

One way of solving the roots for  $\sigma(x)$  is by brute-forcing the finite field elements in the error locator polynomial and check whether the following condition holds:

$$\sigma(\alpha^i) = 0 \quad (2.4.13)$$

This is called the Chien search, as introduced by Chien [15].

- If this condition holds, then there was an error at the inverse position of  $i$ , i.e. in position  $n - i$ .
- If this condition does not hold, there was no error.

**Example 2.4.9.** Take the error locator polynomial  $\sigma(x) = \alpha^{12}x^2 + \alpha^4x + 1$  with  $\sigma_0 = 1$ ,  $\sigma_1 = \alpha^4$  and  $\sigma_2 = \alpha^{12}$  as computed in Example 2.4.8. Evaluating  $\sigma(x)$  for  $x = \alpha$ ,  $x = \alpha^2$ ,  $\dots$ ,  $x = \alpha^n$  (where  $n = 2^m - 1$ , Formula 2.4.2) gives the following set of equations:

$$\begin{aligned} \sigma(\alpha) &= \alpha^{12}(\alpha)^2 + \alpha^4(\alpha) + 1 \\ &= (\alpha^3 + 1) + (\alpha^2 + \alpha) + 1 \\ &= \alpha^3 + \alpha^2 + \alpha + 2 \\ &= \alpha^3 + \alpha^2 + \alpha \\ &\neq 0 \\ \sigma(\alpha^2) &= \alpha^{12}(\alpha^2)^2 + \alpha^4(\alpha^2) + 1 \\ &= \alpha^3 + \alpha^2 + \alpha + 1 \\ &\neq 0 \\ &\vdots \\ \sigma(\alpha^{15}) &= \alpha^{12}(\alpha^{15})^2 + \alpha^4(\alpha^{15}) + 1 \\ &= \alpha^3 + \alpha^2 + 1 \\ &\neq 0 \end{aligned}$$

Solving these equations we find  $\sigma(\alpha^5) = 0$  and  $\sigma(\alpha^{13}) = 0$ . Hence, the roots of the error locator polynomial  $\sigma(x) = \alpha^{12}x^2 + \alpha^4x + 1$  are  $\beta_2^{-1} = 5$  and  $\beta_1^{-1} = 13$  for which Formula 2.4.13 holds.  $\triangleleft$

**2.4.2.2.4 Error Correction** Once the roots  $\beta_\tau^{-1}, \dots, \beta_2^{-1}, \beta_1^{-1}$  of the error locator polynomial  $\sigma(x) = \sigma_\tau x^\tau + \dots + \sigma_1 x + \sigma_0$  are found, we can obtain the error correction polynomial:

$$\mathbf{e}'(x) = x^{n-\beta_\tau^{-1}} + \dots + x^{n-\beta_2^{-1}} + x^{n-\beta_1^{-1}} \quad (2.4.14)$$

Finally, we can obtain the recovered codeword polynomial  $\mathbf{w}''(x)$ :

$$\mathbf{w}''(x) = \mathbf{w}'(x) + \mathbf{e}'(x) \quad (2.4.15)$$

**Example 2.4.10.** Take the received codeword  $W' = [1, 1, 0, 0, 0, 1, 0, 0, 0, 0, 0, 1, 1, 0, 1]$  ( $\mathbf{w}'(x) = x^{14} + x^{13} + x^9 + x^3 + x^2 + 1$ ) and the roots  $\beta_2^{-1} = 5$  and  $\beta_1^{-1} = 13$  of the error locator polynomial  $\sigma(x) = \alpha^{12}x^2 + \alpha^4x + 1$  from the previous exercises. The error correction polynomial is given by using Formula 2.4.14:

$$\begin{aligned} \mathbf{e}'(x) &= x^{15-5} + x^{15-13} \\ &= x^{10} + x^2 \end{aligned}$$

This gives us the error correction vector  $E' = [0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 1, 0, 0]$ . We can see that  $E' = E$  (Exercise 2.4.7). Finally, we can obtain the original codeword polynomial using Formula 2.4.15:

$$\begin{aligned} \mathbf{w}''(x) &= (x^{14} + x^{13} + x^9 + x^3 + x^2 + 1) + (x^{10} + x^2) \\ &= x^{14} + x^{13} + x^{10} + x^9 + x^3 + 1 \end{aligned}$$

This gives us the recovered codeword  $W'' = [1, 1, 0, 0, 1, 1, 0, 0, 0, 0, 0, 1, 0, 0, 1]$ . We can see that  $W'' = W$  (Exercise 2.4.7). Hence, we recovered the original message  $M = [1, 1, 0, 0, 1, 1, 0]$ .  $\triangleleft$

## 2.5 Fuzzy Extractors

Fuzzy Extractors (FEs) were first introduced to turn biometric information into keys usable for cryptographic applications [19]. This biometric data, for example iris scans or fingerprints can be used as a key, where the key must be derived from measurements that are slightly different. With the use of a FE, this data is turned into a key with nearly uniform randomness and helper data to recover this key using another measurement of the biometrics. Even though FEs were first introduced for biometric information, a FE can be used to produce cryptographic keys from any key that is not precisely reproducible and not distributed uniformly given that these keys are ‘close enough’ to each other. For the purpose of this thesis, FEs are used to correct noisy PUF responses into unpredictable keys.

Using a generation procedure, the FE can convert the biometric input into a key that is unpredictable. Moreover, using a generation procedure the FE can produce public information about the biometric input such that this input can exactly be recovered using error-correction codes. These two steps are performed in a Strong Extractor (SE) and a  $\text{Gen}$ , respectively. A reproduction procedure can recover the original biometric input from the public information produced by the generation procedure of the FE. Using the same Strong Extractor (SE) as was used in the generation procedure, this biometric input is converted into the same key.

### 2.5.1 Strong Extractor

The Strong Extractor (SE) converts the noisy data that is not distributed uniformly into a key that is unpredictable. We define a SE as follows [19, p. 528]:

**Definition 2.16** (Strong Extractor). *An efficient  $(n, m', k, \epsilon)$ -strong extractor is a polynomial time probabilistic function  $\mathbf{Ext}(W, X) : \{0, 1\}^n \rightarrow \{0, 1\}^k$  such that for all min-entropy  $m'$  distributions  $W$  we have:*

$$\mathbf{SD}(\langle \mathbf{Ext}(W, X), X \rangle, \langle U_l, X \rangle) \leq \epsilon, \text{ where}$$

$U_l$  denotes the uniform distribution on an  $l$ -bit binary string and  $\mathbf{Ext}(W, X)$  stands for applying  $\mathbf{Ext}$  to  $W$  using uniformly distributed randomness  $X$ .

In other words, a SE can extract a uniformly distributed key from non uniformly distributed input  $W$  and uniformly distributed randomness  $X$ .

Practically, to obtain a high security level, strong assumptions about the min-entropy of the randomness source have to be made. This is often impossible [43, p. 306] and multiple practical solutions have been proposed. Moreover, because we need to use uniformly distributed randomness  $X$  which has to be shared between generation and reproductions, large entropy losses need to be taken into account. This makes the overall key generation as defined in Definition 2.16 impractical.

Some solutions are to use a cryptographic hash function [34] or a Pseudo-Random Function (PRF). For example, one can append a random variable to the noisy data and hash this into a key (salting). However still, one has to make strong assumptions about the min-entropy of the noisy data.

We call these constructions Average-case Extractors (AcEs), which we define as follows [20, p. 10]:

**Definition 2.17** (Average-case Extractor). *Let  $\mathbf{Ext}(W, X) : \{0, 1\}^n \rightarrow \{0, 1\}^l$  be a polynomial time probabilistic function which uses  $r$  bits of randomness. We say that  $\mathbf{Ext}(W, X)$  is an efficient average-case  $(n, m, l, \epsilon)$ -strong extractor if for all pairs of random variables  $(W, I)$  such that  $W$  is an  $n$ -bit string satisfying  $\tilde{\mathbf{H}}_\infty = (W | I) \geq m$ , we have*

$$\mathbf{SD}(\langle \mathbf{Ext}(W, X), X, I \rangle, \langle U_l, X, I \rangle) \leq \epsilon,$$

where  $X$  is uniform on  $\{0, 1\}^r$ .

In other words, if there is enough entropy in  $W$  (taking into account the entropy loss introduced by  $I$ ) and there is enough entropy in  $X$ ,  $\mathbf{Ext}(W, X)$  is indistinguishable from random  $(U_l)$ .

## 2.5.2 Secure Sketch

The Secure Sketch (SS) converts the noisy data that is not distributed uniformly into helper data that can be used to recover that same noisy data. Almost always, SSe use encoding of (a composition of) error-correcting codes as described in Section 2.4.

Let  $\mathcal{W}$  be the set of all possible noisy and non uniformly distributed vectors with distance function  $\mathbf{dist}(W, W')$  ( $W, W' \in \mathcal{W}$ ) as described in Section 2.2.1. We define a SS as follows [19, p. 529]:

**Definition 2.18** (). *An  $(\mathcal{W}, m, m', t)$ -secure sketch is a randomized map  $\mathbf{SS}(X) : \mathcal{W} \rightarrow \{0, 1\}^*$  with the following properties:*

1. *There exists a deterministic recovery function  $\mathbf{Rec}(W', H)$  allowing to recover vector  $W$  from its sketch  $H = \mathbf{SS}(W)$  and any vector  $W'$  close to  $W$ : for all  $W, W' \in \mathcal{M}$  satisfying  $\mathbf{dist}(W, W') \leq t$ , we have  $\mathbf{Rec}(W', \mathbf{SS}(W)) = W$ .*
2. *For all random variables  $W \in \mathcal{W}$  with min-entropy  $m$ , the average min-entropy of  $W$  given  $\mathbf{SS}(W)$  is at least  $m'$ . That is  $\tilde{\mathbf{H}}_\infty = (W | \mathbf{SS}(W)) \geq m'$ .*

In other words, we are able to recover a vector  $W$  using another vector  $W'$  close to  $W$  and the helper data  $H$  generated from the secure sketch  $H = \mathbf{SS}(W)$ . Moreover, the entropy loss during the construction of  $H = \mathbf{SS}(W)$  is  $m - m'$ .

When using an error-correcting code  $\mathcal{C}(n, k, t)$  for the SS, knowledge of the helper data  $H$  does not fully disclose the entropy of  $W$ , only  $n - k$  bits of this helper data. Thus, we can use, store and communicate  $H$  publicly where it still has  $\mathbf{H}(W) - (n - k)$  bits of entropy left in  $H$  [43, p. 305]. The bit error probability  $p_e$  and entropy  $\rho$  of the PUF determine the (composition of) error-correcting codes used in the design of the SS. This should be optimized such that no information is leaked about the key.

## 2.5.3 Fuzzy Extractor

Now that we have described a SE and a SS, we can start defining a FE. As mentioned before the FE composes a generation procedure and a reproduction procedure.

We define a FE as follows [19, p. 530]:

**Definition 2.19** (Fuzzy Extractor). *A  $(\mathcal{W}, m, l, t, \epsilon)$ -fuzzy extractor is given by two procedures (**Gen**, **Rep**).*

1. **Gen**( $W$ ) *is a probabilistic generation procedure, which on input  $W \in \mathcal{W}$  outputs an “extracted” string  $R \in \{0, 1\}^l$  and a public string  $H$ . We require that for any distribution  $W$  on  $\mathcal{W}$  of min-entropy  $m$ , if  $\langle R, H \rangle \leftarrow \mathbf{Gen}(W)$ , then we have  $\mathbf{SD}(\langle R, H \rangle, \langle U_l, H \rangle) \leq \epsilon$ .*

2.  $\mathbf{Rep}(W', H)$  is a deterministic reproduction procedure allowing to recover  $R$  from the corresponding public string  $H$  and any vector  $W'$  close to  $W$ : for all  $W, W' \in \mathcal{W}$  satisfying  $\mathbf{dist}(W, W') \leq t$ , if  $\langle R, H \rangle \leftarrow \mathbf{Gen}(W)$ , then we have  $\mathbf{Rep}(W', H) = R$ .

In other words, a random binary variable  $R$  can be constructed using noisy and non-random input  $W$  using a generation procedure. Moreover, using a reproduction procedure, this randomness  $R$  can be recovered, given a second noisy and non-random input  $W'$  and the helper data  $H$  as constructed by the generation procedure.

We can use Definition 2.17 (Average-case Extractor), Definition 2.18 () and Definition 2.19 (Fuzzy Extractor) to prove that we can construct a FE from SS [20, p. 13]:

**Lemma 2.1** (Fuzzy Extractor from ). *Assume  $\mathbf{SS}(X)$  is a  $(\mathcal{W}, m, m', t)$ -secure sketch with recovery procedure  $\mathbf{Rec}(W', H)$ , and let  $\mathbf{Ext}(W, X)$  be an average case  $(n, m', k, \epsilon)$ -strong extractor. Then the following  $(\mathbf{Gen}, \mathbf{Rep})$  is a  $(\mathcal{W}, m, l, t, \epsilon)$ -fuzzy extractor:*

1.  $\mathbf{Gen}(W)$ : set  $H = \langle \mathbf{SS}(W), X \rangle$ ,  $R = \mathbf{Ext}(W, X)$ , output  $\langle R, H \rangle$
2.  $\mathbf{Rep}(W', \langle H, X \rangle)$ : recover  $W = \mathbf{Rec}(W', H)$  and output  $R = \mathbf{Ext}(W, X)$ .

*Proof.* From Definition 2.18 ()

$$H_\infty(W | \mathbf{SS}(W)) \geq m'$$

And since  $\mathbf{Ext}(W, X)$  is an average-case  $(n, m', k, \epsilon)$ -strong extractor (Definition 2.17), from Definition 2.19 (Fuzzy Extractors) we get:

$$\mathbf{SD}(\langle \mathbf{Ext}(W, X), \mathbf{SS}(W), X \rangle, \langle U_l, \mathbf{SS}(W), X \rangle) = \mathbf{SD}(\langle R, H \rangle, \langle U_l, H \rangle) \leq \epsilon$$

□

**Corollary 2.1** (Fuzzy Extractor from ). *If  $\mathbf{Rec}$  is an  $(\mathcal{W}, m, m', t)$ -secure sketch and  $\mathbf{Ext}$  is an  $(n, m' - \log_2(\frac{1}{\delta}), l, \epsilon)$ -strong extractor, then the above construction from Lemma 2.1  $(\mathbf{Gen}, \mathbf{Rep})$  is a  $(\mathcal{W}, m, l, t, \epsilon + \delta)$ -fuzzy extractor.*

## 2.6 Authenticated Encryption

Before AE, protocol designers used a generic composition paradigm for which they concatenate a privacy-only encryption scheme with a Message Authentication Code (MAC) [5, 33]. However, this naive approach demands multiple procedures which substantially reduces efficiency of the protocols. AE improves efficiency by providing confidentiality, integrity and authenticity into a single, compact mode [56]. However, there was still a need to efficiently authenticate a message header belonging to the plaintext or cipher-text. Authenticated Encryption with Associated Data (AEAD)<sup>3</sup> provides for this by additional authentication of data other than the plaintext. We define an AEAD-scheme as follows [56, p. 4]:

**Definition 2.20** (AEAD-scheme). *An authenticated-encryption scheme with associated data (AEAD-scheme) is a three-tuple*

$$\Pi = (\mathcal{K}, \mathcal{E}, \mathcal{D}).$$

*Associated to  $\Pi$  are sets of strings  $\mathcal{N} \subseteq \{0, 1\}^*$  indicating the nonce,  $\mathcal{M} \subseteq \{0, 1\}^*$  indicating the message and  $\mathcal{A}^{\mathcal{D}} \subseteq \{0, 1\}^*$  indicating the associated data, for example a header.*

- *The key space  $\mathcal{K}$  is a finite nonempty set of strings.*
- *The encryption algorithm  $\mathcal{E}$  is a deterministic algorithm that takes strings  $K \in \mathcal{K}$ ,  $N \in \mathcal{N}$ ,  $M \in \mathcal{M}$  and  $A \in \mathcal{A}^{\mathcal{D}}$  and returns string  $\langle C, T \rangle = \mathcal{E}_K^{N,A}(M) = \mathcal{E}_K(N, A, M)$ .*
- *The decryption algorithm  $\mathcal{D}$  is a deterministic algorithm that takes strings  $K \in \mathcal{K}$ ,  $N \in \mathcal{N}$ ,  $A \in \mathcal{A}^{\mathcal{D}}$ ,  $C \in \{0, 1\}^*$  and  $T \in \{0, 1\}^*$  and returns  $\mathcal{D}_K^{N,A}(\langle C, T \rangle)$ , which is either a string in  $\mathcal{M}$  or the distinguished symbol INVALID.*

*We require that  $\mathcal{D}_K^{N,A}(\mathcal{E}_K^{N,A}(M)) = M$  for all  $K \in \mathcal{K}$ ,  $N \in \mathcal{N}$ ,  $M \in \mathcal{M}$  and  $A \in \mathcal{A}^{\mathcal{D}}$ .*

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<sup>3</sup>In this thesis, we refer to AEAD by referring to AE.

## PROTOCOL DESIGN

In this chapter we describe the proposed privacy-preserving authentication protocol, the Concealing KETJE Protocol (CKP). In this protocol a trusted server and a set of deployed devices will authenticate each other where devices require anonymous authentication such that they are untraceable. As a starting point we take the PUF-based privacy-preserving authentication protocol as proposed by Aysu et al. [3]. However, we want to correct a few design-flaws in the protocol and improve its overall performance. First, the protocol proposed by Aysu et al. makes use of a Fuzzy Extractor (FE) that can be broken using linear equation analysis as pointed out by Becker [3, p. 12]. Moreover, the FE makes use of a pre-shared key (PSK), which increases the overhead of the protocol. We design a new FE that has enough entropy in its output and that does not use a PSK. Second, the protocol uses two cryptographic primitives, namely Symmetric Key Encryption (SKE) and Pseudo-Random Function (PRF), of which for the SKE the SIMON block-cipher is used, an encryption scheme introduced by the untrustworthy National Security Agency (NSA) [18, p. 113] (Snowden revelations [25]). We replace these primitives with a single, compact cryptographic primitive, namely Authenticated Encryption with Associated Data (AEAD).

In Section 3.1 we present the security considerations that play a role in the design of the proposed protocol, which will be presented and elaborated in Section 3.3. In Section 3.2 we present the considerations that we need to take due to the available hardware. Section 3.4 describes the 3-1 Double Arbiter PUF (DAPUF) as is used in our protocol. The extraction of the device credentials together with the construction of the helper data is described in the Reverse FE (RFE), Section 3.5. Finally, our choice for the lightweight AEAD-scheme, KETJE, will be described in Section 3.6.

## 3.1 Security Considerations

In this section we present the security considerations that play a role in the design of the proposed protocol. We identify the operational and cryptographic properties that a device to be authenticated should adhere to, we present the trust- and attacker model and we present the considerations we take providing the available hardware.

### 3.1.1 Operational and Cryptographic Properties

For the security considerations of the operational and cryptographic properties we follow Lee et al. [38]. These properties describe what considerations need to be made when designing a privacy-preserving authentication protocol in general and an untraceable device in particular.

#### 3.1.1.1 Scalability

Many protocols face the pitfall that they are not scalable because of the computational workload on the server that increases linearly with the number of devices. Considering that these authentication protocols often work for a large amount of devices, a thoughtful design is necessary. Our protocol is also subject to this risk, which means that we elaborate on the design rationale to minimize this risk. More about this in Section 6.3.

#### 3.1.1.2 Anti-cloning

It should not be possible to clone a device. One property that a device needs to have is that it should have a key that is unique in the sense that it all the bits of the credential should be unpredictable. This way, if an attacker succeeds to crack one of the devices, he/she cannot use this secret to clone any of the other devices. We base our countermeasure mainly on the use of a Physically Unclonable Function (PUF). At every authentication the device credentials are freshly generated to an unpredictable value.

#### 3.1.1.3 Security Against the Replay Attack

This property implies that an attacker should not be able to authenticate a device using a replayed message (i.e. he/she should not be able to successfully carry out Man-in-the-Middle (MitM) attacks). This implies that all communication over the channel should have enough entropy. We base our countermeasure against this attack mainly on the use of a FE. The FE provides for a fresh key at every authentication-try which has enough entropy considering the transmitted messages. Moreover, the AEAD-scheme provides for confidentiality, integrity and authenticity of the messages in the communication channel.



#### 3.1.1.4 Security Against the Tracking Attack

It should not be possible for an attacker to trace a device over multiple authentications. Moreover, it should not be possible to identify a device by probing the device with challenges. This property ensures that our protocol is privacy-preserving with respect to outsiders, which means that a device (and its owner) remain anonymous. We base our countermeasure against this attack on a True Random Number Generator (TRNG), by using the unpredictable PUF responses both as input (seed) and as output of the TRNG.

#### 3.1.1.5 Backward/Forward Un-traceability

This property, that is stronger than the un-traceability property, implies that it should not be possible to track a device in past or future communications, provided that an attacker has cracked a device. If an attacker manages to recover a key from a device, he should not be able to identify a particular device in the past or in the future. This property ensures that a device (and its owner) remain anonymous always. We base our countermeasure on the authenticate-before-identify strategy we adopted. Devices do not carry, store or communicate device specific identification numbers (IDs), which is not needed because of the use of a PUF that ensures authenticity of the device. Moreover, all communication appears random to an attacker.

### 3.1.2 Trust Model

In order to roll out devices, we present a trust model. Our trust model is mainly based on Aysu et al. [3], the starting point of our proposed protocol. We identified the following trust bases:

- Devices are enrolled in a secure environment using a one-time interface.
- A trusted server and a number of devices will authenticate each other while devices need to remain anonymous.
- Our channel is ideal, i.e. no errors will occur due in the Binary Symmetric Channel (BSC) as described in Section 2.4.
- After enrollment, the server remains trusted but devices are subjected to an attacker.
- The attacker may not know the identity of a device such that the device cannot be tracked.

### 3.1.3 Attacker Model

In order to prove the security of the proposed protocol, an attacker model needs to be constructed. Our attacker model is mainly based on Aysu et al. [3], the starting point of our proposed protocol.

We identified that the attacker may have two goals:

1. The attacker may want to impersonate a device which will result in a violation of the security.
2. The attacker may want to trace devices in between authentications which will result in a violation of the privacy.

These two main goals will be the subjects of the proofs as described in Chapter 4.

We identified the following permissions and constraints for the attacker:

- An attacker can modify all communication between the server and devices.
- An attacker can know the result of the authentication.
- An attacker can access the Non-Volatile Memory (NVM) of the devices.
- An attacker cannot modify data stored in the NVM of the devices.
- An attacker cannot perform implementation attacks on the device and the server.
- An attacker cannot reverse engineer the PUF such that he can predict PUF responses.
- An attacker does not have access to intermediate values on the device (i.e. the registers on the device).
- An attacker cannot physically trace every device in between authentications.
- An attacker cannot use other (non-cryptographic) mechanisms to identify a device (e.g. the one proposed by Lee et al. [37]).

## 3.2 Available Hardware

In order to give performance results of the proposed protocol, we implement the device on a Zedboard by Avnet Inc. [2]. The basic specifications of the Zedboard are given in Appendix A. The main operating chip on the Zedboard is the Zynq®-7000 All Programmable System on Chip (SoC) by Xilinx Inc. [64]. This SoC is composed of a Processing System (PS) with two Advanced RISC Machine (ARM) cores and 28 nm Programmable Logic (PL) that is equivalent to the Xilinx 7-series Field Programmable Gate Arrays (FPGAs).

The Zedboard does not have Static RAM (SRAM) that can be power-cycled, which means that we are restricted in the use of SRAM PUFs. We propose to use an existing and recently proposed PUF by Machida et al. [39], which has promising results for the design rationale of our proposed protocol.

### 3.3 Protocol

The proposed authentication protocol is illustrated in Figure 3.2, its setup phase is illustrated in Figure 3.1. The protocol is based on a PUF that produces noisy, but recoverable, responses on equal challenges due to the unique physical characteristics of the Integrated Circuit (IC) [42]. Because of this behavior, the PUF is identifiable from other PUFs. A FE can extract a key from this noisy data produced by the PUF using helper data generated from a previous key-extraction [19]. However, the recovery procedure is of a higher complexity than the generation of the helper data that is used for this reconstruction. A reverse FE reverses this behavior by placing the helper data generation in the device and the more complex reconstruction in the server [29]. In order to preserve privacy, the device credential is updated at each successful authentication, which results in fresh PUF responses, and thus fresh keys.

The setup procedure is used to synchronize the PUF response of the the device with the server. The responses in the server database will be used to exhaustively search for a matching device. The setup procedure is illustrated in Figure 3.1 and works as follows. In a trusted environment, the server produces a random challenge  $X^1$ . The device uses this challenge to produce a PUF response  $Y^1$  which is being sent to the server. The challenge is being stored in the device non-volatile memory. The server stores the response in a database on index  $n$ , indicating the number of the device. Notice that the response is stored at  $Y$  and  $Y^{old}$  in order to prevent desynchronization.

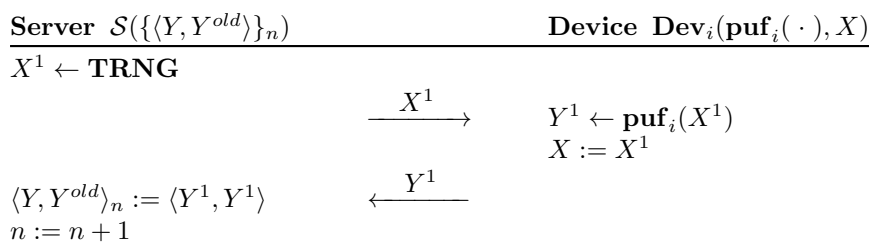


Figure 3.1: Setup phase.

The authentication phase as illustrated in Figure 3.2 works as follows. First, the server generates an unpredictable challenge  $A$  and sends this to the device. The device uses the challenge  $X$  stored in its non-volatile memory to produce a PUF response  $Y^1$ . From this PUF response, helper data  $H$  and an unpredictable key  $R$  is generated using the FE's generation procedure **FE.Gen**. Consecutively, a new challenge  $X^2$  is randomly generated by the device such that it can be updated on a successful authentication. This challenge is fed to the device's PUF in order to receive a new PUF response  $Y^2$ . Following, a nonce  $N$  is randomly generated such that the PUF response can be encrypted using the AEAD-scheme. The resulting cipher-text  $C^1$ , its tag  $T^1$  and the nonce  $N$  will be sent to the server. The server performs an exhaustive search over the database, recovering a key for each index. These keys are used to try to decrypt the cipher-text  $C^1$  using the tag  $T^1$ , challenge

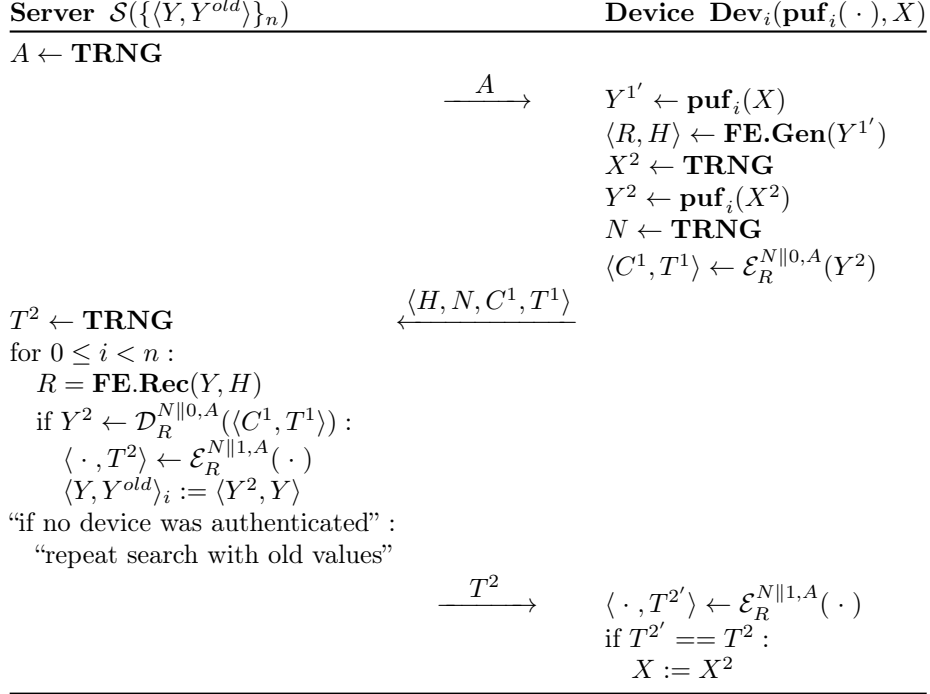


Figure 3.2: Authentication phase.  $|A|, |H|, |N|, |C^1|, |T^1|, |T^2| \geq k$  and PUF responses  $Y$  should contain enough entropy w.r.t.  $H$  s.t.  $|R| \geq k$ .

$A$  and nonce  $N$ . If there is a successful authentication, the server produces another tag  $T^2$  using  $\mathcal{E}$ , but with nonce  $N^2 \parallel 1$  instead of  $N^2 \parallel 0$  in order to create another instance of  $\mathcal{E}$ . This tag is sent to the device. Moreover, the server updates the old PUF-response  $Y$  with the new PUF response  $Y^2$ . If there were no successful authentications, the server repeats the procedure over the previous PUF responses in the database. If after this there were still no successful authentications, the server responds with a random value for  $T^2$ . Finally, the device checks the tag  $T^2$  with its own produced tag in order to reveal whether the authentication succeeded. If the authentication succeeded, the device updates the old challenge  $X$  with the new challenge  $X^2$ .

The remainder of this chapter is dedicated to present a generic approach to create any instance of CKP. This generic approach requires the quality of PUF responses  $\langle p_e, \rho \rangle$ , the desired maximum for the failure rate of the authentications  $p_{\text{fail}}$  and the desired security level  $k$  in order to design the instance. We use the presented examples to construct an instance that forms the basis of our proof of concept in Chapter 5.

### 3.4 3-1 Double Arbiter PUF

The type of PUF used in the protocol motivates most of the other design parameters for the rest of the protocol. For example, depending on the bit-error-probability  $p_e$  of a PUF response-bit, the inter- and intra-distances of the PUF responses, the entropy of the PUF responses  $\rho$  and the desired maximum for the failure rate of the authentications  $p_{\text{fail}}$ , both the number of PUF responses as well as the type and size of error-correcting codes is motivated.

We implement the DAPUF as proposed by Machida et al. [39] because its characteristics are promising for the parameters of our protocol. We use 1275 PUF responses on 64-bit challenges, of which 40 bits are used for the challenge, 12 bits are used to obtain the 1275 unique PUF responses and 12 bits are used to produce random numbers, including a seed for the TRNG that is updated at the beginning of every authentication. More about this design rationale in Section 3.5.1.

This section first presents the design of the DAPUF before elaborating on the main characteristics of the PUF as were described in Section 2.3.

#### 3.4.1 DAPUF Design

In Section 2.3.5.2 we have discussed the arbiter PUF which was illustrated in Figure 2.1. Recent studies have shown that Machine Learning (ML) attacks can predict future PUF responses [58, 57], violating the unpredictability characteristic of a PUF as is described in Definition 2.13. Hence, Machida et al. proposed to alter the design of arbiter PUFs in order to prevent ML attacks having effect.

In Figure 2.1 from Section 2.3.5.2, we call the collection of switch blocks a selector chain. Figure 3.3 illustrates the DAPUF as proposed by Machida et al.. The DAPUF acts on 64-bit challenges, which means that a selector chain contains 64 switch blocks. The DAPUF is composed of three of these selector chains all acting on the same challenge  $X$ . Using an ‘enable’ signal  $E$  ( $E_L$  and  $E_R$ ), the competition is started between the left signals  $E_L$  and the right signals  $E_R$ . For each of the combination of left- or right signals an arbiter is used to measure which signal arrived first at the arbiter. After measuring these race conditions, the results are exclusive-OR (XOR)’ed to collect the 1-bit PUF response  $Y$ . By challenging the DAPUF with 1275 different challenges, we obtain a 1275-bit PUF response.

We call the PUF class of the proposed DAPUF  $\mathcal{P}_{3-1}$ .

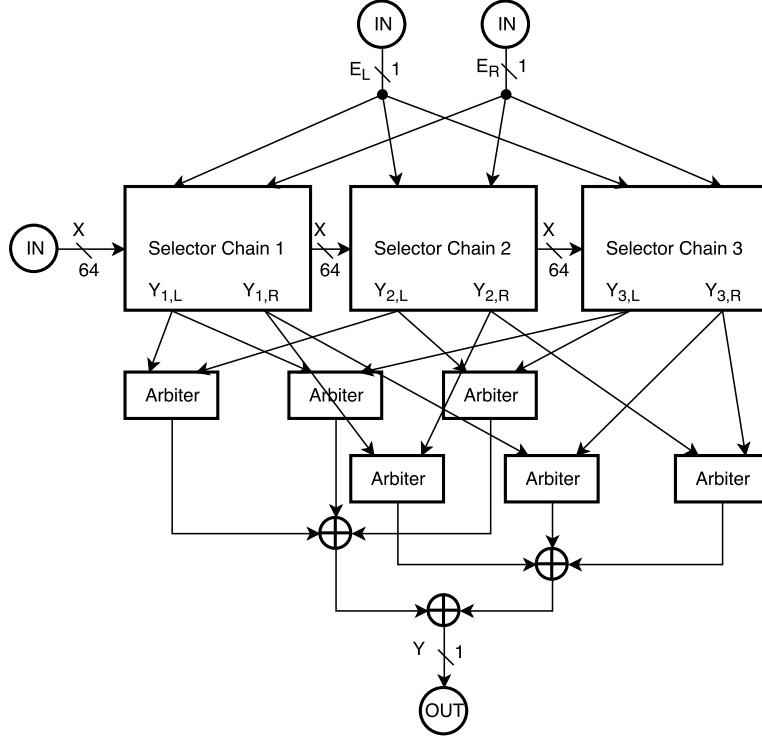


Figure 3.3: DAPUF as proposed by Machida et al. [39].  $\oplus$  denotes a bitwise XOR,  $\textcircled{\text{IN}}$  denotes the input of the DAPUF and  $\textcircled{\text{OUT}}$  denotes the output of the DAPUF.

### 3.4.2 Intra-distance and Reproducibility

As described in Section 2.3.1, the intra-distance provides reproducibility of any unique DAPUF instance  $\mathbf{puf}_{0 \leq i < n} \in \mathcal{P}_{3-1}$  (where  $n$  is the total number of DAPUFs in the DAPUF class  $\mathcal{P}_{3-1}$ ), which means that if two measurements are performed on the same DAPUF, then these responses are with high probability very close to each other.

The reproducibility results (its inverse is called ‘steadiness’) are given in Table 3.1 [40]. In the table, steadiness is calculated by challenging the DAPUF instance  $\mathbf{puf}$  a number of  $m$  times with a set of  $n$  equal challenges  $X$ . Of the  $m$   $n$ -bit responses, the Hamming distances  $\mathbf{HD}(Y, Y')$  between two arbitrary PUF responses  $Y, Y' \leftarrow \mathcal{Y}$  is calculated (thus a total of  $\binom{m}{2}$  combinations) and averaged. These distances are equivalent to the intra-distance as is described in Definition 2.7. Finally, the calculated average is divided by the bit-length  $n$  of the responses. This way, we immediately find the bit-error-probability  $p_e$  of DAPUF class  $\mathcal{P}_{3-1}$ . This is the average probability that a response bit is different between challenges. Ideally, the average steadiness is 0%. From the table we see that the average steadiness is approximately 12%, which means that the bit-error-probability  $p_e$  is 0.12. These results have been achieved by taking  $m = 128$  and  $n = 128$ . The reproducibility is  $100\% - \text{steadiness} = 88\%$ .

Table 3.1: Results of the overall evaluation of the 3-1 Double Arbiter PUF [40].

Metric	FPGA	Results
Prediction rate [%] (with 1,000 training data)	A	56.47
	B	57.45
	C	56.75
Steadiness [%]	A	14.11
	B	10.93
	C	10.35
Uniqueness [%]	A with B	50.60
	B with C	51.34
	C with A	48.78
Randomness [%]	A	55.68
	B	52.54
	C	53.59

### 3.4.3 Inter-distance and Uniqueness

As described in Section 2.3.2, the inter-distance provides uniqueness of any DAPUF instance  $\mathbf{puf}_{0 \leq i < n}$  in the DAPUF collection  $\mathcal{P}_{3-1}$  (where  $n$  is the total number of DAPUFs in the DAPUF class  $\mathcal{P}_{3-1}$ ), which implies that responses of measurements performed on different DAPUFs are with high probability far apart.

The uniqueness results are given in Table 3.1 [40]. In the table, uniqueness is calculated by challenging two DAPUF instances  $\mathbf{puf}_i$  and  $\mathbf{puf}_j$  ( $i \neq j$ ) on two distinct FPGAs a number of  $n$  times using randomly chosen challenges  $X$ . Of these two  $n$ -bit responses  $Y, Y' \leftarrow \mathcal{Y}$ , the the Hamming distances  $\mathbf{HD}(Y, Y')$  is calculated. This distance is equivalent to the inter-distance as is described in Definition 2.9. Finally, the distance metric is divided by the bit-length  $n$  of the two responses. Ideally, the average uniqueness between DAPUF instances is 50%. From the table we see that the average uniqueness is approximately 50%, which is close to ideal. These results have been achieved by taking  $n = 5,000$  measurements.

### 3.4.4 Unclonability and Unpredictability

As described in Section 2.3.4, unclonability assures that physically and technically, a DAPUF instance  $\mathbf{puf}_{i'} \in \mathcal{P}_{3-1}$  is difficult (or even impossible) to create from an other DAPUF instance  $\mathbf{puf}_i \in \mathcal{P}_{3-1}$ .

Because of the characteristics explained in Section 2.3.5.2, arbiter PUFs and thus also DAPUFs are hard to clone. There are several un-plausible techniques an attacker might try [36].

- An attacker can try to clone the PUF by remembering all Challenge-Response Pairs (CRPs). However, this is implausible because this requires applying an exponential amount of challenges.

- An attacker can try to reproduce the PUF such that the behavior is equal to the original PUF. However, this is implausible because of the random variations that are intrinsically introduced in the manufacturing process.
- An attacker can probe the PUF physically such that delays can be measured and a timing model can be constructed to predict future PUF responses. However, probing with sufficient precision is likely to be very difficult, and will likely cause the delays to be influenced by the probe.
- An attacker could build a non-invasive model, a so called “virtual counterfeit”. However, until now, no such model has been proposed.

As described in Section 2.3.4, unpredictability ensures that unobserved responses remain sufficiently random, even after observing responses to other challenges on the same DAPUF instance. This characteristic applies both to the prediction rate of the DAPUF class  $\mathcal{P}_{3-1}$ , as well as the randomness of the DAPUF class  $\mathcal{P}_{3-1}$ .

First, from Table 3.1 we see that the prediction rate is approximately 57%, which approximates a random guess (i.e. 50%). This is a considerable improvement for arbiter PUF constructions because the prediction rate of conventional arbiter PUFs is 86% [40, p. 8].

Second, from the table we see that the randomness is approximately 54%. This randomness is calculated by challenging a DAPUF instance **puf** a number of  $n$  times with randomly chosen challenges  $X$ . Then, the Hamming weight  $\mathbf{HW}(Y)$  of the result is calculated, giving the number of ones in the PUF response  $Y$ . Finally, this number is divided by the number of challenges  $n$ , giving the probability that a PUF response-bit is  $Y_i = 1$ . The randomness of 54% ( $\Pr(Y_i = 1) = 0.54$ ) has been achieved by taking  $n = 2^{16}$  measurements. From this result, we can calculate the entropy of the PUF responses  $\rho$  using the binary entropy function  $\mathbf{h}(p)$  from Formula 2.2.1, Section 2.2.2:

$$\begin{aligned}\rho &= -\Pr(Y_i = 1) \log_2(\Pr(Y_i = 1)) - \Pr(Y_i = 0) \log_2(\Pr(Y_i = 0)) \\ &= -0.54 \log_2(0.54) - 0.46 \log_2(0.46) \\ &= 0.9954\end{aligned}\tag{3.4.1}$$

The entropy of the PUF responses  $\rho = 0.9954$  is an extremely good result considering true randomness is  $\rho = 1$ . From this entropy and the bit-error-probability  $p_e = 0.12$  as calculated in Section 3.4.2, we conclude that the quality of the PUF responses is  $\langle p_e = 0.12, \rho = 0.9954 \rangle$ - $\mathcal{P}_{3-1}$ . These findings will be used to motivate the design of the RFE.

### 3.5 Reverse Fuzzy Extractor

As mentioned in Section 3.3, we use a reverse FE construction with the computationally lighter generation procedure in the device and the computationally heavier reproduction procedure on the server. In order to be able to recover the PUF responses, we use a concatenation of error-correcting codes as introduced by Bösch et al. [13], which is a technique to increase the correction rate while minimizing



the computational overhead. Our proposed RFE uses a concatenation code of a repetition code  $\mathcal{C}_{\text{REP}}(n, 1, t) = C_{\text{REP}}(5, 1, 2)$  and a Bose-Chaudhuri-Hocquenghem (BCH) code  $\mathcal{C}_{\text{BCH}}(n, k, t) = C_{\text{BCH}}(255, 139, 15)$ . The 1275-bit PUF response is cut into words of 5 bits, which are encoded using the repetition code. The first bit of each word (total of 255 bits) is used to extract a key of 128 bits by using the AEAD-scheme with an empty message. The other four bits of each word (total of 1020 bits) are used to produce helper data that can recover the value of the first bit of each word. In order to further decrease the failure rate of the authentications, for these 255 recovered bits a BCH code with error correcting capability of 15 bits is used.

### 3.5.1 RFE Design Rationale

In this section, we describe the design rationale of the parameters of the concatenation code. Our goal is to construct a 128-bit key from the DAPUF responses with quality  $\langle p_e = 0.12, \rho = 0.9954 \rangle$ . In this rationale, we assume that all bits of the PUF response are independent.

#### 3.5.1.1 Fail rate

We aim for a fail rate of  $p_{\text{fail}} = 10^{-6}$ , which is considered an acceptable fail rate for standard performance levels [42].

The probability that a received codeword of  $n$  bits has more than  $t$  errors is given by [26, 13]:

$$\begin{aligned} \Pr(\text{">}t \text{ errors"}) &= \sum_{i=t+1}^n \binom{n}{i} p_e^i (1-p_e)^{n-i} \\ &= 1 - \sum_{i=0}^t \binom{n}{i} p_e^i (1-p_e)^{n-i}, \end{aligned} \tag{3.5.1}$$

where  $p_e$  is the bit-error-probability.

When using a  $C_{\text{REP}}(5, 1, 2)$  repetition code, we can decrease the bit-error-probability  $p_e = 0.12$  to:

$$\begin{aligned} p_{e,\text{REP}} &= 1 - \sum_{i=0}^2 \binom{5}{i} 0.12^i (1-0.12)^{5-i} \\ &= 0.01432 \end{aligned}$$

Using a  $C_{\text{BCH}}(255, 139, 15)$  BCH code on top of that further decreases the bit-error-probability  $p_{e,\text{REP}} = 0.01432$  to a fail rate  $p_{\text{fail}}$  of:

$$\begin{aligned} p_{\text{fail}} &= 1 - \sum_{i=0}^{15} \binom{255}{i} 0.01432^i (1-0.01432)^{255-i} \\ &= 1.176 \cdot 10^{-6} \end{aligned}$$

As a result, using a concatenation code of a  $C_{\text{REP}}(5, 1, 2)$  repetition code and a  $C_{\text{BCH}}(255, 139, 15)$  BCH code achieves a fail rate that is acceptable for standard performance levels [42].

### 3.5.1.2 Entropy

When implementing a concatenation code, careful considerations of the input entropy is necessary, otherwise the output might yield zero leftover entropy [35]. When using a  $C_{\text{REP}}(5, 1, 2)$  repetition code on 5-bit words of the 1275-bit PUF response, 4-bits per word are disclosed as helper data. Hence, we have an entropy loss of:

$$\mathbf{H}_{\text{REP loss}} = 4 \cdot 255 = 1020 \text{ bits}$$

The entropy loss of the  $C_{\text{BCH}}(255, 139, 15)$  BCH code is introduced by the random string that is needed to construct the code. Hence, we have an entropy loss of:

$$\mathbf{H}_{\text{BCH loss}} = n - k = 255 - 139 = 116 \text{ bits}$$

As a result, the total entropy loss of the 1275-bit PUF response by disclosing the helper data is:

$$\mathbf{H}_{\text{loss}} = \mathbf{H}_{\text{REP loss}} + \mathbf{H}_{\text{BCH loss}} = 1020 + 116 = 1136 \text{ bits}$$

This leaves  $(1275 - 1136) \cdot \rho = 139 \cdot 0.9958 = 138$  bits of entropy left in the 255 bits of the BCH codeword. These 255 bits will be compressed in a 128-bit key using the AEAD-scheme.

### 3.5.2 Extraction

As mentioned in the previous section, the 255 bits ( $R_{\text{REP}}$ ) will be compressed into a 128-bit key. This method is similar to the construction of Maes et al. [43] and Kelsey et al. [34]. An advantage is that the AEAD-scheme can be used for this construction, minimizing the number of primitives that need to be implemented on the device. Moreover, not using additional randomness decreases the amount of data that needs to be communicated between server and device. However, the amount of entropy in the input needs to be carefully considered.

For this construction we introduce the novel definition of a new type of Extractor, the Entropy Accumulator (EA):

**Definition 3.1** (Entropy Accumulator). *Let  $\mathbf{Acc}(W) : \{0, 1\}^n \rightarrow \{0, 1\}^l$  ( $n < l$ ) be a polynomial time probabilistic function. We say that  $\mathbf{Acc}(W)$  is an efficient  $(n, m, l, \epsilon)$ -entropy accumulator if for all pairs of random variables  $(W, I)$  such that  $W$  is an  $n$ -bit string satisfying  $\mathbf{H}_{\infty}(W | I) \geq m$ , we have*

$$\mathbf{SD}(\langle \mathbf{Acc}(W), I \rangle, \langle U_l, I \rangle) \leq \epsilon.$$

We prove that we can construct a FE from  $s$  using Definition 3.1 (Entropy Accumulator), Definition 2.18 (Secure Sketch) and Definition 2.19 (Fuzzy Extractor):

**Lemma 3.1** (Fuzzy Extractor from II). *Assume  $\mathbf{SS}(X)$  is a  $(\mathcal{W}, m, m', t)$ -secure sketch with recovery procedure  $\mathbf{Rec}(W', H)$ , and let  $\mathbf{Acc}(W)$  be an  $(n, m', k, \epsilon)$ -entropy accumulator. Then the following  $(\mathbf{Gen}, \mathbf{Rep})$  is a  $(\mathcal{W}, m, l, t, \epsilon)$ -fuzzy extractor:*

1.  $\mathbf{Gen}(W)$ : set  $H = \mathbf{SS}(W)$ ,  $R = \mathbf{Acc}(W)$ , output  $\langle R, H \rangle$
2.  $\mathbf{Rep}(W', H)$ : recover  $W = \mathbf{Rec}(W', H)$  and output  $R = \mathbf{Acc}(W)$ .

*Proof.* From Definition 2.18 (Secure Sketch)

$$H_\infty(W | \mathbf{SS}(W)) \geq m'$$

And since  $\mathbf{Acc}(W)$  is a  $(n, m', k, \epsilon)$ -entropy accumulator (Definition 3.1), from Definition 2.19 (Fuzzy Extractors) we get:

$$\mathbf{SD}(\langle \mathbf{Acc}(W), \mathbf{SS}(W) \rangle, \langle U_l, \mathbf{SS}(W) \rangle) = \mathbf{SD}(\langle R, H \rangle, \langle U_l, H \rangle) \leq \epsilon$$

□

**Corollary 3.1** (Fuzzy Extractor from II). *If  $\mathbf{Rec}$  is an  $(\mathcal{W}, m, m', t)$ -secure sketch and  $\mathbf{Acc}$  is a  $(n, m' - \log_2(\frac{1}{\delta}), l, \epsilon)$ -entropy accumulator, then the above construction from Lemma 3.1  $(\mathbf{Gen}, \mathbf{Rep})$  is a  $(\mathcal{W}, m, l, t, \epsilon + \delta)$ -fuzzy extractor.*

### 3.5.3 Secure Sketch

We use a concatenation code of a  $C_{\text{REP}}(5, 1, 2)$  repetition code and a  $C_{\text{BCH}}(255, 139, 15)$  BCH code for the Secure Sketch (SS) [13]. This section will describe both code constructions in more detail.

#### 3.5.3.1 Repetition Code

As mentioned in Section 2.4.1.1, there are more advanced techniques of using repetition codes. Simply repeating bits of the PUF response will disclose information in the helper data about this response.

**3.5.3.1.1 Encoding** Figure 3.4 illustrates the repetition code encoding construction. In this figure,  $Y$  denotes the 5-bit word of the original PUF response and  $H_{\text{REP}}$  denotes the 4-bit helper data that is used by the decoder to retrieve the first bit of  $Y$ ,  $R_{\text{REP}}$ .

**Example 3.5.1.** See Figure 3.4. As an example we take  $Y = [1, 0, 1, 1, 0]$ . The repetition code encoding construction gives the helper data  $H_{\text{REP}} = [1, 0, 0, 1]$  and secret value  $R_{\text{REP}} = [1]$ . ◁

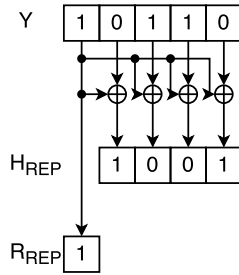


Figure 3.4: Repetition code encoding construction.  $\oplus$  denotes an XOR.

Note that, as we have assumed in the calculation of the leftover entropy (Section 3.5.1.2), the 4-bit helper data  $H_{\text{REP}}$  does not disclose any information about the first bit of the 5-bit PUF response word  $Y$ .

The first bit of the 5-bit word  $Y$ ,  $R_{\text{REP}}$ , will be encoded using the BCH code.

**3.5.3.1.2 Decoding** Figure 3.5 illustrates the repetition code decoding construction. In this figure,  $Y'$  denotes the 5-bit word of the stored PUF response,  $H_{\text{REP}}$  denotes the 4-bit received helper data and  $S$  denotes the resulting syndrome vector. If the Hamming weight **HW** of the syndrome vector  $S$  is larger than  $t$ , chances are that the first bit of  $Y'$  was faulty. Note that this construction will wrongly correct a bit that was assumed faulty if the number of errors  $e > t$ . Hence, we need the BCH code construction on top of the repetition code construction.

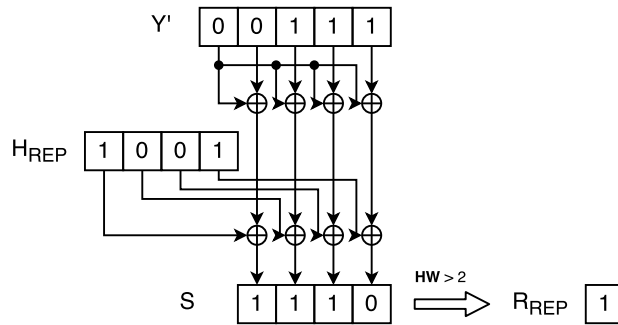


Figure 3.5: Repetition code decoding construction.  $\oplus$  denotes a bitwise XOR.

**Example 3.5.2.** See Figure 3.5. As an example we take  $Y = [1, 0, 1, 1, 0]$  from Example 3.5.1 and  $Y' = [0, 0, 1, 1, 1]$ . The repetition code decoding construction gives the syndrome vector  $S = [1, 1, 1, 0]$ . The Hamming weight **HW** of the syndrome vector  $S$  is  $\text{HW} = 3 > t$ , thus, highly likely the secret value  $R_{\text{REP}}$  equals  $R_{\text{REP}} = [1]$ .  $\triangleleft$

### 3.5.3.2 BCH Code

In order to further decrease the fail rate  $p_{\text{fail}}$ , a BCH code with error correcting capability  $t = 15$  is applied over the binary string that contains the first bit of the 5-bit PUF response words. Then using Formulas 2.4.2 to 2.4.4 we take a BCH code  $\mathcal{C}_{\text{BCH}}(n, k, t)$  with order  $m = 8$ , block-length  $n = 2^m - 1 = 255$ , error correcting capability  $t = 15$ , message length  $k = 139$ ,  $n - k = 116$  parity-check bits and design distance  $d = 2t + 1 = 31$ .

**3.5.3.2.1 Encoding** As mentioned in Section 2.4.2.1, for BCH encoding we have to construct the generator polynomial  $\mathbf{g}(x)$ . This generator polynomial forms the basis of the Linear Feedback Shift Register (LFSR) design in the hardware of the device, more about this in Section 5.2.2.

Let  $\alpha$  be a primitive element of  $\mathbf{GF}(2^8)$  generated by the primitive polynomial  $\mathbf{p}(x) = x^4 + x^3 + x^2 + 1$ . The finite field table is partially given in Appendix B.2. Then, using Formula 2.4.5, we find the generator polynomial  $\mathbf{g}(x)$ :

$$\begin{aligned} \mathbf{g}(x) = & x^{116} + x^{114} + x^{111} + x^{108} + x^{107} + x^{106} + x^{105} + x^{103} + x^{102} + x^{101} \\ & + x^{99} + x^{98} + x^{97} + x^{95} + x^{93} + x^{90} + x^{89} + x^{88} + x^{87} + x^{84} + x^{82} \\ & + x^{77} + x^{76} + x^{74} + x^{73} + x^{72} + x^{70} + x^{67} + x^{65} + x^{64} + x^{63} + x^{59} \\ & + x^{58} + x^{57} + x^{56} + x^{54} + x^{53} + x^{49} + x^{48} + x^{47} + x^{45} + x^{44} + x^{42} \\ & + x^{41} + x^{40} + x^{39} + x^{38} + x^{31} + x^{30} + x^{25} + x^{23} + x^{22} + x^{20} + x^{19} \\ & + x^{18} + x^{17} + x^9 + x^8 + x^4 + x^3 + 1 \end{aligned}$$

Figure 3.6 illustrates the BCH code encoding construction that we use. Note that we use a random message polynomial  $\mathbf{m}(x)$  of degree 139 to construct the remainder polynomial  $\mathbf{r}(x)$  (and thus the code polynomial  $\mathbf{w}(x)$ ) using the previously calculated generator polynomial  $\mathbf{g}(x)$ . This codeword  $W$  (the code polynomial  $\mathbf{w}(x)$ ) is then XOR'ed with the binary string that contains the first bit of the all the 5-bit PUF response words  $R_{\text{REP}}$ . The resulting string is the helper data  $H_{\text{BCH}}$ . Using this construction, we can encode a 255-bit string instead of a 139-bit string as described in Section 2.4.2.

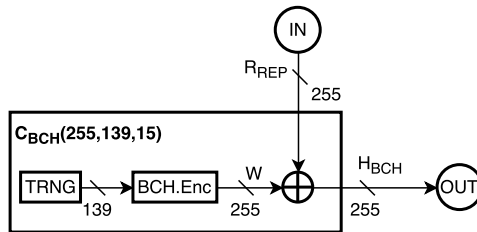


Figure 3.6: BCH code encoding construction.  $\oplus$  denotes a bitwise XOR,  $\textcircled{\text{IN}}$  denotes the input string and  $\textcircled{\text{OUT}}$  denotes the output string.

**3.5.3.2.2 Decoding** Decoding is executed on the server. Figure 3.7 illustrates the BCH code decoding construction that we use. First the helper data  $H_{\text{BCH}}$  that is received from the device is XOR'ed with the string that contains the recovered first bit of the all the 5-bit PUF response words  $R'_{\text{REP}}$ , this results in the received codeword  $W'$ . Note that this string might still contain faulty bits. Then, this received codeword  $W'$  is decoded into the recovered codeword  $W''$ , which is XORed with  $H_{\text{BCH}}$  to produce the recovered PUF response bits  $R''_{\text{REP}}$ .

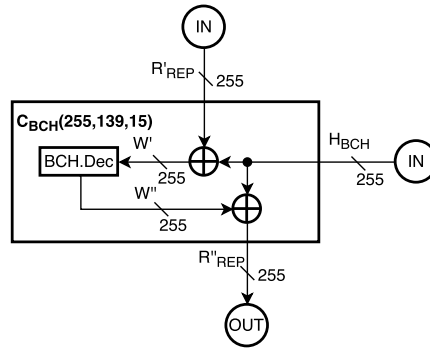


Figure 3.7: BCH code decoding construction.  $\oplus$  denotes a bitwise XOR,  $\textcircled{\text{IN}}$  denotes the input strings and  $\textcircled{\text{OUT}}$  denotes the output string.

## 3.6 KETJE

In our implementation of the protocol we use the AEAD-scheme KETJE, one of the 56 candidates in the Competition for Authenticated Encryption: Security, Applicability and Robustness (CAESAR) [7] which was announced in 2013 at the Early Symmetric Crypto workshop in Mondorf-les-Bains, Luxembourg. Similarly to the Advanced Encryption Standard (AES) [16], the European Network of Excellence in Cryptology (ECRYPT) Stream Cipher Project (eSTREAM, [4]), SHA-3 (Keccak [8]) and the Password Hashing Competition (PHC) (Argon2 [12]), CAESAR seeks to select a portfolio of algorithms that enhances AEAD applicability.

We use the AEAD-scheme KETJE for the EA in the RFE, the encryption and decryption of the second PUF response  $Y^2$  and the computation of the authenticator  $T^2$ .

KETJE is an AEAD-scheme that is aimed at constrained devices such as Radio-Frequency Identification (RFID) tags and nodes in the Internet of Things (IoT) [11]. The scheme is composed of KETJE JR and KETJE SR, of which KETJE JR is an even more lightweight variant with a security level of 96 bits. However, for the security level of our protocol (128 bits), we use KETJE SR. As a result, we describe all metrics of KETJE SR. Also, when we mention KETJE we refer to the specific instance of KETJE SR.

As with all AEAD schemes, KETJE relies on nonce uniqueness in order for the

crypto-system to be semantically secure<sup>1</sup>. For KETJE this is very important, as it can be broken when messages are encrypted with the same nonce. For the permutations, KETJE uses KECCAK-**p**, a permutation that relies on a round reduced version KECCAK-**f** [8]. The construction that calls these permutations is called MONKEYDUPLEX which is based on the duplex construction that is described by Bertoni et al. [9]. The mode that calls the MONKEYDUPLEX construction is called MONKEYWRAP, which is similar and functionally equivalent to SPONGEWRAP, also described by Bertoni et al. [9].

### 3.6.1 KECCAK-**p**

The KECCAK cryptographic primitive is a subset of the SHA-3 cryptographic hash function that has been standardized by the National Institute of Standards and Technology (NIST) [49]. Hence, KECCAK-**p**( $b, n_r$ ) relies on a round reduced version of KECCAK-**f**( $b$ ) which is defined by its width  $b = 25 \cdot 2^l$ , with  $b \in \{25, 50, 100, 200, 400, 800, 1600\}$ , and its number of rounds  $n_r$  [8]. More specifically, KECCAK-**p**( $b, n_r$ ) consists of the last  $n_r$  rounds of KECCAK-**f**( $b$ ), when  $n_r = 12 + 2 \cdot l$ , KECCAK-**p**( $b, n_r$ ) = KECCAK-**f**( $b$ ).

During the permutations of KECCAK-**p**( $b, n_r$ ), there are five operations that act on a state  $\mathcal{T}(x, y, z)$  that is illustrated in Figure 3.8. The size of this state is  $\mathcal{T}(5, 5, w)$ , with  $w = 2^l$ . For  $0 \leq a, b < 5$  and  $0 \leq c < w$ , we call  $\mathcal{T}(x, b, z)$  a plane,  $\mathcal{T}(x, y, c)$  a slice,  $\mathcal{T}(a, y, z)$  a sheet,  $\mathcal{T}(x, b, c)$  a row,  $\mathcal{T}(a, y, c)$  a column,  $\mathcal{T}(a, b, z)$  a lane and  $\mathcal{T}(a, b, c)$  a bit. For KETJE, KECCAK-**p**( $b, n_r$ ) with  $b = 400$  and  $l = 4$  is used.  $n_r$  varies per operation in the MONKEYDUPLEX construction, more about this in Section 3.6.2.

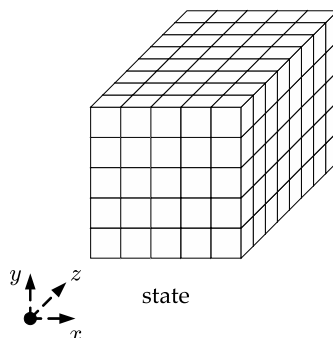


Figure 3.8: State  $\mathcal{T}(x, y, z)$  of KECCAK-**p**.

The permutations of one round  $\mathbf{R}(\mathcal{T})$  on the state  $\mathcal{T}(x, y, z)$  are described by five operations:

$$\mathbf{R}(\mathcal{T}) = \iota(\mathcal{T}) \circ \chi(\mathcal{T}) \circ \pi(\mathcal{T}) \circ \rho(\mathcal{T}) \circ \theta(\mathcal{T}) \quad (3.6.1)$$

The operations in the  $x$  and  $y$  coordinates are in modulo 5, whereas operations in the  $z$  coordinate is in modulo  $w$ .

<sup>1</sup>Here a system “[...]” is semantically secure if whatever an eavesdropper can compute about the cleartext given the cipher-text, he can also compute without the cipher-text.” [23].

### 3.6.1.1 $\theta$ -operation

Figure 3.9 illustrates the  $\theta$ -operation. The  $\theta$ -operation is linear and aimed at diffusion of the state.  $\theta$  is given by the following formula:

$$\theta(\mathcal{T}(x, y, z)) = \mathcal{T}(x, y, z) + \sum_{y'=0}^4 \mathcal{T}(x-1, y', z) + \sum_{y'=0}^4 \mathcal{T}(x+1, y', z-1) \quad (3.6.2)$$

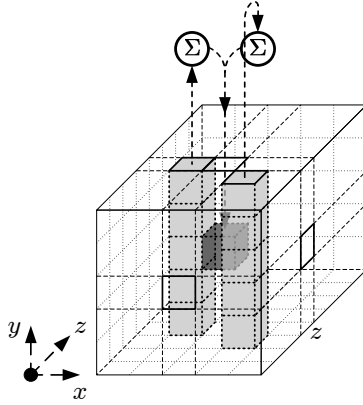


Figure 3.9:  $\theta$ -operation.

### 3.6.1.2 $\rho$ -operation

Figure 3.10 illustrates the  $\rho$ -operation. The  $\rho$ -operation consists of translations within the lanes aimed at providing inter-slice dispersion.  $\rho$  is given by the following formula:

$$\rho(\mathcal{T}(x, y, z)) = \mathcal{T}\left(x, y, z - \frac{(t+1)(t+2)}{2}\right), \quad (3.6.3)$$

with  $t$  satisfying  $0 \leq t < 24$  and  $\begin{bmatrix} 0 & 1 \\ 2 & 3 \end{bmatrix}^t \begin{bmatrix} 1 \\ 0 \end{bmatrix} = \begin{bmatrix} x \\ y \end{bmatrix}$  in  $\mathbf{GF}(5)^{2 \times 2}$ , or  $t = -1$  if  $x = y = 0$ .

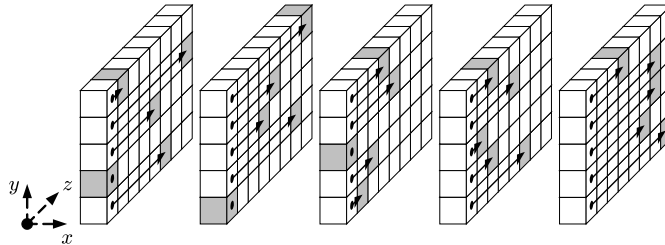


Figure 3.10:  $\rho$ -operation.



### 3.6.1.3 $\pi$ -operation

Figure 3.11 illustrates the  $\pi$ -operation. The  $\pi$ -operation is based on a transposition of the lanes that provides dispersion aimed at long-term diffusion.  $\pi$  is given by the following formula:

$$\forall z : \pi(\mathcal{T}(x, y, z)) = \mathcal{T}(x', y', z), \quad (3.6.4)$$

$$\text{with } \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ 2 & 3 \end{bmatrix} \begin{bmatrix} x' \\ y' \end{bmatrix}.$$

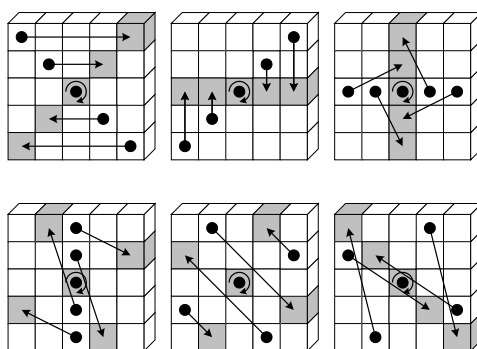


Figure 3.11:  $\pi$ -operation.

### 3.6.1.4 $\chi$ -operation

Figure 3.12 illustrates the  $\chi$ -operation. The  $\chi$ -operation is the only nonlinear mapping of KECCAK-p.  $\chi$  is given by the following formula:

$$\forall y, z : \chi(\mathcal{T}(x, y, z)) = \mathcal{T}(x, y, z) + (\mathcal{T}(x, y, z) + 1) \cdot \mathcal{T}(x + 2, y, z) \quad (3.6.5)$$

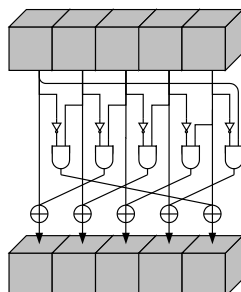


Figure 3.12:  $\chi$ -operation.

### 3.6.1.5 $\iota$ -operation

The  $\iota$ -operation consists of applying round-constants in order to disrupt symmetry.  $\iota$  is given by the following formula:

$$\iota(\mathcal{T}(x, y, z)) = \mathcal{T}(x, y, z) + \mathbf{RC}_i \quad (3.6.6)$$

Here,  $\mathbf{RC}_i$  is given by the following formula, indicating the round-constant for round  $i$ :

$$\mathbf{RC}_i(0, 0, 2^j - 1) = \mathbf{rc}(j + 7i), \forall 0 \leq j \leq l,$$

and all other values of  $\mathbf{RC}_i(x, y, z)$  are zero. The values  $\mathbf{rc}(t) \in \mathbf{GF}(2)$  are given by the LFSR:

$$\mathbf{rc}(t) = (x^t \bmod x^8 + x^6 + x^5 + x^4 + 1) \bmod x$$

## 3.6.2 MONKEYDUPLEX

In this section, we give a brief description of the MONKEYDUPLEX construction. For a full description we encourage the reader to consult Bertoni et al. [11, 10].

The MONKEYDUPLEX construction was introduced by Bertoni et al. [10] and then improved by the same authors [11]. The construction is aimed at building stream ciphers and authenticated encryption schemes. MONKEYWRAP, which describes the AEAD-mode of KETJE builds on top of MONKEYDUPLEX, more about this in Section 3.6.3.

Figure 3.13 illustrates the MONKEYDUPLEX construction. In this figure, we see that the MONKEYDUPLEX construction is composed of three operations: **start**, **step** and **stride**. These three operations use a permutation function  $\mathbf{f}$  (e.g. KECCAK- $\mathbf{p}(b, n_r)$ ) with different number of rounds  $n_r$ .

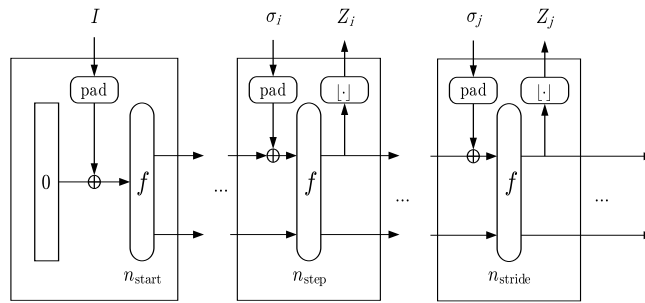


Figure 3.13: The MONKEYDUPLEX construction.

The  $\text{MONKEYDUPLEX}(\mathbf{f}, r, n_{\text{start}}, n_{\text{step}}, n_{\text{stride}})$  construction works as follows:

**start** starts the MONKEYDUPLEX construction on an empty state of  $b$  bits. The operation sets the state with the string  $I$  padded up to  $b$  bits. Here, in the padding, a single bit 1 is appended to  $I$ , followed by the minimum number of

bits 0 followed by a single bit 1 such that the length of the result is a multiple of  $b$ . Subsequently, the permutation function  $\mathbf{f}(n_{\text{start}})$  is applied to the state.

**step** can process an injection of string  $\sigma_i$  of up to  $r - 2$  bits. Here, equal to **start**, padding is applied before an XOR with the current state. Subsequently, the permutation function  $\mathbf{f}(n_{\text{step}})$  is applied to the state. Finally, the first  $l$  bits of the state are extracted (where  $l \leq r$ ), denoted in the figure by  $\lfloor \cdot \rfloor$ .

**stride** is similar to **step**, however, **stride** aims at providing resistance to output forgery on top of providing resistance against state retrieval. As a result, we require  $n_{\text{step}} < n_{\text{stride}}$ .

### 3.6.3 MONKEYWRAP

In this section, we give a brief description of the MONKEYWRAP construction. For a full description we encourage the reader to consult Bertoni et al. [11].

As mentioned, the MONKEYWRAP construction acts as KETJE's AEAD-mode and builds on top of the MONKEYDUPLEX construction. Equivalent to the encryption-scheme  $\mathcal{E}$  and decryption-scheme  $\mathcal{D}$  of the AEAD-scheme  $\Pi$  as described in Definition 2.20, Section 2.6, MONKEYWRAP is composed of a construction to wrap ( $\mathcal{E}$ ) and a construction to unwrap ( $\mathcal{D}$ ). The wrapping construction takes as input a message  $M$  and associated data  $A$  respectively and outputs a cryptogram  $C$  and a tag  $T$  respectively. The unwrapping construction reverses this by taking the associated data  $A$ , a cryptogram  $C$  and a tag  $T$  as input and returning the message  $M$  if the tag  $T$  is correct.

Figure 3.13 illustrates the wrapping of a message and associated data using the MONKEYWRAP construction. In this figure, the MONKEYWRAP key should be a Secret Unique Value (SUV), which means that it is composed of the key  $K$  and a unique nonce  $N$ . An advantage of the construction is that we can produce a tag  $T$  without cryptogram  $C$  by inputting an empty message  $M$ . This is useful for the EA of the FE and the computation of the authenticator  $T^2$  in our protocol.

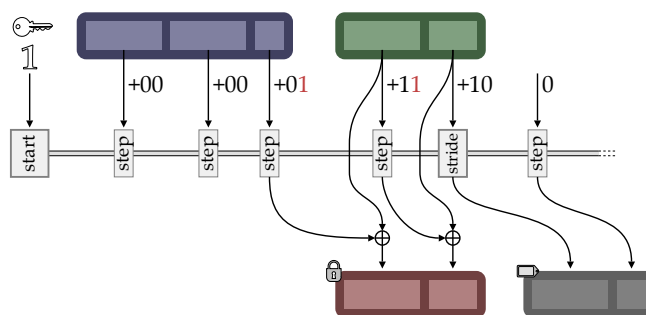


Figure 3.14: The wrapping of a message and authenticated data using the MONKEYWRAP construction.

The **start**, **step** and **stride** operations in the figure are the operations in the MONKEYDUPLEX construction as described in Section 3.6.2. For KETJE the per-

mutation function is  $\mathbf{f} = \text{KECCAK-p}(400)$ , the input blocks are of size  $r = 32$ , the number of rounds in **start** is  $n_{\text{start}} = 12$ , the number of rounds in **step** is  $n_{\text{step}} = 1$  and the number of rounds in **stride** is  $n_{\text{stride}} = 6$ .

## SECURITY ANALYSIS

In this chapter we describe the security analysis of the proposed privacy-preserving authentication protocol, the Concealing KETJE Protocol (CKP). We follow the security analyses of the protocols described by Aysu et al. [3] and Moriyama et al. [48] because of the fact that our protocol is based thereon. By doing this, we also base our security analysis on the indistinguishability-based security model of Juels and Weis [32]. Moreover, we consider an active attacker who is able to desynchronize the shared secret between the device and the server [50]. Hence, we assume that the server and the device are able to execute an honest session before and after the challenge phase in the privacy definition.

In Section 4.1 we describe the security model. Section 4.2 describes the formal security definitions. Finally, in Section 4.3 we prove the security and the privacy of the proposed protocol.

## 4.1 Security Model

In this section we describe the security model, the formal description of the security policy that describes the proposed protocol. We describe the communication model, the theoretical security and the theoretical privacy.

### 4.1.1 Communication Model

With the security considerations described in Section 3.1 in mind, we take one trusted server  $\mathcal{S}(\{Y, Y^{old}\}_n)$  with  $n$  devices  $\mathbf{Dev}_i(\mathbf{puf}_i(\cdot), X)$ . Here, the set of  $n$  devices is denoted as  $\Delta := \{\mathbf{Dev}_0, \mathbf{Dev}_1, \dots, \mathbf{Dev}_{n-1}\}$ . We denote the security parameter as  $k$ .

Following Aysu et al. [3] and Moriyama et al. [48], devices will be enrolled in a trusted environment, this happens in a setup phase using a setup algorithm  $\mathbf{Setup}(1^k)$  which generates public parameter  $P$  and shared-secret  $Y$ . Here  $P$  denotes all the public parameters available to the environment ( $P := X^1 \parallel N^1 \parallel \langle H, N^2, C^1, T^1 \rangle \parallel T^2$  in our protocol) and  $Y$  denotes the secret Physically Unclonable Function (PUF) response. During the authentication phase, the server  $\mathcal{S}$  remains trusted, however, the devices  $\Delta$  and the communication channel will be subjected to the actions of an attacker. At the end of the authentication phase, both the server and the device will output acceptance ( $B_0 = 1$ ) or rejection ( $B_0 = 0$ ) as result of the authentication.

We call the sequence of communication between the server and the device a session, which is distinguished by a session identifier  $I$ . This session identifier  $I$  is the transcript of the authentication phase ( $I := N^1 \parallel \langle H, N^2, C^1, T^1 \rangle \parallel T^2$  in our protocol). Whenever the communication messages generated by the server and the device are honestly transferred until they authenticate each other, we call that a session has a matching session (i.e.  $I$  is untampered with). The correctness of the proposed authentication protocol is that the server and the device always accept the session if the session has the matching session.

### 4.1.2 Security

Following Aysu et al. [3] and Moriyama et al. [48], we consider the canonical security level for authentication protocols, namely the resilience to the Man-in-the-Middle (MitM) attack. This means that the power of an attacker is modeled by letting the attacker control all communication of the protocol. As mentioned earlier, if and only if the communication message is honestly transferred, the authentication results for both the server  $\mathcal{S}$  and the device  $\mathbf{Dev}_i$  will be  $B_0 = 1$ . Supplementary to the security requirement of resilience to MitM attacks, we permit the attacker to access the information stored in the non-volatile memory of the device  $\mathbf{Dev}_i$  in between sessions ( $X$  in our protocol).

Figure 4.1 illustrates the security evaluation on a theoretical level. In this figure,  $\mathbf{Exp}_{\Psi, \mathcal{A}}^{\text{Sec}}(k)$  denotes the security experiment between the proposed protocol  $\Psi$  and an attacker  $\mathcal{A}$  with security parameter  $k$  (128-bits in our protocol).

---


$$\begin{array}{l}
\mathbf{Exp}_{\Psi, \mathcal{A}}^{\text{Sec}}(k) \\
\hline
\langle P, Y \rangle \leftarrow \mathbf{Setup}(1^k) \\
\langle \mathbf{Dev}_i, I' \rangle \leftarrow \mathcal{A}^{\langle \mathbf{Launch}, \mathbf{SendServer}, \mathbf{SendDev}, \mathbf{Result}, \mathbf{Reveal} \rangle}(P, \mathcal{S}, \Delta) \\
B_0 := \mathbf{Result}(\mathbf{Dev}_i, I') \\
\text{Output } B_0 \\
\hline
\end{array}$$


---

Figure 4.1: Security experiment  $\mathbf{Exp}_{\Psi, \mathcal{A}}^{\text{Sec}}(k)$ .

After the setup phase, and thus after receiving  $\langle P, \mathcal{S}, \Delta \rangle$ , the attacker  $\mathcal{A}$  can query the server  $\mathcal{S}$  and the device  $\mathbf{Dev}_i$  with the oracle queries

$\mathcal{O} := \langle \mathbf{Launch}, \mathbf{SendServer}, \mathbf{SendDev}, \mathbf{Result}, \mathbf{Reveal} \rangle$ :

- **Launch**( $1^k$ ): Launch the server  $\mathcal{S}$  to start a new session with security parameter  $k$ .
- **SendServer**( $M$ ): Send an arbitrary message  $M$  to the server  $\mathcal{S}$ .
- **SendDev**( $\mathbf{Dev}_i, M$ ): Send an arbitrary message  $M$  to device  $\mathbf{Dev}_i \in \Delta$
- **Result**( $G, I$ ): Output whether the session  $I$  of  $G$  is accepted or not where  $G \in \{\mathcal{S}, \Delta\}$ .
- **Reveal**( $\mathbf{Dev}_i$ ): Output all the information stored in the Non-Volatile Memory (NVM) of  $\mathbf{Dev}_i$ .

The advantage of attacker  $\mathcal{A}$  against  $\Psi$  is defined as:

$$\mathbf{Adv}_{\Psi, \mathcal{A}}^{\text{Sec}}(k) := \Pr(\mathbf{Exp}_{\Psi, \mathcal{A}}^{\text{Sec}}(k) \rightarrow 1 \mid \text{“}I \text{ of } G \text{ has no matching session”}) \quad (4.1.1)$$

We define security of an authentication protocol as follows:

**Definition 4.1** (Security). *An authentication protocol  $\Psi$  holds the security against MitM attacks with memory compromise if for any probabilistic polynomial time attacker  $\mathcal{A}$ ,  $\mathbf{Adv}_{\Psi, \mathcal{A}}^{\text{Sec}}(k)$  is negligible in  $k$  (for large enough  $k$ ).*

In other words, the security of authentication protocol  $\Psi$  is based on the fact that the advantage of an attacker is insignificant if  $k$  is large enough.

### 4.1.3 Privacy

Following Aysu et al. [3] and Moriyama et al. [48], we define the privacy definition using indistinguishability between two devices. Here, an attacker selects two devices and tries to distinguish the communication, and thus the identification, between the two devices.

We use the privacy experiment between an attacker  $\mathcal{A} := \langle \mathcal{A}_1, \mathcal{A}_2, \mathcal{A}_3 \rangle$  as illustrated in Figure 4.2.

Similar to the security experiment described in Section 4.1.2, the attacker can interact with the devices and the server through the oracle queries

$\mathcal{O} := \langle \mathbf{Launch}, \mathbf{SendServer}, \mathbf{SendDev}, \mathbf{Result}, \mathbf{Reveal} \rangle$ .

$$\begin{array}{l}
\mathbf{Exp}_{\Psi, \mathcal{A}}^{\text{IND}^* - b}(k) \\
\hline
\langle P, Y \rangle \leftarrow \mathbf{Setup}(1^k) \\
\langle \mathbf{Dev}_0^*, I^{0'}, \mathbf{Dev}_1^*, I^{1'} \rangle \leftarrow \mathcal{A}_1^{\mathcal{O}}(P, \mathcal{S}, \Delta) \\
b \leftarrow \{0, 1\} \\
\Delta' := \Delta \setminus \langle \mathbf{Dev}_0^*, \mathbf{Dev}_1^* \rangle \\
\psi_0 \leftarrow \mathbf{Execute}(\mathcal{S}, \mathbf{Dev}_0^*) \\
\psi_1 \leftarrow \mathbf{Execute}(\mathcal{S}, \mathbf{Dev}_1^*) \\
\langle I^{0''}, I^{1''} \rangle \leftarrow \mathcal{A}_2^{\mathcal{O}}(\mathcal{S}, \Delta', \mathcal{I}(\mathbf{Dev}_b^*), \psi_0, I^{0'}, \psi_1, I^{1'}) \\
\psi'_0 \leftarrow \mathbf{Execute}(\mathcal{S}, \mathbf{Dev}_0^*) \\
\psi'_1 \leftarrow \mathbf{Execute}(\mathcal{S}, \mathbf{Dev}_1^*) \\
B_0 \leftarrow \mathcal{A}_3^{\mathcal{O}}(\mathcal{S}, \Delta', \psi'_0, I^{0''}, \psi'_1, I^{1''}) \\
\hline
\text{Output } B_0
\end{array}$$

Figure 4.2: Privacy experiment  $\mathbf{Exp}_{\Psi, \mathcal{A}}^{\text{IND}^* - b}(k)$  in which it is allowed to communicate with two devices.

After the setup-phase, and similar to the security experiment, the attacker interacts with the server and two randomly chosen devices through the oracle queries  $\mathcal{O}$ . These two devices  $\mathbf{Dev}_0^*, \mathbf{Dev}_1^*$  are being sent to the challenger who flips a coin to choose with which device the attacker will communicate anonymously. This anonymous communication is accomplished by adding a special identity  $\mathcal{I}$  which honestly transfers the communication messages between  $\mathcal{A}$  and  $\mathbf{Dev}_b^*$ .

It is trivial that the attacker can trace devices in case the **Reveal** query is issued when there are no successful authentications. Hence, we provide re-synchronization before and after the anonymous access by adding the **Execute** query. This query does a normal protocol execution between the server  $\mathcal{S}$  and the device  $\mathbf{Dev}_i^*$ . During this execution, the attacker can not modify the communications, however the transcript  $\psi_i$  is delivered to the attacker.

The advantage of the attacker is defined as:

$$\mathbf{Adv}_{\Psi, \mathcal{A}}^{\text{IND}^*}(k) := |\mathbf{Pr}(\mathbf{Exp}_{\Psi, \mathcal{A}}^{\text{IND}^* - 0}(k) \rightarrow 1) - \mathbf{Pr}(\mathbf{Exp}_{\Psi, \mathcal{A}}^{\text{IND}^* - 1}(k) \rightarrow 1)| \quad (4.1.2)$$

We define privacy of an authentication protocol as follows:

**Definition 4.2** (Privacy). *An authentication protocol  $\Psi$  holds forward and backward privacy if for any probabilistic polynomial time attacker  $\mathcal{A}$ ,  $\mathbf{Adv}_{\Psi, \mathcal{A}}^{\text{IND}^*}(k)$  is negligible in  $k$  (for large enough  $k$ ).*

In other words, the privacy preservation of authentication protocol  $\Psi$  is based on the fact that the advantage of an attacker is insignificant if  $k$  is large enough.



## 4.2 Formal Security Definitions

In this section, we describe the formal security definitions of the several protocol components by following Aysu et al. [3] and Moriyama et al. [48].

### 4.2.1 Physical Unclonable Function

We define a PUF using the definitions described in Section 2.3 and the definition described by Aysu et al. [3, p. 24].

For this definition we use  $Y \leftarrow \mathbf{puf}_i(X) \in \mathcal{P}$  as a notation for a PUF  $\mathbf{puf}_i \in \mathcal{P}$  which takes challenge  $X$  and produces response  $Y$ . To distinguish between multiple devices, we denote the PUF class  $\mathcal{P}$  as  $\{\mathbf{puf}_0(\cdot), \mathbf{puf}_1(\cdot), \dots, \mathbf{puf}_{n-1}(\cdot)\}$ , where  $n$  is the number of devices. We denote the set of all possible challenges  $X$  which can be applied to an instance of  $\mathcal{P}$  as  $\mathcal{X}_{\mathcal{P}}$ . We say that the PUF class  $\mathcal{P}$  is a  $\langle n, l, d, h, \epsilon \rangle$ -secure PUF class  $\mathcal{P}$  if the following conditions hold:

1. For any PUF instance  $\mathbf{puf}_i(\cdot) \leftarrow \mathcal{P}$  and for any input  $X \leftarrow \mathcal{X}_{\mathcal{P}}$ ,

$$\Pr(\mathbf{dist}(Y \leftarrow \mathbf{puf}_i(X), Y' \leftarrow \mathbf{puf}'_i(X)) < d) = 1 - \epsilon$$

2. For any two PUF instances  $\mathbf{puf}_i(\cdot), \mathbf{puf}_j(\cdot) \leftarrow \mathcal{P}$ , where  $i \neq j$  and for any input  $X \leftarrow \mathcal{X}_{\mathcal{P}}$ ,

$$\Pr(\mathbf{dist}(Y \leftarrow \mathbf{puf}_i(X), Y' \leftarrow \mathbf{puf}_j(X)) > d) = 1 - \epsilon$$

3. For any PUF instance  $\mathbf{puf}_i(\cdot) \leftarrow \mathcal{P}$  and for any two inputs  $X^a, X^b \leftarrow \mathcal{X}_{\mathcal{P}}$ , where  $a \neq b$ ,

$$\Pr(\mathbf{dist}(Y \leftarrow \mathbf{puf}_i(X^a), Y' \leftarrow \mathbf{puf}_i(X^b)) > d) = 1 - \epsilon$$

4. For any PUF instance  $\mathbf{puf}_i(\cdot) \leftarrow \mathcal{P}$  and for any input  $X^a \leftarrow \mathcal{X}_{\mathcal{P}}$ ,

$$\Pr(\tilde{\mathbf{H}}_{\infty}(Y \leftarrow \mathbf{puf}_i(X^a) \mid \{Y^j \leftarrow \mathbf{puf}_j(X^b)\}_{0 \leq j < n, 0 \leq b < l, i \neq j, a \neq b}) > h) = 1 - \epsilon$$

These conditions provide that the intra-distance  $\mathcal{D}_{\mathcal{P}}^{\text{intra}}$  is smaller than  $d$ , the inter-distance  $\mathcal{D}_{\mathcal{P}}^{\text{inter}}$  (from two metrics) is larger than  $d$  and the min-entropy of the PUF class  $\mathcal{P}$  is always larger than  $h$ .

**Definition 4.3** ( $\langle n, l, d, h, \epsilon \rangle$ -secure PUF class  $\mathcal{P}$ ). *A PUF class  $\mathcal{P}$  satisfies  $\langle n, l, d, h, \epsilon \rangle$ -secure PUF class  $\mathcal{P}$  if all the above conditions hold.*

### 4.2.2 Fuzzy Extractor

We define a Fuzzy Extractor (FE) using the definitions described in Section 2.5 and the definition described by Aysu et al. [3, p. 24].

A  $\langle d, h, \epsilon \rangle$ -FE consists of two algorithms: a key generation algorithm **Gen** and a reconstruction algorithm **Rec**. **Gen** takes as input variable  $Z$  and outputs key  $R$  and helper data  $H$ . For correctness, **Rec** recovers the key  $R$  from input variable  $Z'$  and helper data  $H$  if the distance **dist** between  $Z$  and  $Z'$  is at most  $d$ . The FE provides unpredictable outputs if the min-entropy of input  $Z$  is at least  $h$ . In that case,  $R$  is statistically  $\epsilon$ -close to a uniformly random variable in  $\{0, 1\}^k$ , even if the helper data  $H$  is disclosed.

**Definition 4.4** ( $\langle d, h, \epsilon \rangle$ -secure FE). *A FE satisfies  $\langle d, h, \epsilon \rangle$ -secure FE if the following conditions hold:*

1.  $\Pr(R := \mathbf{Rec}(Z', H) \mid \langle R, H \rangle = \mathbf{Gen}(Z), \mathbf{dist}(Z, Z') \leq d) = 1$
2. If  $\tilde{\mathbf{H}}_\infty(Z) \geq h$ ,  $\langle R, H \rangle = \mathbf{Gen}(Z)$  is statistically  $\epsilon$ -close to  $\langle R', H \rangle$  where  $R' \leftarrow \{0, 1\}^k$  is chosen uniformly at random.

### 4.2.3 AEAD-scheme

We take the definition of an AEAD-scheme  $\Pi$  from Definition 2.20, Section 2.6.

The security of the AEAD-scheme  $\Pi$  is defined by the following experiment (Chosen-Plaintext Attack (CPA)) between a challenger and an attacker  $\mathcal{A}$ :

1. First, the challenger randomly selects coin  $b \leftarrow \{0, 1\}$  and secret key  $K \leftarrow \{0, 1\}^k$ .
2. The challenger then prepares a truly random function **RF**.
3. The attacker  $\mathcal{A}$  can adaptively issue an oracle query to the challenger to obtain a response of a function.
  - (a) If  $b = 1$  and the attacker  $\mathcal{A}$  sends message  $M \leftarrow \{0, 1\}^*$ , challenge  $N \leftarrow \{0, 1\}^k$  and associated data  $A \leftarrow \{0, 1\}^*$ , the challenger responds with  $\langle C, T \rangle = \mathcal{E}_K^{N, A}(M)$ .
  - (b) On the other hand, if  $b = 0$ , the challenger inputs the message  $M \leftarrow \{0, 1\}^*$ , challenge  $N \leftarrow \{0, 1\}^k$  and associated data  $A \leftarrow \{0, 1\}^*$  to **RF** and responds with its result  $\langle C', T' \rangle$ .
4. Finally, the attacker outputs a guess  $b'$ . If  $b' = b$ , the attacker wins the experiment.

Similarly, this construction can be applied to test the security of the decryption algorithm  $\mathcal{D}_K^{N, A}(\langle C, T \rangle)$ .

The advantage of the attacker to win the experiment is defined by  $\mathbf{Adv}_\mathcal{A}^\Pi(k) = |2 \cdot \Pr(b' = b) - 1|$ .

**Definition 4.5** ( $\epsilon$ -secure AEAD-scheme). *An AEAD-scheme is an  $\epsilon$ -secure AEAD-scheme if for any probabilistic polynomial time attacker  $\mathcal{A}$ ,  $\mathbf{Adv}_\mathcal{A}^\Pi(k) \leq \epsilon$ .*

## 4.3 Security Proofs

In this section, we give the security proof and privacy proof for the proposed protocol. We follow the proof by game-transformations as described by Aysu et al. [3] and Moriyama et al. [48].

### 4.3.1 Security

**Theorem 4.1 (Security).** *Let PUF instance  $\text{puf}^* \leftarrow \mathcal{P}$  be a  $\langle n, l, d, h, \epsilon_1 \rangle$ -secure PUF, FE be a  $\langle d, h, \epsilon_2 \rangle$ -secure FE and the AEAD-scheme be an  $\epsilon_3$ -secure AEAD-scheme. Then our protocol  $\Psi$  is secure against MitM attacks with memory compromise. Especially, we have  $\text{Adv}_{\Psi, \mathcal{A}}^{\text{Sec}}(k) \leq l \cdot n \cdot (\epsilon_1 + \epsilon_2 + \epsilon_3)$ .*

*Proof.* The aim of the attacker  $\mathcal{A}$  is to violate the security experiment which means that either the server or a device accepts a session without it being the matching session. We call  $S_i$  the advantage that the attacker wins the game in **Game**  $i$ . We consider the following game transformations:

**Game 0:** This is the original game between the challenger and the attacker.

**Game 1:** The challenger randomly guesses the device  $\text{Dev}^* \leftarrow \Delta$ . If the attacker does not impersonate  $\text{Dev}^*$  to the server, the challenger aborts the game. Thus, the attacker needs to participate in session  $I^*$  and cannot tamper with the communication.

**Game 2:** Assume that  $l$  is the upper bound of the number of sessions that the attacker can establish in the game. For  $0 \leq j < l$ , we evaluate or change the variables related to the session between the server and  $\text{Dev}^*$  up to the  $l$ -th session as the following games:

**Game 2- $j$ -1:** The challenger evaluates the output from the PUF instance  $\text{puf}^*$  implemented in  $\text{Dev}^*$  at the  $j$ -th session. If the intra-distance is larger than  $d$ , the inter-distance is smaller than  $d$  or the min-entropy of the output is smaller than  $h$ , the challenger aborts the game.

**Game 2- $j$ -2:** The output from the FE  $H$  is changed to a random variable.

**Game 2- $j$ -3:** The output from the encryption algorithm  $\mathcal{E}_R^{N||0, A}(Y)$  of the AEAD-scheme is derived from a truly random function **RF**.

**Game 2- $j$ -4:** The output from the encryption algorithm  $\mathcal{E}_R^{N||1, A}(\cdot)$  of the AEAD-scheme is derived from a truly random function **RF**.

The strategy of the security proof is to change the communication messages corresponding to the target device  $\text{Dev}^*$  to random variables. However, we must take care of the PUF construction and challenge-update mechanism in our protocol that updates the secret PUF response  $Y$ . Hence, we must proceed with the game transformation starting from the first invocation of device  $\text{Dev}^*$ . The communication messages gradually change from **Game 2- $j$ -1** to **Game 2- $j$ -4**, and when these are finished, we can move to the next session. This strategy is recursively applied up to the upper bound of  $l$  of the sessions that the attacker can establish.

In short, if the implemented PUF instance creates enough entropy, the FE can provide variables that are statistically close to random strings. Then, this output can be applied as a key for the AEAD-scheme which both authenticates the device as well as encrypts the next secret PUF response  $Y^2$ . Finally, the server can be authenticated using the AEAD-scheme without encrypting a message.

**Lemma 4.1** (Random Guess).  $S_0 = n \cdot S_1$  (where  $n$  is the number of devices).

*Subproof.* The violation of security means that there is a session which the server or device accepts while the communication is modified by the attacker. Since we assume that the number of devices is at most  $n$ , the challenger can correctly guess the related session with a probability of at least  $1/n$ .  $\diamond$

**Lemma 4.2** (PUF Response).  $|S_1 - S_{2-1-1}| \leq \epsilon_1$  and  $|S_{2-(j-1)-4} - S_{2-j-1}| \leq \epsilon_1$  for any  $1 \leq j < l$  if the PUF instance  $\mathbf{puf}^*$  is a  $\langle n, l, d, h, \epsilon_1 \rangle$ -secure PUF.

*Subproof.* We now assume that the PUF instance  $\mathbf{puf}^*$  satisfies a  $\langle n, l, d, h, \epsilon_1 \rangle$ -secure PUF in advance. This means that the intra-distance  $\mathcal{D}_{\mathcal{P}}^{\text{intra}}$  is smaller than  $d$ , the inter-distance  $\mathcal{D}_{\mathcal{P}}^{\text{inter}}$  is larger than  $d$  and the min-entropy of the PUF class  $\mathcal{P}$  is always larger than  $h$  except the negligible probability  $\epsilon_1$ . Since  $S_1$  and  $S_{2-(j-1)-4}$  assume these conditions except the negligible probability  $\epsilon_1$  and  $S_{2-1-1}$  and  $S_{2-j-1}$  require these conditions with probability 1, respectively, the gap between them is bounded by  $\epsilon_1$ .  $\diamond$

**Lemma 4.3** (FE Output).  $\forall 0 \leq j < l, |S_{2-j-1} - S_{2-j-2}| \leq \epsilon_2$  if the FE is a  $\langle d, h, \epsilon_2 \rangle$ -secure FE.

*Subproof.* From the subproof of Lemma 4.2, we can assume that the PUF instance  $\mathbf{puf}^*$  provides enough min-entropy  $h$ . Then the property of the  $\langle d, h, \epsilon_2 \rangle$ -secure FE guarantees that the output for the FE is statistically close to random and no attacker can distinguish the difference between the two games.  $\diamond$

**Lemma 4.4** (Authenticated Encryption).  $\forall 0 \leq j < l, |S_{2-j-2} - S_{2-j-3}| \leq \mathbf{Adv}_{\mathcal{A}}^{\Pi}(k)$  for a probabilistic polynomial time algorithm  $\mathcal{B}$ .

*Subproof.* We construct the algorithm  $\mathcal{B}$  which breaks the security of our AEAD-scheme  $\Pi$ .  $\mathcal{B}$  can access the real encryption algorithm  $\mathcal{E}_R^{N||0,A}(Y)$ , the real decryption algorithm  $\mathcal{D}_R^{N||0,A}(\langle C^1, T^1 \rangle)$  or the truly random function  $\mathbf{RF}$ .  $\mathcal{B}$  sets up all secret keys and simulates our protocol except the  $n$ -th session (the current session). When the attacker invokes the  $n$ -th session  $\mathcal{B}$  sends the uniformly random distributed challenge  $A \leftarrow \{0, 1\}^k$  as the output of the server. When the attacker  $\mathcal{A}$  sends the challenge  $A^*$  to a device  $\mathbf{Dev}_i$ ,  $\mathcal{B}$  randomly selects a nonce  $N$  and issues this to the oracle instead of the real computation of  $\mathcal{E}_R^{N||0,A}(Y)$ . Upon receiving  $\langle C, T \rangle$ ,  $\mathcal{B}$  continues the computation as the protocol specification and outputs  $\langle H, N, C^1, T^1 \rangle$  as the device's response. When the attacker sends  $\langle H^*, N^*, C^{1*}, T^{1*} \rangle$ ,  $\mathcal{B}$  issues challenge  $A$  and nonce  $N^*$  to the oracle and obtains either  $Y$  or the distinguished symbol INVALID.

If  $\mathcal{B}$  accesses the real encryption and decryption algorithms  $\langle \mathcal{E}, \mathcal{D} \rangle$ , this simulation

is equivalent to **Game** 2- $j$ -2. Otherwise, the oracle query issued by  $\mathcal{B}$  is completely random and this distribution is equivalent to **Game** 2- $j$ -3. Thus we have  $|S_{2-j-2} - S_{2-j-3}| \leq \text{Adv}_{\mathcal{A}}^{\Pi}(k)$ .  $\diamond$

**Lemma 4.5** (Authentication).  $\forall 0 \leq j < l$ ,  $|S_{2-j-3} - S_{2-j-4}| \leq 2 \cdot \text{Adv}_{\mathcal{A}}^{\Pi}(k)$  for a probabilistic polynomial time algorithm  $\mathcal{B}$ .

*Subproof.* Consider an algorithm  $\mathcal{B}$  which interacts with the encryption algorithm  $\mathcal{E}_R^{N||1,A}(\cdot)$  and truly random function **RF**.  $\mathcal{B}$  runs the setup procedure and simulates the protocol up to the  $n$ -th session. Similarly to the subproof of Lemma 4.4, when the attacker invokes the  $n$ -th session  $\mathcal{B}$  sends the uniformly random distributed challenge  $A \leftarrow \{0, 1\}^k$  as the output of the server.  $\mathcal{B}$  continues the computation as the protocol specification and outputs  $\langle H, N, C^1, T^1 \rangle$  as the device's response. If the attacker  $\mathcal{A}$  has sent the challenge  $A^*$  to a device  $\text{Dev}_i$ ,  $\mathcal{B}$  randomly selects nonce  $N$  and issues this to the oracle instead of the real computation  $\mathcal{E}_R^{N||1,A}(\cdot)$ . When the attacker sends  $\langle H^*, N^*, C^{1*}, T^{1*} \rangle$ ,  $\mathcal{B}$  issues challenge  $A$  and nonce  $N^*$  to the oracle and obtains  $T^2$ .

If  $\mathcal{B}$  accesses the real encryption algorithm  $\mathcal{E}$ , this simulation is equivalent to **Game** 2- $j$ -3. Otherwise, the oracle query issued by  $\mathcal{B}$  is completely random and this distribution is equivalent to **Game** 2- $j$ -4. Thus we have  $|S_{2-j-3} - S_{2-j-4}| \leq \text{Adv}_{\mathcal{A}}^{\Pi}(k)$ .  $\diamond$

When we transform **Game** 0 to **Game** 2- $l$ -4, there is no advantage of the attacker to violate the security. Given the fact that the attacker knows the PUF challenge  $X$  from the device's NVM, the attacker cannot produce a valid PUF response. This results in the fact that the attacker cannot produce a key  $R$  which matches any of the keys in the server's database. This means that the cryptogram produced by an attacker will never be accepted by the decryption algorithm of the AEAD-scheme in the server. Additionally, changing the authenticator  $T^2$  will only prevent the device from updating its PUF challenge, this is why the server also performs an exhaustive search over the old  $(j - 1)$  PUF responses.

Therefore, no attacker can successfully mount the MitM attack in our proposed protocol.  $\square$

### 4.3.2 Forward and Backward Privacy

In this section, we give the privacy proof for the proposed protocol.

**Theorem 4.2 (Privacy).** *Let PUF instance  $\mathbf{puf}^* \leftarrow \mathcal{P}$  be a  $\langle n, l, d, h, \epsilon_1 \rangle$ -secure PUF, FE be a  $\langle d, h, \epsilon_2 \rangle$ -secure FE and the AEAD-scheme be an  $\epsilon_3$ -secure AEAD-scheme. Then our protocol  $\Psi$  holds forward and backward privacy.*

*Proof.* This proof will be similar to the proof of Theorem 4.1. However, we remark that it is important to assume that our protocol satisfies security first for privacy to hold. This is because if security does not hold, a malicious attacker might be able to desynchronize the secret PUF response  $Y$  of device  $\mathbf{Dev}^*$  to a chosen one. In that case, even if the attacker honestly transfers the communication message between  $\mathcal{I}(\mathbf{Dev}^*)$  and the server in the challenging phase the authentication result is always  $B_0 = 0$  and the adversary can observe whether device  $\mathbf{Dev}^*$  was selected as the challenge device.

Based on the same **Game** transformation that was describes in the proof of Theorem 4.1, we continuously change the communication messages for the device  $\mathbf{Dev}^*$ , however, we now call this device  $\mathbf{Dev}_1^*$ . We do a similar game transformation for a second target device  $\mathbf{Dev}_2^*$ . In **Game 1**, the attacker can guess which device will be chosen by the challenger in the privacy game with probability of at least  $1/n^2$ . Upon continuing, the game transformation in **Game 2** is applied to the sessions related to device  $\mathbf{Dev}_1^*$  and device  $\mathbf{Dev}_2^*$ . Then, all the message transcripts of the **Game** transformations are changed to random variables and no biased information which identifies the challenger's coin is leaked. Also here, information stored in the NVM ( $X$  in our protocol) of devices  $\mathbf{Dev}_1^*$  and  $\mathbf{Dev}_2^*$  will not disclose any information because these memories are updated from random sources.

Therefore, no attacker can distinguish any two devices with probability higher than  $1/n^2$ , hence, the proposed protocol satisfies forward and backward privacy.  $\square$

## PROOF OF CONCEPT

Following the protocol design as described in Chapter 3, this chapter gives a proof of concept of the proposed protocol. To this end, we implement the device on a Zedboard and the server on a Linux PC.

In Section 5.1 we describe the architecture of the system. Accordingly, in Section 5.2 we describe the architecture of the device for which we describe the 3-1 Double Arbitrator PUF (DAPUF), Bose-Chaudhuri-Hocquenghem (BCH) encoder and KETJE in more detail. Finally, in Section 5.3 we describe the server implementation.

## 5.1 System Architecture

Figure 5.1 illustrates the system architecture of the device and server. The device is implemented on a Zedboard which contains a Xilinx Zynq-7000 All Programmable System on Chip (SoC) XC7Z020-CLG484-1 (see Appendix A.1 for specifications). The server is implemented on a Linux PC. We design the system architecture using Xilinx Vivado and the Xilinx Vivado Software Development Kit (SDK).

The Zynq SoC is composed of 28 nm Programmable Logic (PL) and a Processing System (PS), which can both be programmed through the Universal Serial Bus (USB) Joint Test Action Group (JTAG). Apart from other components, the PS contains two Advanced RISC Machine (ARM)-cores, of which one is used to:

1. control the communication between the device and the server by reading and writing Advanced Extensible Interface (AXI)-addresses from the device and sending and receiving serial data through the Universal Asynchronous Receiver/Transmitter (UART);
2. update the Physically Unclonable Function (PUF) challenge on the device Non-Volatile Memory (NVM) by re-writing to a SD-card plugged into the Zedboard.

The central communication travels through a bus, the Central Interconnect (CI), which is connected with all the components on the Zynq. Communication between the device and the ARM-core is supported with a 32-bit AXI.

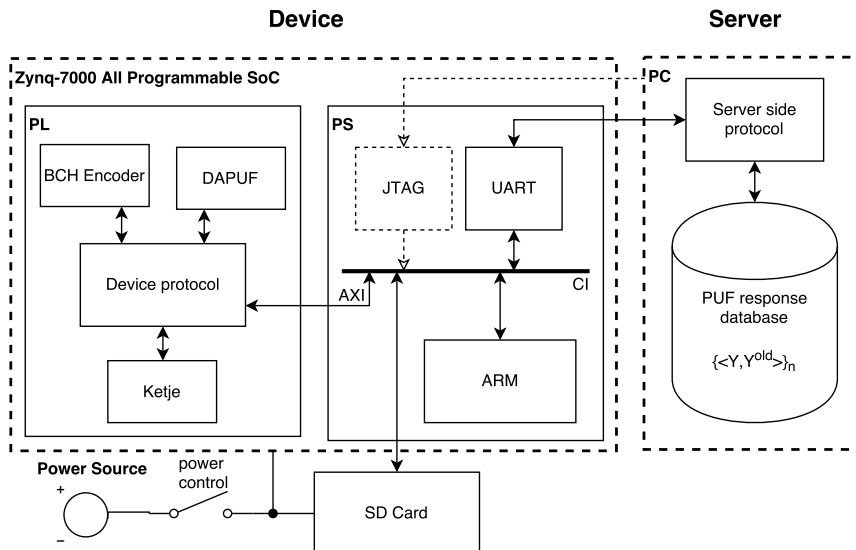


Figure 5.1: System architecture of the Device and Server.



## 5.2 Device

In this section we describe the architecture of the device. We describe the architectures of the DAPUF, BCH encoder and KETJE in more detail. The source code of the device is given in Appendix C.2.1. We design the device in VHSIC Hardware Description Language (VHDL) using Xilinx Integrated Development Environment (IDE) for High Level Synthesis (HLS) and Xilinx ISE Simulator (iSim) for testing.

Figure 5.2 illustrates the floor-planning of the device as generated by Xilinx Vivado. In this figure, in the top left, the full area of the SoC is illustrated; on the right side the area is illustrated that contains the device logic. The green area represents the PS which uses the yellow, purple and pink logic to set and reset the AXI peripherals. Furthermore, four Physical Blocks (Pblocks) have been defined to constrain the DAPUF component (white logic), the BCH encoder (light blue logic), the KETJE component (orange logic) and the controller (blue logic) to specific areas on the SoC. The three selector chains of the DAPUF are clearly visible (in white).

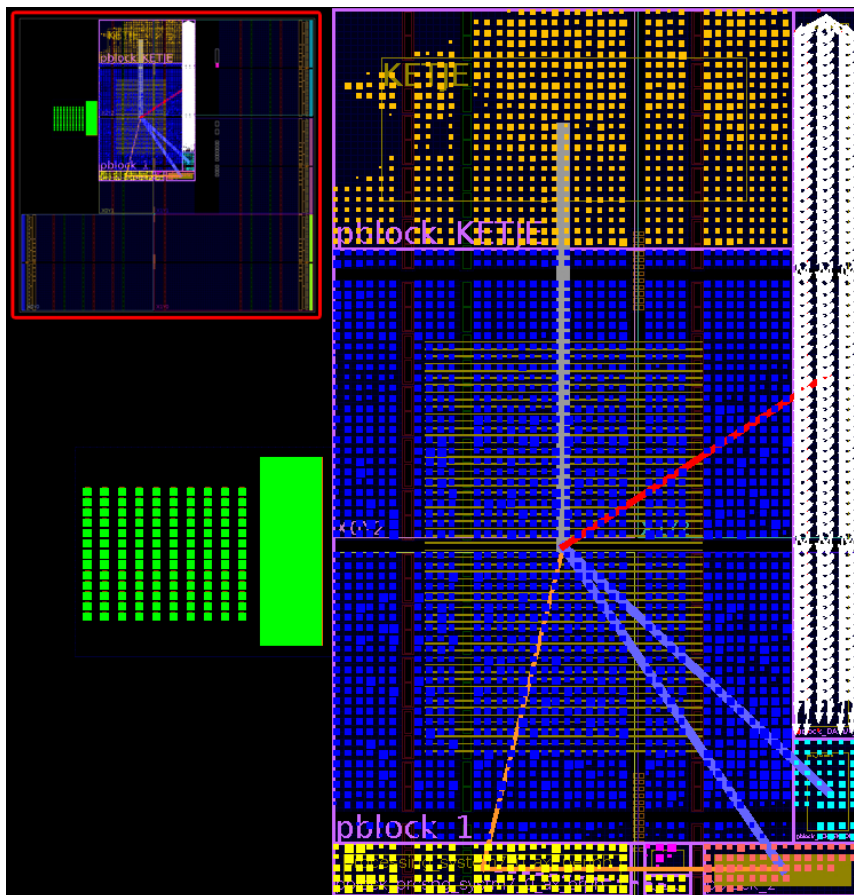


Figure 5.2: Floor-planning of the device.

The controller (blue logic) is composed of seven processes:

**Main process** : The main process handles all responses for the DAPUF and starts the other processes accordingly. The order of the various subprocesses can be summarized as follows:

1. Update the seed by challenging the DAPUF.
2. Generate the PUF response  $Y^{1'}$  by challenging the DAPUF. Subsequently, the repetition encoder process is started.
3. Generate the random value for BCH encoding by challenging the DAPUF. Subsequently, the BCH encoder process is started.
4. Generate the challenge  $N$  by challenging the DAPUF. Subsequently, the KETJE mode is set to accumulate the entropy of the PUF response  $Y^{1'}$ . Finally, the KETJE process is started.
5. Generate the second challenge  $X^2$  by challenging the DAPUF.
6. Generate the second PUF response  $Y^2$  by challenging the DAPUF. Subsequently, the KETJE mode is set to encrypt the second PUF response  $Y^2$ . Finally, the KETJE process is started.
7. When the KETJE process is finished the KETJE mode is set to compute the authenticator  $T^{2'}$  and the KETJE process is started.
8. Finally, the process waits to receive the authenticator  $T^2$  from the server and compares this with  $T^{2'}$ . If they are equal, the challenge  $X$  is updated with  $X^2$ .

**DAPUF challenger process:** This process challenges the DAPUF by setting an ‘enable’ signal and the challenge at the first clock cycle. At the third clock cycle, the response is either 0 or 1. This process is repeated every three clock cycles.

**Linear Feedback Shift Register (LFSR) process:** This process feeds the PUF challenge space. It can operate on two modes, either to feed challenges for the 1275-bit PUF responses, or to feed challenges for the random variables. For both modes, 12 bits have been reserved in the challenge space. As a result the full challenge space of 64 bits is decreased to  $64 - 12 - 12 = 40$ -bit challenges per authentication. More about this, and about the distribution of the bits, is explained in Section 6.1. The LFSR is either reset with initial value  $[0, 1, 0, 1, 0, 1, 0, 1, 0, 1, 0, 1]$ , or with the seed as the initial value.

**Repetition encoder process:** The repetition encoder encodes the DAPUF response and sets the results to the output. The 255-bit DAPUF response is fed to the BCH encoder.

**BCH encoder process:** The BCH encoder encodes the 255-bit using a random number generated by the DAPUF and sets the results to the output.

**KETJE mode process:** This process sets KETJE’s values according to a specified mode. This mode either signals to accumulate the entropy of the PUF response  $Y^{1'}$ , to encrypt the second PUF response  $Y^2$ , or to compute the authenticator  $T^{2'}$ .

**KETJE process:** This process feeds all input data to the KETJE component at the correct clock cycles. Depending on the mode KETJE is running, inputting the message  $M$  is skipped or not. As a result, the cipher-text and tag is received or only the tag.

### 5.2.1 DAPUF

As mentioned in Section 3.4 we implement the DAPUF as proposed by Machida et al. [39]. We obtained the source code designed for a Xilinx Virtex-7 from Machida et al. and adapted this to work for the Xilinx Zynq. This design heavily relies on the constraints that set the specific logic and location of the components in Vivado. These constraints can be set using the following Tool Command Language (Tcl) commands:

```
set_property BEL <logic-type> [get_cells <address>]
set_property LOC <slice> [get_cells <address>]
```

Where `<logic-type>` is replaced with the desirable type of logic, `<slice>` with the desirable slice location and `<address>` with the specific address of the component in Vivado's Netlist. Without these constraints, Vivado will replace the Multiplexers (MUXes) with Look-Up Tables (LUTs) because these require less area and can operate on a higher frequency. The source code of the implemented DAPUF is given in Appendix C.2.3 and the constraints in Appendix C.2.4.

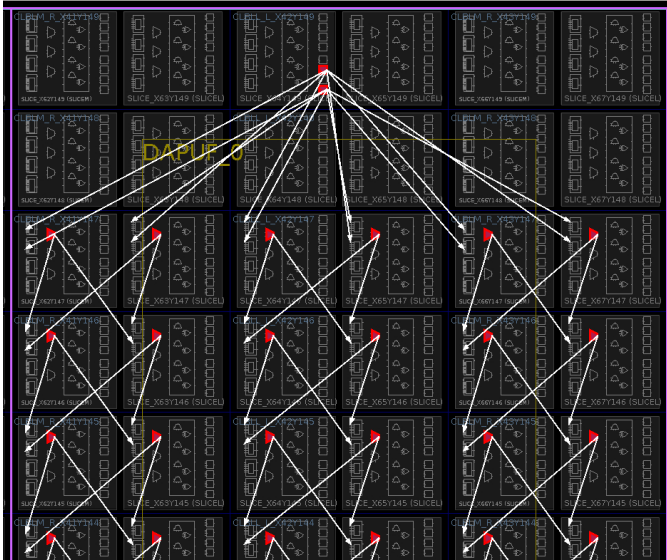
Figure 5.3a illustrates the floor-planning of the first three switch blocks in the three selector chains of the DAPUF as generated by Xilinx Vivado. In the top of the figure, the two registers that contain the 'enable' signals  $E_L$  and  $E_R$  are illustrated. Then, in three columns all MUXes are constrained to their own logic slice such that path-lengths are equal for equivalent paths.

Figure 5.3b illustrates the floor-planning of the last switch blocks and the arbiters of the DAPUF as generated by Xilinx Vivado. Also here, all MUXes and negative-ANDs (NANDs) are constrained to their own logic slice such that path-lengths are equal for equivalent paths.

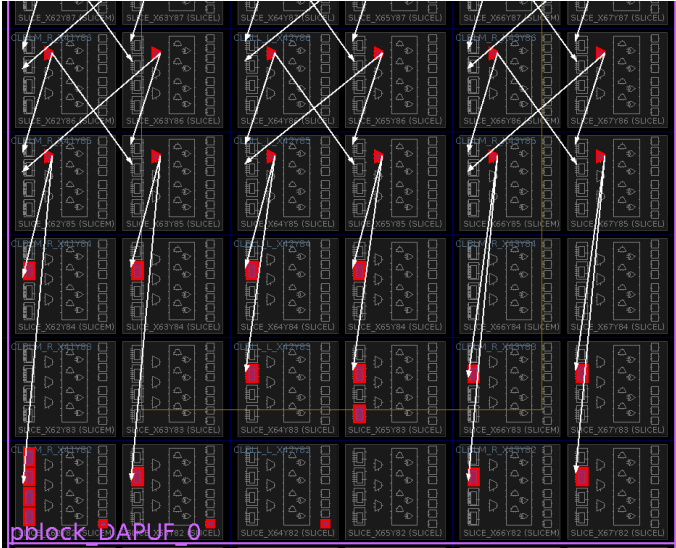
Because of the fact that race conditions are undesirable in conventional Field Programmable Gate Array (FPGA) designs, the following Tcl command should be used as a pre-script to Vivado's bitstream generation:

```
set_property SEVERITY {Warning} [get_drc_checks LUTLP-1]
```

Without this command, Vivado will not allow to generate the bitstream that is needed to program the PL through the USB JTAG.



(a) Floorplanning of the start.



(b) Floorplanning of the finish.

Figure 5.3: Floorplanning of 3-1 Double Arbiter PUF.

### 5.2.2 BCH Encoder

The implemented BCH encoder is designed using a paper by Mathew et al. [46]. The source code of the implemented BCH encoder is given in Appendix C.2.5.

Figure 5.4 illustrates the LFSR that is constructed using the generator polynomial  $\mathbf{g}(x)$  as was calculated in Section 3.5.3.2. We omitted the exponents 9 to 107 in the formula and the figure for clarity:

$$\mathbf{g}(x) = x^{116} + x^{114} + x^{111} + x^{108} + \dots + x^8 + x^4 + x^3 + 1$$

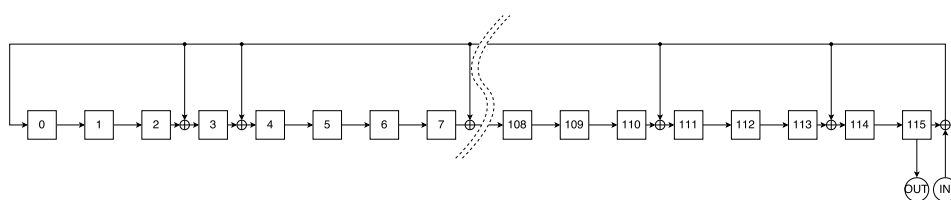


Figure 5.4: Block diagram of the BCH encoder.  $\oplus$  denotes an exclusive-OR (XOR),  $\textcircled{\text{IN}}$  denotes the input bit,  $\textcircled{\text{OUT}}$  denotes the output bit. The indices correspond to the bit locations and the exponents of the generator polynomial  $\mathbf{g}(x)$ .

Using this architecture, in 139 clock cycles, the coefficients of the random BCH input polynomial  $\mathbf{m}(x)$  are fed to the LFSR. Once this is finished, in 116 clock cycles, the coefficients of the redundancy polynomial  $\mathbf{r}(x)$  are obtained. Finally, in the controller these two can be concatenated to obtain the codeword polynomial  $\mathbf{w}(x)$ .

### 5.2.3 KETJE

We obtained the source code of the KETJE hardware implementation from Bertoni et al.. The received implementation is designed for the Competition for Authenticated Encryption: Security, Applicability and Robustness (CAESAR) and thus follows the George Mason University (GMU) hardware Application Program Interface (API) for authenticated ciphers [31]. Because this Authenticated Encryption with Associated Data (AEAD)-core is excessively large, we only use the KETJE cipher-core. This cipher-core can perform encryption with message  $\langle C, T \rangle = \mathcal{E}_K^{N,A}(M)$ , encryption without message  $\langle \cdot, T \rangle = \mathcal{E}_K^{N,A}(\cdot)$  and decryption  $\mathcal{D}_K^{N,A}(\langle C, T \rangle)$ . Moreover, it supports sessions such that session based encryption and decryption is possible. We need the KETJE hardware implementation for encryption (for which we have fixed input sizes) but not for decryption. Although this cipher-core is still too large for our purposes, we accept the overhead.

### 5.3 Server

The server is implemented on a Linux PC using the Python programming language version 2.7.10 [53]. The source code is given in Appendix C.2.5.

Algorithm 1 gives the server-side setup procedure, which is performed in a trusted environment. We rely on serial communication between the PC and the Zedboard through the USB UART.

---

**Algorithm 1** Server-side setup procedure

---

```
1: procedure MAIN
2:    $X^1 \leftarrow \text{TRNG}(40)$            ▷ generate random bit-string of length 40
3:    $\text{DEVICE} \leftarrow X^1$            ▷ send serial data to device
4:    $Y^1 \leftarrow \text{DEVICE}$          ▷ receive serial data from device
5:    $\mathcal{Y}[n] \leftarrow Y^1$          ▷  $n$ : number of devices
6:    $\mathcal{Y}^{\text{old}}[n] \leftarrow Y^1$ 
7:    $n := n + 1$ 
8:   return 1
```

---

Algorithm 2 gives the server-side authentication procedure. Note that because of the conditional branches, this implementation does not prevent an attacker from performing Side-Channel Analysis (SCA). However, for simplicity, in Section 3.1 we stated that an attacker can not perform any implementation attacks. In order to prevent an attacker from successfully performing SCA attacks, one should design a leakage resilient implementation using sound cryptographic engineering.

Also note that the authentication procedure both tries to authenticate devices over the most recent PUF responses as well as the older PUF responses. This is needed because in the event of a loss of connection (card tearing) in the last communication (receiving the authenticator  $T^2$  from the server), a desynchronization will take place between the server and the device.

**Algorithm 2** Server-side authentication procedure

---

```

1: procedure MAIN
2:    $T^2 \leftarrow \text{TRNG}(128)$  ▷ generate random bit-string of length 128
3:    $B_0 := 0$  ▷ set authentication result to 0
4:    $A \leftarrow \text{START}$ 
5:    $H, N, C^1, T^1 \leftarrow \text{DEVICE}$  ▷ receive serial data from device
6:   for  $0 \leq i < n$  do ▷  $n$ : number of devices
7:      $Y \leftarrow \mathcal{Y}[i]$ 
8:      $B_0, T^2 \leftarrow \text{AUTHENTICATETRY}(Y, H, C^1, T^1, A, N, T^2)$ 
9:      $Y \leftarrow \mathcal{Y}^{\text{old}}[i]$ 
10:     $B_0, T^2 \leftarrow \text{AUTHENTICATETRY}(Y, H, C^1, T^1, A, N, T^2)$ 
11:    $\text{DEVICE} \leftarrow T^2$  ▷ send serial data to device
12:   return  $B_0$ 
13: procedure START
14:    $A \leftarrow \text{TRNG}(40)$  ▷ generate random bit-string of length 40
15:    $\text{DEVICE} \leftarrow A$  ▷ send serial data to device
16:   return  $A$ 
17: procedure AUTHENTICATETRY( $Y, H, C^1, T^1, A, N, T^2$ )
18:    $R \leftarrow \text{FE.REC}(Y, H)$ 
19:   if  $Y^2 \leftarrow \text{KETJE.DEC}(R, C^1, T^1, N \parallel 0, A)$  then
20:      $T^2 \leftarrow \text{KETJE.ENC}(R, [], N \parallel 1, A)$ 
21:      $\mathcal{Y}[i] \leftarrow Y^2$ 
22:      $\mathcal{Y}^{\text{old}}[i] \leftarrow Y$ 
23:      $B_0 := 1$  ▷ update the authentication result to 1
24:   return  $B_0, T^2$ 
25: procedure FE.REC( $Y, H$ )
26:    $R' := []$ 
27:   for  $0 \leq i < 255$  do
28:      $R' += [\text{REP.DEC}(Y[i \cdot 5 : i \cdot 5 + 5], H[i \cdot 4 : i \cdot 4 + 4])]$ 
29:    $R'' \leftarrow \text{BCH.DEC}(R', H)$ 
30:   return  $R''$ 
31: procedure REP.DEC( $y, h$ )
32:    $s := [y[0] \text{ xor } y[i + 1] \text{ xor } h[i] \text{ for } i \text{ in range}(4)]$ 
33:   if  $\text{sum}(s) > 2$  then ▷ Hamming weight of the syndrome vector
34:      $e := 1$ 
35:   else
36:      $e := 0$ 
37:   return  $e \text{ xor } y[0]$ 

```

---





RESULTS

This chapter describes the research results of the protocol. We both describe results from the protocol as supported by the mathematical foundation as well as results from the protocol supported by the proof of concept.

In Section 6.1 we calculate the quality of the Physically Unclonable Function (PUF) responses and compare these to the specified quality by Machida et al. [39]. Section 6.2 summarizes the hardware performance in terms of timing and utilization. Following, in Section 6.3 we discuss the software performance. In Section 6.4 we analyze our protocol using a benchmark for PUF-based authentication protocols [17]. Finally, in Section 6.5 we compare our protocol with the protocol proposed by Moriyama et al. [48] and Aysu et al. [3].

## 6.1 PUF Response Analysis

Although in Section 3.5.1 we assumed that all the PUF response bits are independent, we found out this is not the case. This is best illustrated with Figure 6.1a. In this figure we see two PUF selector chains each having two data paths. These selector chains have been initialized with two different challenges that only differ at the Least Significant Bits (LSBs). We can see that by doing this, the length of the path fragments that differ in both selector chains is very small. As a result, the probability that the results of the arbiters are different is small. A possible reason why this is not reflected in the results by Machida et al. [39] is that they challenge the PUF instances with random challenges (weak unpredictability, see Definition 2.13, Section 2.3.4). Moreover, the Machine Learning (ML) algorithm is trained with only 1,000 training samples, which means that the probability of having two challenges with low Hamming distance is small.

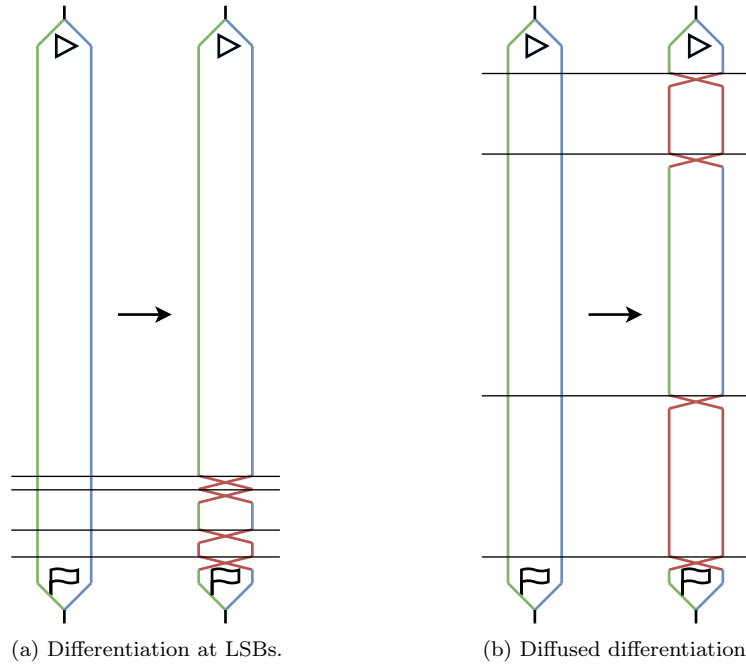


Figure 6.1: Illustration of dependency in PUF response bits.

This characteristic means that the 12 bits that are used to retrieve the PUF responses in the protocol need to be diffused throughout the challenge space resulting in the highest probability of having different data paths. This construction is illustrated in Figure 6.1b. Same holds for the 12 bits that are used to retrieve the random variables in the protocol. Moreover, we found out that by feeding these 12 bits using a Linear Feedback Shift Register (LFSR) instead of a counter, more diffusion is created in the switch blocks.

Table 6.1 summarizes the quality of the PUF responses that have been obtained by challenging three PUF instances using the construction that is used in our proof of

concept. Because of the limited amount of Zedboards available, we implemented these three PUFs on the same System on Chip (SoC) at different locations. This gives us a good approximation of the PUF response quality on distinct SoCs. The metrics are calculated similarly as Machida et al. did in their paper [39]. However, our results have been achieved by challenging three PUF instances with 40-bit challenges multiple times, obtaining multiple 1275-bit responses. More specifically, steadiness is calculated by challenging the PUF a number of  $m = 1275$  times with a set of  $n = 128$  equal challenges. Of the 128 1275-bit responses, the Hamming distances between two arbitrary PUF responses is calculated and averaged. Uniqueness is calculated by challenging two PUF instances a number of  $m = 1275$  times with a set of  $n = 500$  randomly chosen challenges. Of each of these  $\binom{500}{2}$  pairs of 1275-bit responses, the the Hamming distances are calculated and averaged. Finally, randomness is calculated by challenging a PUF instance a number of  $m = 1275$  times with a set of  $n = 500$  randomly chosen challenges. Then, the Hamming weight of these 500 1275-bit results is calculated and averaged.

Table 6.1: Quality of the PUF responses.

Metric	DAPUF	Results
Steadiness [%]	A	5.51
	B	4.03
	C	7.38
Uniqueness [%]	A with B	45.54
	B with C	46.47
	C with A	43.56
Randomness [%]	A	65.56
	B	62.92
	C	70.74

From this table, and Table 3.1 we can see that in the 3-1 Double Arbiter PUF (DAPUF) in our SoC the measure for steadiness is lower (6% versus 12%), which means that our implementation has a higher reproducibility. Moreover, the randomness of our implementation is higher (66% versus 54%), meaning that the probability of a response bit being ‘1’ is higher. To illustrate the effect of the measured quality, we calculate whether enough entropy is left for the Entropy Accumulator (EA) (Definition 3.1) to construct a 128-bit key. Moreover, a recalculation of the fail rate  $p_{\text{fail}}$  will indicate the performance of the authentications.

We recalculate the entropy of the PUF responses  $\rho$  using the binary entropy function  $\mathbf{h}(p)$  from Formula 2.2.1, Section 2.2.2:

$$\begin{aligned}
 \rho &= -\Pr(Y_i = 1) \log_2(\Pr(Y_i = 1)) - \Pr(Y_i = 0) \log_2(\Pr(Y_i = 0)) \\
 &= -0.66 \log_2(0.66) - 0.34 \log_2(0.34) \\
 &= 0.9248
 \end{aligned} \tag{6.1.1}$$

Recall from Section 3.5.1.2 that  $139 \cdot \rho$  bits of entropy is left in the 255 bits of the Bose-Chaudhuri-Hocquenghem (BCH) codeword due to entropy losses through the communicated helper data. Thus,  $139 \cdot 0.9248 = 128$  bits of entropy is left to accumulate the 255 bits BCH codeword, which is just enough to construct a 128-bit key. As a result, no information about the key will be leaked through the helper data.

Next, we recalculate the fail rate  $p_{\text{fail}}$  using Formula 3.5.1, Section 3.5.1.1. When using the implemented  $C_{\text{REP}}(5, 1, 2)$  repetition code, we decrease the bit-error-probability  $p_e = 0.06$  to:

$$\begin{aligned} p_{e,\text{REP}} &= 1 - \sum_{i=0}^2 \binom{5}{i} 0.06^i (1 - 0.06)^{5-i} \\ &= 0.001970 \end{aligned}$$

Using the implemented  $C_{\text{BCH}}(255, 139, 15)$  BCH code on top of that further decreases the bit-error-probability  $p_{e,\text{REP}} = 0.001970$  to a fail rate  $p_{\text{fail}}$  of:

$$\begin{aligned} p_{\text{fail}} &= 1 - \sum_{i=0}^{15} \binom{255}{i} 0.001970^i (1 - 0.001970)^{255-i} \\ &= 8.438 \cdot 10^{-15} \end{aligned}$$

This is a considerable improvement because we aimed for a fail rate of  $p_{\text{fail}} = 10^{-6}$ .

## 6.2 Hardware Performance

This section elaborates on the hardware performance of the proof of concept. The results have been generated by Vivado without the use of Block RAM (BRAM) or Digital Signal Processors (DSPs) and without optimization of the DAPUF design. Synthesis settings are set at `Default` and optimization options are set at `Area`. Furthermore, we allow race conditions to occur due to the nature of the DAPUF.

### 6.2.1 Timing

By using this specific DAPUF, timing results are suboptimal. Because of the long paths the signals have to travel through the DAPUF, the path delay is high. In the worst case scenario, the data path delay is 76.509 ns which means that the maximum frequency of the SoC is 12 MHz. Considering that some Symmetric Key Encryption (SKE) hardware implementations can run in the magnitude of GHz's, the achieved result is suboptimal. However, the authentication phase of the device takes 8205 clock cycles, which on the frequency of 12 MHz takes 0.63 ms. As a result, our proof of concept might not be applicable to devices in the Internet of Things (IoT) but only to conventional use in Radio-Frequency Identification (RFID) systems.

### 6.2.2 Utilization

Table 6.2 summarizes the number of Look-Up Tables (LUTs) per component that have been generated by Vivado without optimization in the implementation such that the DAPUF’s design is kept. In total, our proof of concept utilizes 8,305 LUTs. Similar to the timing results, these utilization results are suboptimal. In this case the registers take a lot of area because of the long variables in the protocol. We explicitly did not replace these registers with BRAM and DSPs because we want to mimic a passive RFID device which normally does not have these kinds of components.

Table 6.2: Number of LUTs per component.

Component	LUTs
Controller	5,464
KETJE	2,630
DAPUF	195
BCH encoder	16
Total	8,305

## 6.3 Software Performance

The computation time of the server-side protocol increases linearly in the number of devices in the database. In our implementation the execution time of the server-side protocol is  $0.05 \cdot n$  seconds. This means that our implementation might not be applicable to devices in the IoT but only to conventional use in RFID systems.

In a real world scenario, the server would be implemented in hardware which could substantially decrease the execution time. We can not say anything about the performance of a hardware implementation, but it is promising for IoT applications. However, in RFID applications this protocol is more suitable because the number of devices is lower and the maximum execution time is often larger.

## 6.4 Benchmark Analysis

We analyze our protocol using the recently proposed benchmark for PUF-based authentication protocols [17]. The benchmark results can be summarized as follows:

**Resources:** Our device uses a PUF, True Random Number Generator (TRNG), Fuzzy Extractor (FE) **Gen** procedure, cryptographic primitive (AEAD-scheme) and a one-time interface.

**PUF type:** Our PUF is a so-called Strong PUF, indicating that the number of Challenge-Response Pairs (CRPs) is at most  $2^l$ , where  $l$  is the number of bits in the challenge.

**#CRPs:** The amount of CRPs for  $n$  authentications is  $n + 1$  because we use a one-time interface for the setup.

**Claims:** The protocol supports server authenticity, device authenticity, device privacy, and memory disclosure.

**#Authentications:** The protocol can support  $d$ -authentications for a perfect privacy use-case and  $\infty$ -authentications without token anonymity.

**Robustness:** Our PUF is noise-robust because of the error correction and modeling-robust because of the EA.

**Authenticity:** Mutual authentication provides for both server and device authenticity.

**Denial-of-Service (DoS) prevention:** There is no internal synchronization which means that our implementation is not susceptible to DoS attacks.

**Scalability:** The execution time of the server per authentication is linear in the amount of devices.

## 6.5 Protocol Comparison

Table 6.3 summarizes the comparison between the proposed protocol (Concealing KETJE Protocol (CKP)) and the protocols by Moriyama et al. [48] and Aysu et al. [3]. The characteristic that all these protocols have in common is that they are all provably secure PUF-based privacy-preserving protocols. However, the paper by Moriyama et al. only provides a theoretical basis for their proposed protocol, instead of also giving a proof of concept. As a result, no sensible answer can be given to the question whether their protocol is practical or not. On the other hand, the protocol by Aysu et al. uses the paper by Moriyama et al. as a basis. As mentioned, this protocol is vulnerable to linear equation analysis of the FE output [3, p. 12]. Their performance results would highly likely be worsened because their FE needs to be redesigned. To this end, most likely they need more PUF response bits to meet the failure rate requirements. As a consequence, their hardware implementation needs more LUTs and might run slower. Moreover, their implementation stores a key in Non-Volatile Memory (NVM) that does not increase

the unpredictability of the communication messages. This overhead is eliminated in our protocol.

Table 6.3: Comparison with previous work.

Reference	Moriyama [48]	Aysu [3]	CKP
Proofs for security and privacy	✓	✓	✓
Implemented parties	✗	device, server	device, server
Security flaws	✗	✓ <sup>1</sup>	✗
Reconfiguration method	✗	modify SW, update microcode	follow generic approach, modify HW and SW
Demonstrator	✗	FPGA, PC	SoC, PC
Security-level	$k$	64-bit/128-bit	128-bit
NVM	PUF challenge & key	PUF challenge & key	PUF challenge
Device FE procedure	<b>Rec</b>	<b>Gen</b>	<b>Gen</b>
PUF type	✗	Weak PUF	Strong PUF
PUF instance	✗	SRAM	DAPUF
Hardware platform	✗	XC5VLX30	XC7Z020
Communication interface	✗	bus, UART	bus, UART
Execution time (clock cycles)	✗	18,597	8,205
Logic cost (w/o PUF)	✗	1,221 LUTs	6,579 LUTs

<sup>1</sup>Due to a vulnerability in their implemented FE.





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CHAPTER  
**SEVEN**

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CONCLUSIONS

## 7.1 Conclusions

In this research we have proposed a novel PUF-based privacy-preserving authentication protocol. We base the authenticity of a device on the Challenge-Response Pairs (CRPs) of the Physically Unclonable Function (PUF). Because the responses on equal challenges are not equal, error-correcting codes have to be applied to recover previous PUF responses. Moreover, because the PUF responses are not uniformly distributed, an Entropy Accumulator (EA) is proposed to ‘compress’ the response into a key. Additionally, confidentiality, authenticity and integrity is supported by an AEAD-scheme. Privacy is preserved by using a challenge updating mechanism in the device’s Non-Volatile Memory (NVM). We have evaluated the protocol both by providing a mathematical proof as well as providing a proof of concept.

We evaluated the security and privacy of the protocol using a mathematical proof. We defined a communication model where we assume full control of the attacker over the communication channel as well as read permissions of the device’s NVM. We defined security with a security experiment in which the attacker can perform unlimited oracle queries to a device and server that have been setup already. The correctness of the protocol is that the server and the device always accept the session if and only if the session has a matching session. We defined privacy using a similar construction. However in the privacy experiment, the attacker communicates with two devices of which one of the devices honestly transfers the communication messages to the attacker. A re-synchronization step is added in the experiment to make sure successful authentications can occur. The experiment can be won if the attacker can distinguish with which device he has been communicating. We prove security and privacy using a game transformation that shows that all communication in the channel appears random to the attacker always.

We evaluated the applicability and practicality of the protocol by presenting a proof of concept. We have seen that there is a dependency in 3-1 Double Arbiter PUF (DAPUF) response bits when the challenges are close to each other. Also, we have seen that the quality of the DAPUF responses differ on our System on Chip (SoC) with regard to the Field Programmable Gate Array (FPGA) used by Machida et al. [40]. However, these differences are small enough for our implementation to be considered secure and thus privacy-preserving with respect to our security considerations. Because of the use of the DAPUF, timing is suboptimal. However, we still achieve an authentication delay of only 0.63 ms which might make our proof of concept applicable to use for the Internet of Things (IoT) and to conventional use-cases with RFID-technology (e.g. in access control and in supply chains). Also, we have seen that because of the large intermediate registers, utilization is suboptimal.

Concluding, we have seen that in comparison to other similar authentication protocols our implementation does not need a key in NVM and is simpler in its design. Although our implementation is slower and consumes more resources, we claim to have an implementation that is both secure and privacy-preserving with respect to our security considerations.

## 7.2 Discussion

Although the protocol is mathematically secure and privacy-preserving, we did not achieve a faster and smaller proof of concept in relation to Aysu et al. [3]. This is mainly due to the implemented PUF which defines the design of the Fuzzy Extractor (FE) and the variable sizes in the protocol. Moreover, the authentication time of the server is linear in the number of devices in the database, which makes the protocol impractical with a substantially large number of devices. As a result, our proof of concept might not be practical for use in the IoT but only for conventional use with Radio-Frequency Identification (RFID) technology. There might be various options to design an instance that is applicable to the IoT. We summarize them as follows.

- We can optimize the KETJE scheme which is now a hardware implementation extracted from the George Mason University (GMU) hardware Application Program Interface (API) for Competition for Authenticated Encryption: Security, Applicability and Robustness (CAESAR). Because we use fixed instances of the KETJE scheme, a lot of optimizations are possible.
- Another option is to optimize the controller of our device, which is now implemented using various processes. Sound cryptographic engineering can substantially optimize the area of the SoC.
- With a Strong PUF that has higher quality, following the generic approach, much smaller protocol variables can be achieved, decreasing the area consumption on the Integrated Circuit (IC).
- A different type of PUF can substantially increase the operating frequency of the IC, which decreases the delay of authentication. One solution can be to use a non-intrinsic PUF that are physically embedded in an IC, for example a coating PUF.
- The server could run in parallel, substantially decreasing the time it takes to authenticate a device.

These options can make the protocol more applicable for various use-cases. However, this is not guaranteed because we rely on a Strong PUF which is still in a young research field. If it turns out that practically a Strong PUF cannot be implemented, our PUF-based protocol is only usable with a bounded amount of authentications with respect to a Weak PUF. However, the protocol can be used without token anonymity and can also easily be adapted to be used with biometric sources like fingerprints and iris-scans.

## 7.3 Future Work

This research mainly focussed on designing a new type of PUF-based privacy-preserving authentication protocol, namely with the use of an AEAD-scheme. Because our proposal provides a protocol design, a mathematical proof and a proof of concept, three aspects can be further examined in future research.

The design of our protocol might be optimized further. Similar to what this research has achieved with relation to the protocol by Aysu et al. [3]. It would be interesting to see whether we overlooked specific aspects that improve the protocol.

Moreover, our proofs are based on the advantage of a probabilistic polynomial time attacker. Many scientists consider this asymptotic approach outdated and propose a concrete or exact approach specifying precise estimates of the computational complexities of adversarial tasks. It would be interesting to see whether our proof can easily be adapted to this approach.

Our proof of concept might be optimized further. Mainly, future research has to be carried out towards Strong PUF implementations, because these form the basis of our protocol. A Strong PUF that has better quality of PUF responses can substantially reduce the consumption of the device.

## 7.4 Closing Remarks

Although we have seen that the Concealing KETJE Protocol (CKP) is mathematically secure, it is questionable whether our proof of concept is secure because of the implemented DAPUF. As mentioned, we discovered that the DAPUF response bits are dependent on the input challenge. This makes the DAPUF responses predictable when the challenges are adaptively chosen in a Machine Learning (ML) attack (Definition 2.13, Section 2.3.4). In a personal communication, Maes, who studied PUFs for his PhD [42], even pointed out: “[...] there are not so much arguably secure implementations of Strong PUFs, it is even debatable whether they can be build at all.”

We close this thesis with a recent quote from Bruce Schneier, a renowned specialist in cryptography, security and privacy. This quote matches the conclusions of this thesis and serves as subject for thought.

“ [...] math has no agency; it can't actually secure anything. For cryptography to work, it needs to be written in software, embedded in a larger software system, managed by an operating system, run on hardware, connected to a network, and configured and operated by users. Each of these steps brings with it difficulties and vulnerabilities. ”

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Bruce Schneier, *Cryptography Is Harder than It Looks*, 2016 [59]

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## ABBREVIATIONS

<b>AcE</b>	Average-case Extractor. [used at p. 25, 27, 101]
<b>AE</b>	Authenticated Encryption. [used at p. 3, 4, 6, 7, 28, 58, 102]
<b>AEAD</b>	Authenticated Encryption with Associated Data. [used at p. 4–7, 28, 29, 33, 39, 40, 44, 48, 49, 56–60, 67, 76, 80, 81, 101]
<b>AES</b>	Advanced Encryption Standard. [used at p. 44]
<b>API</b>	Application Program Interface. [used at p. 67, 81]
<b>ARM</b>	Advanced RISC Machine. [used at p. 32, 62]
<b>ASIC</b>	Application Specific IC. [used at p. 103]
<b>AXI</b>	Advanced Extensible Interface. [used at p. 62, 63]
<b>BCH</b>	Bose-Chaudhuri-Hocquenghem. [used at p. 3, 7, 17–20, 39–44, 61, 63, 64, 67, 74, 75, 95, 97]
<b>BRAM</b>	Block RAM. [used at p. 74, 75]
<b>BSC</b>	Binary Symmetric Channel. [used at p. 16, 17, 31, 97]
<b>CAESAR</b>	Competition for Authenticated Encryption: Security, Applicability and Robustness. [used at p. 4, 44, 67, 81]
<b>CI</b>	Central Interconnect. [used at p. 62]
<b>CKP</b>	Concealing KETJE Protocol. [used at p. 6, 29, 34, 51, 76, 77, 82]
<b>CODEC</b>	coder/decoder. [used at p. 104]
<b>CPA</b>	Chosen-Plaintext Attack. [used at p. 56]
<b>CRP</b>	Challenge-Response Pair. [used at p. 2, 37, 76, 80]
<b>DAPUF</b>	3-1 Double Arbiter PUF. [used at p. 2, 29, 35–39, 61, 63–66, 73–75, 77, 80, 82, 96, 97, 99]
<b>DDR3</b>	Double Data Rate Type Three. [used at p. 103]
<b>DoS</b>	Denial-of-Service. [used at p. 76]
<b>DSP</b>	Digital Signal Processor. [used at p. 74, 75, 103]
<b>EA</b>	Entropy Accumulator. [used at p. 4, 40, 41, 44, 49, 73, 76, 80, 101]
<b>ECRYPT</b>	European Network of Excellence in Cryptology. [used at p. 44]

<b>FE</b>	Fuzzy Extractor. [used at p. 2–4, 6, 7, 24, 26, 27, 29, 30, 33, 38, 41, 49, 55–58, 60, 76, 77, 81, 101, 102]
<b>FF</b>	Flip-Flop. [used at p. 103]
<b>FMC</b>	FPGA Mezzanine Card. [used at p. 104]
<b>FPGA</b>	Field Programmable Gate Array. [used at p. 32, 37, 65, 77, 80, 103]
<b>GMU</b>	George Mason University. [used at p. 67, 81]
<b>HDMI</b>	High-Definition Multimedia Interface. [used at p. 104]
<b>HLS</b>	High Level Synthesis. [used at p. 63]
<b>HW</b>	Hardware. [used at p. 77]
<b>I/O</b>	Input/Output. [used at p. 104]
<b>I2C</b>	Inter-IC Sound. [used at p. 104]
<b>IC</b>	Integrated Circuit. [used at p. 14–16, 33, 81]
<b>ID</b>	identification number. [used at p. 31]
<b>IDE</b>	Integrated Development Environment. [used at p. 63]
<b>IoT</b>	Internet of Things. [used at p. 2, 4, 5, 44, 74, 75, 80, 81]
<b>iSim</b>	ISE Simulator. [used at p. 63]
<b>JTAG</b>	Joint Test Action Group. [used at p. 62, 65, 103]
<b>LFSR</b>	Linear Feedback Shift Register. [used at p. 43, 48, 64, 67, 72]
<b>LSB</b>	Least Significant Bit. [used at p. 72]
<b>LUT</b>	Look-Up Table. [used at p. 65, 75–77, 99, 103]
<b>MAC</b>	Message Authentication Code. [used at p. 28]
<b>MACC</b>	Multiply Accumulator. [used at p. 103]
<b>MitM</b>	Man-in-the-Middle. [used at p. 30, 52, 53, 57, 59]
<b>ML</b>	Machine Learning. [used at p. 13, 14, 35, 72, 82]
<b>MUX</b>	Multiplexer. [used at p. 65]
<b>NAND</b>	negative-AND. [used at p. 14, 65]
<b>NIST</b>	National Institute of Standards and Technology. [used at p. 45]
<b>NSA</b>	National Security Agency. [used at p. 29]
<b>NVM</b>	Non-Volatile Memory. [used at p. 2, 32, 53, 59, 60, 62, 76, 77, 80]
<b>OLED</b>	Organic LED. [used at p. 104]
<b>OTG</b>	On-The-Go. [used at p. 103]
<b>OTP</b>	One-Time Pad. [used at p. 14]
<b>OWASP</b>	Open Web Application Security Project. [used at p. 5]
<b>Pblock</b>	Physical Block. [used at p. 63]
<b>PC</b>	Personal Computer. [used at p. 4, 61, 62, 68, 77]
<b>PHC</b>	Password Hashing Competition. [used at p. 44]
<b>PL</b>	Programmable Logic. [used at p. 32, 62, 65, 104]
<b>Pmod</b>	Peripheral Module. [used at p. 104]

<b>PRF</b>	Pseudo-Random Function. [used at p. 3, 4, 25, 29]
<b>PRNG</b>	Pseudo-Random Number Generator. [used at p. 3]
<b>PS</b>	Processing System. [used at p. 32, 62, 63, 104]
<b>PSK</b>	pre-shared key. [used at p. 2, 3, 29]
<b>PUF</b>	Physically Unclonable Function. [used at p. 2–7, 10–17, 24, 26, 29–44, 52, 55, 57–60, 62, 64, 68, 71–73, 76, 77, 80–82, 95–97, 99, 101, 102]
<b>QSPI</b>	Quad-SPI. [used at p. 103]
<b>RAM</b>	Random-Access Memory. [used at p. 103]
<b>RFE</b>	Reverse FE. [used at p. 3, 29, 38, 39, 44]
<b>RFID</b>	Radio-Frequency Identification. [used at p. 2–5, 44, 74, 75, 80, 81]
<b>ROPUF</b>	Ring Oscillator PUF. [used at p. 13, 15, 97]
<b>SCA</b>	Side-Channel Analysis. [used at p. 68]
<b>SD</b>	Secure Digital. [used at p. 62, 103]
<b>SDK</b>	Software Development Kit. [used at p. 62]
<b>SE</b>	Strong Extractor. [used at p. 4, 24–26, 101]
<b>SKC</b>	Symmetric Key Cryptography. [used at p. 2]
<b>SKE</b>	Symmetric Key Encryption. [used at p. 4, 29, 74]
<b>SoC</b>	System on Chip. [used at p. 32, 62, 63, 73, 74, 77, 80, 81, 103]
<b>SRAM</b>	Static RAM. [used at p. 3, 13, 14, 32, 77]
<b>SS</b>	Secure Sketch. [used at p. 24, 26, 27, 41, 101]
<b>SUV</b>	Secret Unique Value. [used at p. 49]
<b>SW</b>	Software. [used at p. 77]
<b>Tcl</b>	Tool Command Language. [used at p. 65]
<b>TRNG</b>	True Random Number Generator. [used at p. 3, 31, 35, 76]
<b>UART</b>	Universal Asynchronous Receiver/Transmitter. [used at p. 62, 68, 77, 103]
<b>USB</b>	Universal Serial Bus. [used at p. 62, 65, 68, 103]
<b>VGA</b>	Video Graphics Array. [used at p. 104]
<b>VHDL</b>	VHSIC Hardware Description Language. [used at p. 63]
<b>WSW</b>	World-Sized Web. [used at p. 5]
<b>WWW</b>	World Wide Web. [used at p. 5]
<b>XADC</b>	Xilinx Analog to Digital Converter. [used at p. 104]
<b>XOR</b>	exclusive-OR. [used at p. 8, 35, 36, 42–44, 49, 67]





## NOMENCLATURE

<b>Adv</b> <sub><math>\Psi, \mathcal{A}</math></sub> <sup>IND*</sup> ( $k$ )	Privacy advantage of attacker $\mathcal{A}$ on authentication protocol $\Psi$ . [used at p. 54]
<b>Adv</b> <sub><math>\Psi, \mathcal{A}</math></sub> <sup>Sec</sup> ( $k$ )	Security advantage of attacker $\mathcal{A}$ on authentication protocol $\Psi$ , i.e. the probability that <b>Exp</b> <sub><math>\Psi, \mathcal{A}</math></sub> <sup>Sec</sup> ( $k$ ) outputs $B_0 = 1$ on the condition that $I$ of $G$ has no matching session. [used at p. 53, 57]
<b>C</b> <sub>BCH</sub> ( $n, k, t$ )	Binary Bose-Chaudhuri-Hocquenghem (BCH) code of order $m$ , length $n = 2^m - 1$ , distance $d$ and error correcting capability $t = \lfloor \frac{d-1}{2} \rfloor$ , see Definition 2.15. [used at p. 19, 20, 39, 43]
<b>C</b> <sub>REP</sub> ( $n, 1, t$ )	Binary repetition code with length $n$ and error correcting capacity $t = \lfloor \frac{n-1}{2} \rfloor$ , see Definition 2.14. [used at p. 17, 18, 39]
<b>D</b> <sub><math>\mathcal{P}</math></sub> <sup>inter</sup>	Inter-distance for a random challenge in PUF class $\mathcal{P}$ , see Definition 2.9. [used at p. 12]
<b>D</b> <sub><math>\mathcal{P}</math></sub> <sup>intra</sup>	Intra-distance for a random PUF instance and a random challenge in PUF class $\mathcal{P}$ , see Definition 2.7. [used at p. 11, 12]
<b>Exp</b> <sub><math>\Psi, \mathcal{A}</math></sub> <sup>IND*</sup> <sup>-b</sup> ( $k$ )	Indistinguishability privacy experiment of attacker $\mathcal{A}$ on authentication protocol $\Psi$ with security parameter $k$ . [used at p. 54, 97]
<b>Exp</b> <sub><math>\Psi, \mathcal{A}</math></sub> <sup>Sec</sup> ( $k$ )	Security experiment of attacker $\mathcal{A}$ on authentication protocol $\Psi$ with security parameter $k$ . [used at p. 52, 53, 95, 97]
<b>h</b> ( $p$ )	Binary entropy function of binary random variable $Y \leftarrow \{0, 1\}$ with probability $p$ , see Formula 2.2.1. [used at p. 9, 38, 73]
<b>H</b> ( $Y$ )	Shannon entropy of binary string $Y \leftarrow \mathcal{Y}$ , see Definition 2.3. [used at p. 9]
<b><math>\tilde{\mathbf{H}}</math></b> <sub><math>\infty</math></sub> ( $Y$ )	Min-entropy, or Rényi entropy of binary string $Y \leftarrow \mathcal{Y}$ , see Definition 2.4. [used at p. 9]
<b>HD</b> ( $Y, Y'$ )	Hamming distance of binary strings $Y, Y' \leftarrow \mathcal{Y}$ , see Definition 2.1. [used at p. 8, 9, 36, 37]
<b>HW</b> ( $Y$ )	Hamming weight of binary string $Y \leftarrow \mathcal{Y}$ , see Definition 2.2. [used at p. 9, 38]

$\mathcal{P}$	PUF class. [used at p. 10–13, 55, 95, 96]
$\mathcal{P}_{3-1}$	DAPUF class. [used at p. 35–38]
$p_e$	Bit error probability. [used at p. 11, 26, 34–36, 38, 39]
$\Pr(x)$	Probability that $x$ occurs. [used at p. 10]
$\mathbf{puf}$	PUF instance $\mathbf{puf} \in \mathcal{P}$ . [used at p. 11–13, 17, 36–38, 96]
$\mathbf{SD}(A, B)$	Statistical distance between two probability distributions $A$ and $B$ , see Definition 2.5. [used at p. 10]
$X$	PUF challenge. [used at p. 11–13, 17, 35–38, 55]
$Y$	PUF response. [used at p. 11–13, 17, 35–38, 57, 58, 60, 73]

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## HARDWARE SPECIFICATIONS

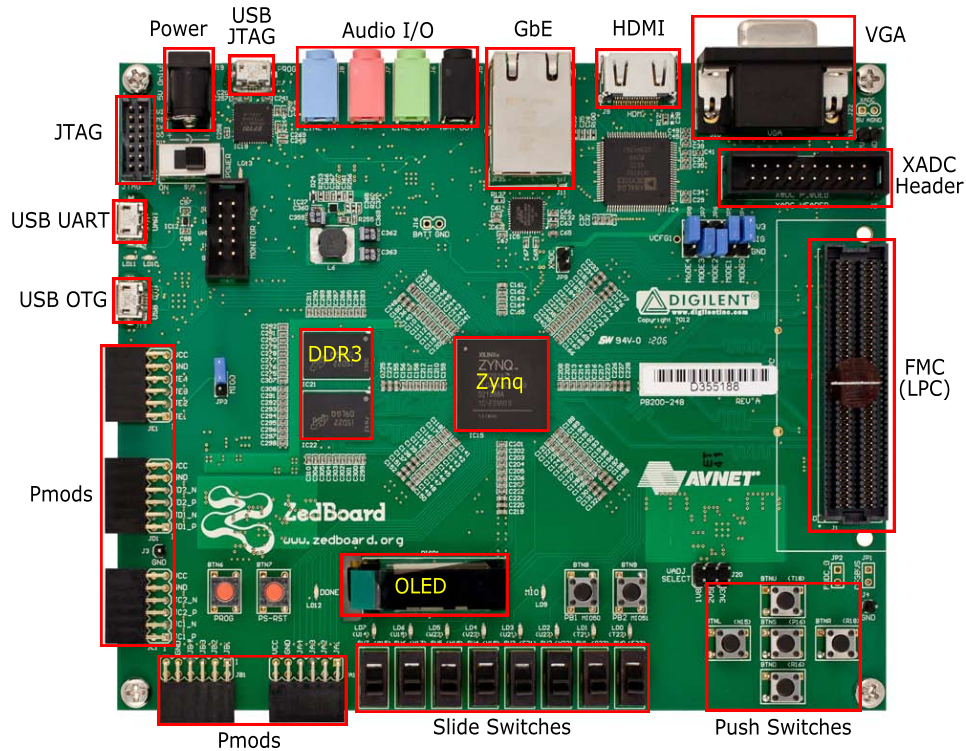
### A.1 Zedboard

This appendix contains the basic specifications of the Zedboard, illustrated in Figure A.1 [2]. The Zedboard includes a Zynq®-7000 by Xilinx Inc. [64].

- Zynq®-7000 28 nm All Programmable SoC XC7Z020-CLG484-1
  - Equivalent to Xilinx 7 Series Programmable Logic Artix®-7 FPGA
  - 85K Programmable Logic Cells (~1.3M Approximate ASIC Gates)
  - 53,200 LUTs
  - 106,400 Flip-Flops (FFs)
  - 560 KB Extensible Block Random-Access Memory (RAM) (140x36 Kb Blocks)
  - 220 Programmable Digital Signal Processor (DSP) Slices (18x25 Multiply Accumulators (MACCs))
- Memory
  - 512 MB Double Data Rate Type Three (DDR3)
  - 256 Mb Quad-SPI (QSPI) Flash
  - 4 GB SD-card
- Onboard Universal Serial Bus (USB)-Joint Test Action Group (JTAG) Programming
- 10/100/1000 Ethernet
- USB On-The-Go (OTG) 2.0 and USB-Universal Asynchronous Receiver/Transmitter (UART)

## Appendix A. Hardware specifications

- Processing System (PS) & Programmable Logic (PL) Input/Output (I/O) expansion (FPGA Mezzanine Card (FMC), Peripheral Module (Pmod) Compatible, Xilinx Analog to Digital Converter (XADC))
- Multiple displays (1080p High-Definition Multimedia Interface (HDMI), 8-bit Video Graphics Array (VGA), 128 x 32 Organic LED (OLED))
- Inter-IC Sound (I2C) Audio coder/decoder (CODEC)



\* SD card cage and QSPI Flash reside on backside of board

Figure A.1: Functional Overlay of the Zedboard by Avnet Inc. [2].

## GALOIS FIELD TABLES

**B.1 GF(2<sup>4</sup>) generated by  $p(x) = x^4 + x + 1$** 

Table B.1: Galois Field table **GF(2<sup>4</sup>)** as generated by the primitive polynomial  $p(x) = x^4 + x + 1$ . REP denotes ‘representation’.

Power REP	Polynomial REP				Binary REP
0					{0, 0, 0, 0}
1					{0, 0, 0, 1}
$\alpha$			$\alpha$		{0, 0, 1, 0}
$\alpha^2$		$\alpha^2$			{0, 1, 0, 0}
$\alpha^3$	$\alpha^3$				{1, 0, 0, 0}
$\alpha^4$			$\alpha$	+ 1	{0, 0, 1, 1}
$\alpha^5$		$\alpha^2$	+ $\alpha$		{0, 1, 1, 0}
$\alpha^6$	$\alpha^3$	+ $\alpha^2$			{1, 1, 0, 0}
$\alpha^7$	$\alpha^3$		+ $\alpha$	+ 1	{1, 0, 1, 1}
$\alpha^8$		$\alpha^2$		+ 1	{0, 1, 0, 1}
$\alpha^9$	$\alpha^3$		+ $\alpha$		{1, 0, 1, 0}
$\alpha^{10}$		$\alpha^2$	+ $\alpha$	+ 1	{0, 1, 1, 1}
$\alpha^{11}$	$\alpha^3$	+ $\alpha^2$	+ $\alpha$		{1, 1, 1, 0}
$\alpha^{12}$	$\alpha^3$	+ $\alpha^2$	+ $\alpha$	+ 1	{1, 1, 1, 1}
$\alpha^{13}$	$\alpha^3$	+ $\alpha^2$		+ 1	{1, 1, 0, 1}
$\alpha^{14}$	$\alpha^3$			+ 1	{1, 0, 0, 1}

## B.2 GF(2<sup>8</sup>) generated by $p(x) = x^4 + x^3 + x^2 + 1$

Table B.2: Galois Field table **GF(2<sup>8</sup>)** as generated by the primitive polynomial  $p(x) = x^4 + x^3 + x^2 + 1$ . REP denotes ‘representation’.

Power REP	Polynomial REP	Binary REP
0	0	{0, 0, 0, 0, 0, 0, 0, 0}
1	1	{0, 0, 0, 0, 0, 0, 0, 1}
$\alpha$	$\alpha$	{0, 0, 0, 0, 0, 0, 1, 0}
$\alpha^2$	$\alpha^2$	{0, 0, 0, 0, 0, 1, 0, 0}
$\alpha^3$	$\alpha^3$	{0, 0, 0, 0, 1, 0, 0, 0}
$\alpha^4$	$\alpha^4$	{0, 0, 0, 1, 0, 0, 0, 0}
$\alpha^5$	$\alpha^5$	{0, 0, 1, 0, 0, 0, 0, 0}
$\alpha^6$	$\alpha^6$	{0, 1, 0, 0, 0, 0, 0, 0}
$\alpha^7$	$\alpha^7$	{1, 0, 0, 0, 0, 0, 0, 0}
$\alpha^8$	$\alpha^4 + \alpha^3 + \alpha^2 + 1$	{0, 0, 0, 1, 1, 1, 0, 1}
$\alpha^9$	$\alpha^5 + \alpha^4 + \alpha^3 + \alpha$	{0, 0, 1, 1, 1, 0, 1, 0}
$\alpha^{10}$	$\alpha^6 + \alpha^5 + \alpha^4 + \alpha^2$	{0, 1, 1, 1, 0, 1, 0, 0}
$\vdots$	$\vdots$	$\vdots$
$\alpha^{132}$	$\alpha^7 + \alpha^5 + \alpha^4 + \alpha^3$	{1, 0, 1, 1, 1, 0, 0, 0}
$\alpha^{133}$	$\alpha^6 + \alpha^5 + \alpha^3 + \alpha^2 + 1$	{0, 1, 1, 0, 1, 1, 0, 1}
$\alpha^{134}$	$\alpha^7 + \alpha^6 + \alpha^4 + \alpha^3 + \alpha$	{1, 1, 0, 1, 1, 0, 1, 0}
$\alpha^{135}$	$\alpha^7 + \alpha^5 + \alpha^3 + 1$	{1, 0, 1, 0, 1, 0, 0, 1}
$\alpha^{136}$	$\alpha^6 + \alpha^3 + \alpha^2 + \alpha + 1$	{0, 1, 0, 0, 1, 1, 1, 1}
$\alpha^{137}$	$\alpha^7 + \alpha^4 + \alpha^3 + \alpha^2 + \alpha + 1$	{1, 0, 0, 1, 1, 1, 1, 0}
$\alpha^{138}$	$\alpha^5 + \alpha^2 + \alpha + 1$	{0, 0, 1, 0, 0, 0, 0, 1}
$\alpha^{139}$	$\alpha^6 + \alpha + 1$	{0, 1, 0, 0, 0, 0, 1, 0}
$\alpha^{140}$	$\alpha^7 + \alpha^2 + 1$	{1, 0, 0, 0, 0, 1, 0, 0}
$\alpha^{141}$	$\alpha^4 + \alpha^2 + 1$	{0, 0, 0, 1, 0, 1, 0, 1}
$\alpha^{142}$	$\alpha^5 + \alpha^3 + \alpha$	{0, 0, 1, 0, 1, 0, 1, 0}
$\alpha^{143}$	$\alpha^6 + \alpha^4 + \alpha^2$	{0, 1, 0, 1, 0, 1, 0, 0}
$\alpha^{144}$	$\alpha^7 + \alpha^5 + \alpha^3$	{1, 0, 1, 0, 1, 0, 0, 0}
$\vdots$	$\vdots$	$\vdots$
$\alpha^{243}$	$\alpha^6 + \alpha^5 + \alpha^4 + \alpha^3 + \alpha^2 + 1$	{0, 1, 1, 1, 1, 1, 0, 1}
$\alpha^{244}$	$\alpha^7 + \alpha^6 + \alpha^5 + \alpha^4 + \alpha^3 + \alpha$	{1, 1, 1, 1, 1, 0, 1, 0}
$\alpha^{245}$	$\alpha^7 + \alpha^6 + \alpha^5 + \alpha^3 + 1$	{1, 1, 1, 0, 1, 0, 0, 1}
$\alpha^{246}$	$\alpha^7 + \alpha^6 + \alpha^3 + \alpha^2 + \alpha + 1$	{1, 1, 0, 0, 1, 1, 1, 1}
$\alpha^{247}$	$\alpha^7 + \alpha^2 + \alpha + 1$	{1, 0, 0, 0, 0, 0, 1, 1}
$\alpha^{248}$	$\alpha^4 + \alpha^3 + \alpha + 1$	{0, 0, 0, 1, 1, 0, 1, 1}
$\alpha^{249}$	$\alpha^5 + \alpha^4 + \alpha^2 + \alpha$	{0, 0, 1, 1, 0, 1, 1, 0}
$\alpha^{250}$	$\alpha^6 + \alpha^5 + \alpha^3 + \alpha^2$	{0, 1, 1, 0, 1, 1, 0, 0}
$\alpha^{251}$	$\alpha^7 + \alpha^6 + \alpha^4 + \alpha^3$	{1, 1, 0, 1, 1, 0, 0, 0}
$\alpha^{252}$	$\alpha^7 + \alpha^5 + \alpha^3 + \alpha^2 + 1$	{1, 0, 1, 0, 1, 1, 0, 1}
$\alpha^{253}$	$\alpha^6 + \alpha^2 + \alpha + 1$	{0, 1, 0, 0, 0, 1, 1, 1}
$\alpha^{254}$	$\alpha^7 + \alpha^3 + \alpha^2 + \alpha$	{1, 0, 0, 0, 1, 1, 1, 0}

## SOURCE CODE LISTINGS

This appendix lists the most relevant source code produced in this research. For clarity, similar lines of code have been omitted which is indicated by comments.

## C.1 Software

### C.1.1 Server

```
1 #*****#
2 # Author: J.G. (Gerben) Geltink # g.geltink@gmail.com
3 # Module: Server Side Protocol # main.py
4 # This module describes the server side protocol of the device DAPUF in the Concealing Ketje
5 # Protocol as presented by the guiding MSc thesis: Geltink, J. G. (2016). "Concealing Ketje: A
6 # Lightweight PUF-based Privacy Preserving Authentication Protocol".
7 #
8 # Copyright (c) 2016 J.G. Geltink under MIT license
9 #*****#
10 import commands
11 import timeit
12 import serial
13 import random
14 import struct
15
16 ser = 0
17
18 def init_serial():
19     global ser #Must be declared in Each Function
20     ser = serial.Serial()
21     ser.baudrate = 115200
22     ser.port = '/dev/ttyACM0' #If Using Linux
23     ser.timeout = 10
24     ser.open() #Opens SerialPort
25
26
27 def xor_bitarray(a, b):
28     return map(lambda x: x[0] ^ x[1], zip(a, b))
29
30 def int_to_bitlist(n, length):
31     return [n >> i & 1 for i in range(length-1,-1,-1)]
32
33 def bitlist_to_int(bitlist):
34     out = 0
35     for bit in bitlist:
36         out = (out << 1) | bit
37     return out
38
39
40
```

## Appendix C. Source Code Listings

```

41 def int_to_hexstring(i, n):
42     string = hex(i);
43     if string[len(string)-1] == "L":
44         return string[2:len(string)-1].zfill(2*n)
45     else:
46         return string[2:].zfill(2*n)
47
48 def int_to_bytelist(n, length):
49     return [ n >> (8*i) & 0xff for i in range(length-1,-1,-1)]
50
51 def bch_dec(a_prime, hd):
52     '''Code derived from Robert Morelos-Zaragoza: Encoder/decoder for binary BCH codes in C (Version 3.1, 1997)
53     using BCH(255,139,15)
54     NOTE: not in constant time!'''
55     t = 15
56     length = 255
57     n = 255
58     cw_prime = xor_bitarray(a_prime, hd)
59     cw = cw_prime[:]
60     # print 'cw_prime\t', cw_prime
61     # index->polynomial form: alpha_to[] contains j=alpha^i;
62     alpha_to = [1, 2, 4, 8, 16, 32, 64, 128, 113, 226, 181, 27, 54, 108, 216, 193, 243, 151, 95, 190, 13, 26, 52,
104, 208, 209, 211, 215, 223, 207, 239, 175, 47, 94, 188, 9, 18, 36, 72, 144, 81, 162, 53, 106, 212,
217, 195, 247, 159, 79, 158, 77, 154, 69, 138, 101, 202, 229, 187, 7, 14, 28, 56, 112, 224, 177, 19,
38, 76, 152, 65, 130, 117, 234, 165, 59, 118, 236, 169, 35, 70, 140, 105, 210, 213, 219, 199, 255, 143,
111, 222, 205, 235, 167, 63, 126, 252, 137, 99, 198, 253, 139, 103, 206, 237, 171, 39, 78, 156, 73,
146, 85, 170, 37, 74, 148, 89, 178, 21, 42, 84, 168, 33, 66, 132, 121, 242, 149, 91, 182, 29, 58, 116,
232, 161, 51, 102, 204, 233, 163, 55, 110, 220, 201, 227, 183, 31, 62, 124, 248, 129, 115, 230, 189,
11, 22, 44, 88, 176, 17, 34, 68, 136, 97, 194, 245, 155, 71, 142, 109, 218, 197, 251, 135, 127, 254,
141, 107, 214, 221, 203, 231, 191, 15, 30, 60, 120, 240, 145, 83, 166, 61, 122, 244, 153, 67, 134, 125,
250, 133, 123, 246, 157, 75, 150, 93, 186, 5, 10, 20, 40, 80, 160, 49, 98, 196, 249, 131, 119, 238,
173, 43, 86, 172, 41, 82, 164, 57, 114, 228, 185, 3, 6, 12, 24, 48, 96, 192, 241, 147, 87, 174, 45, 90,
180, 25, 50, 100, 200, 225, 179, 23, 46, 92, 184, 0]
63     # polynomial form -> index form: index_of[j=alpha^i] = i
64     index_of = [-1, 0, 1, 231, 2, 207, 232, 59, 3, 35, 208, 154, 233, 20, 60, 183, 4, 159, 36, 66, 209, 118, 155,
251, 234, 245, 21, 11, 61, 130, 184, 146, 5, 122, 160, 79, 37, 113, 67, 106, 210, 224, 119, 221, 156,
242, 252, 32, 235, 213, 246, 135, 22, 42, 12, 140, 62, 227, 131, 75, 185, 191, 147, 94, 6, 70, 123,
195, 161, 53, 80, 167, 38, 109, 114, 203, 68, 51, 107, 49, 211, 40, 225, 189, 120, 111, 222, 240, 157,
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199, 196, 173, 162, 97, 54, 101, 81, 176, 168, 88, 39, 188, 110, 239, 115, 127, 204, 17, 69, 194, 52,
166, 108, 202, 50, 48, 212, 134, 41, 139, 226, 74, 190, 93, 121, 78, 112, 105, 223, 220, 241, 31, 158,
65, 117, 250, 244, 10, 129, 145, 254, 230, 206, 58, 34, 153, 19, 182, 237, 15, 164, 46, 215, 171, 99,
86, 248, 143, 56, 180, 137, 91, 103, 29, 24, 25, 83, 26, 44, 84, 178, 27, 14, 45, 170, 85, 142, 179,
90, 28, 64, 249, 9, 144, 229, 57, 152, 181, 133, 138, 73, 92, 77, 104, 219, 30, 187, 238, 126, 16, 196,
165, 201, 47, 149, 216, 198, 172, 96, 100, 175, 87]
65     t2 = 2 * t; #2* error correcting capability
66     # first form the syndromes
67     syn_error = False
68     s = [0 for i in range(t2+1)]
69     for i in range(L, t2+1):
70         for j in range(length):
71             if (cw_prime[j] != 0):
72                 s[i] ^= alpha_to[(i * j) % n]
73         if (s[i] != 0):
74             syn_error = True
75         s[i] = index_of[s[i]]
76     # print 's\t', s[1:]
77     # print 'syn_error\t', syn_error
78     if syn_error:
79         # /* initialise table entries */
80         d = [0 for i in range(t2 + 2)]
81         elp = [[0 for i in range(t2 + 2)] for j in range(t2 + 2)]
82         l = [0 for i in range(t2 + 2)]
83         u_lu = [0 for i in range(t2 + 2)]
84         d[0] = 0; #/* index form */
85         d[1] = s[1]; #/* index form */
86         elp[0][0] = 0; #/* index form */
87         elp[1][0] = 1; #/* polynomial form */
88         for i in range(1,t2):
89             elp[0][i] = -1; #/* index form */
90             elp[1][i] = 0; #/* polynomial form */
91         l[0] = 0;
92         l[1] = 0;
93         u_lu[0] = -1;
94         u_lu[1] = 0;
95         u = 0; # 0 -> t2+1
96         while True:
97             u += 1
98             if (d[u] == -1):
99                 l[u + 1] = l[u]
100                 for i in range(l[u] + 1):
101                     elp[u + 1][i] = elp[u][i]
102                     elp[u][i] = index_of[elp[u][i]]
103             else:
104                 # search for words with greatest u_lu[q] for
105                 # which d[q]!=0
106                 q = u - 1
107                 while ((d[q] == -1) and (q > 0)):
108                     q -= 1
109                 # have found first non-zero d[q]
110                 if (q > 0):
111                     j = q
112                     while True:
113                         j -= 1
114                         if ((d[j] != -1) and (u_lu[q] < u_lu[j])):
115                             q = j;

```

```

116         if not (j > 0):
117             break
118         # have now found q such that d[u]!=0 and u_lu[q] is maximum
119         # store degree of new elp polynomial
120         if (l[u] > l[q] + u - q):
121             l[u + 1] = l[u]
122         else:
123             l[u + 1] = l[q] + u - q
124         # form new elp(x)
125         for i in range(t2):
126             elp[u + 1][i] = 0
127         for i in range(l[q] + 1):
128             if (elp[q][i] != -1):
129                 elp[u + 1][i + u - q] = alpha_to[(d[u] + n - d[q] + elp[q][i]) % n]
130         for i in range(l[u] + 1):
131             elp[u + 1][i] ^= elp[u][i]
132             elp[u][i] = index_of[elp[u][i]]
133         u_lu[u + 1] = u - l[u + 1]
134         # form (u+1)th discrepancy
135         if (u < t2):
136             # no discrepancy computed on last iteration
137             if (s[u + 1] != -1):
138                 d[u + 1] = alpha_to[s[u + 1]]
139             else:
140                 d[u + 1] = 0
141             for i in range(1, l[u + 1] + 1):
142                 if ((s[u + 1 - i] != -1) and (elp[u + 1][i] != 0)):
143                     d[u + 1] ^= alpha_to[(s[u + 1 - i] + index_of[elp[u + 1][i]]) % n]
144             # put d[u+1] into index form
145             d[u + 1] = index_of[d[u + 1]]
146         if not ((u < t2) and (l[u + 1] <= t)):
147             break
148         u += 1
149         if (l[u] <= t): # Can correct errors
150             # put elp into index form
151             for i in range(l[u] + 1):
152                 elp[u][i] = index_of[elp[u][i]]
153             sigma = []
154             for i in range(l[u] + 1):
155                 sigma += [elp[u][i]]
156             # print 'sigma(x) =\t', sigma
157             # Chien search: find roots of the error location polynomial
158             reg = [0 for x in range(l[u] + 1)]
159             root = [0 for x in range(l[u])]
160             loc = [0 for x in range(l[u])]
161             for i in range(1, l[u] + 1):
162                 reg[i] = elp[u][i]
163             count = 0
164             for i in range(1, n + 1):
165                 q = 1
166                 for j in range(1, l[u] + 1):
167                     if (reg[j] != -1):
168                         reg[j] = (reg[j] + j) % n
169                         q ^= alpha_to[reg[j]]
170                 if (q == 0): # store root and error location number indices
171                     root[count] = i
172                     loc[count] = n - i
173                     count += 1
174             if (count == l[u]):
175                 # print 'Roots:\t', loc
176                 print "\t#errors corrected BCH\t", str(len(loc))
177                 for i in range(l[u]):
178                     cw[loc[i]] ^= 1
179             else:
180                 l == 1
181                 print '\tBCH incomplete decoding: errors detected'
182             # print 'cw\t', cw
183             return xor_bitarray(cw, hd)
184
185 def rep_decode(hd_rep, y_1):
186     errors = 0
187     e = [7, 11, 13, 14, 15] #faulty syndromes
188     r_p = 0
189     ry_pb = 0
190     for i in range(255):
191         hd = (hd_rep >> 4 * i) & 0b1111
192         y = (y_1 >> 5 * i) & 0b11111
193         y_pb = (y_1 >> 5 * i) & 0b1
194
195         if y_pb == 1: #compute syndromes
196             s = 0b1111 ^ (y >> 1) ^ hd
197         else:
198             s = 0 ^ (y >> 1) ^ hd
199
200         if s in e:
201             r_pb = y_pb ^ 1
202             errors += 1
203         else:
204             r_pb = y_pb
205
206         r_p += r_pb << i #LSB on right
207
208     print "\t#errors corrected REP\t", str(errors)
209     return r_p
210
211
212 x = random.randint(1, 2 ** 64)

```

## Appendix C. Source Code Listings

```
213 x_list = int_to_bytelist(x, 16)
214 init_serial()
215 ser.write([0x90])
216 ser.write(x_list[:4])
217 ser.write(x_list[4:8])
218 y_l = ser.readline()[0:-1]
219 print "device set up:\t", y_l[-64:], "<Y> (showing rightmost 32 bytes)"
220 print "-----\n"
221 ser.close()
222
223 while(1):
224
225     n1 = random.randint(1,2**128)
226
227     init_serial()
228
229     n1_list = int_to_bytelist(n1, 16)
230     ser.write([0x90])
231     ser.write(n1_list[:4])
232     ser.write(n1_list[4:8])
233     ser.write(n1_list[8:12])
234     ser.write(n1_list[12:])
235
236     print "challenge sent:\t\t", int_to_hexstring(n1,16), "<N1>"
237
238     hd_rep = ser.readline()[0:-1]
239     hd_bch = ser.readline()[1:-1]
240     c = ser.readline()[1:-1]
241     n2 = ser.readline()[1:-1]
242     t = ser.readline()[1:-1]
243
244     ser.close()
245
246     print "responses received:\t", t, "<HD, N2, C1, T1> (only showing T1)"
247
248     hd_rep = int(hd_rep, 16)
249     y_l = int(y_l, 16)
250     hd_bch = int(hd_bch,16)
251     hd = int_to_bitlist(hd_bch, 255)
252     c = [c[i:i+8] for i in range(0,len(c),8)]
253     c.reverse()
254     c = "".join(c) # c is feeded in reverse
255     clen = 160
256     klen = 16
257     nlen= 16
258     adlen = 16
259     tlen = 16
260     auth = False
261
262     start = timeit.default_timer()
263     r_p = rep_decode(hd_rep, y_l)
264     a_prime = int_to_bitlist(r_p, 255)
265     r_pp = bch_dec(a_prime, hd)
266     r_pp = bitlist_to_int(r_pp)
267     r_pp_str = int_to_hexstring(r_pp, 32)
268
269     key = r_pp_str[:32] # left part of r_pp
270     nonce = n2
271     ad = r_pp_str[32:] # right part of r_pp
272     ad = ad[24:] + ad[16:24] + ad[8:16] + ad[:8] #ad is feeded in reverse!
273     challenge = r"./Ketje_enc " + key + " " + str(klen) + " " + nonce + " " + str(nlen) + " " + ad + " " + str(
        adlen) + c + str(clen) + t + str(tlen)
274     response = commands.getstatusoutput(challenge)
275     dev_key = response[1].split()[0]
276     # print "dev_key = [" + dev_key + "]"
277
278     nonce = int_to_hexstring(n1,16)
279     ad = n2
280     ad = ad[24:] + ad[16:24] + ad[8:16] + ad[:8] #ad is feeded in reverse!
281
282     challenge = r"./Ketje_dec " + dev_key + " " + str(klen) + " " + nonce + " " + str(nlen) + " " + ad + " " +
        str(adlen) + " " + c + " " + str(clen) + " " + t + " " + str(tlen)
283     response = commands.getstatusoutput(challenge)
284     y_2 = response[1].split()[0]
285     y_2 = [y_2[i:i+8] for i in range(0,len(y_2),8)]
286     y_2.reverse()
287     y_2 = "".join(y_2) # y_2 is received in reverse
288
289     if (y_2 == "".zfill(320)):
290         t2 = random.randint(1,2**128)
291         y_l = int_to_hexstring(y_l,160)
292     else:
293         auth = True
294         y_l = y_2
295         nonce = int_to_hexstring(n1,16)
296         ad = int_to_hexstring(int(n2, 16) + 2**127, 16)
297         ad = ad[24:] + ad[16:24] + ad[8:16] + ad[:8] #ad is feeded in reverse!
298         challenge = r"./Ketje_enc " + dev_key + " " + str(klen) + " " + nonce + " " + str(nlen) + " " + ad + " " +
            str(adlen) + c + str(clen) + t + str(tlen)
299         response = commands.getstatusoutput(challenge)
300         t2 = response[1].split()[0]
301         t2 = int(t2,16)
302     end = timeit.default_timer()
303
304     if auth:
305         print "\033[92mSUCCESSFULL AUTHENTICATION\033[0m"
```







```

52 END COMPONENT;
53 COMPONENT ketjeSr --component received from Guido Bertoni
54 PORT (
55     clk          : IN STD_LOGIC;
56     rst          : IN STD_LOGIC;
57     npub        : IN STD_LOGIC_VECTOR(127 DOWNTO 0);
58     nsec        : IN STD_LOGIC_VECTOR(127 DOWNTO 0);
59     key         : IN STD_LOGIC_VECTOR(127 DOWNTO 0);
60     rdkey       : IN STD_LOGIC_VECTOR(127 DOWNTO 0);
61     bdi         : IN STD_LOGIC_VECTOR(31 DOWNTO 0);
62     exp_tag     : IN STD_LOGIC_VECTOR(127 DOWNTO 0);
63     len_a      : IN STD_LOGIC_VECTOR(63 DOWNTO 0);
64     len_d      : IN STD_LOGIC_VECTOR(63 DOWNTO 0);
65     key_ready   : IN STD_LOGIC;
66     key_updated : OUT STD_LOGIC;
67     key_needs_update : IN STD_LOGIC;
68     rdkey_ready : IN STD_LOGIC;
69     rdkey_read  : OUT STD_LOGIC;
70     npub_ready  : IN STD_LOGIC;
71     npub_read   : OUT STD_LOGIC;
72     nsec_ready  : IN STD_LOGIC;
73     nsec_read   : OUT STD_LOGIC;
74     bdi_ready  : IN STD_LOGIC;
75     bdi_proc   : IN STD_LOGIC;
76     bdi_ad     : IN STD_LOGIC;
77     bdi_nsec   : IN STD_LOGIC;
78     bdi_pad    : IN STD_LOGIC;
79     bdi_decrypt : IN STD_LOGIC;
80     bdi_eot    : IN STD_LOGIC;
81     bdi_eoi    : IN STD_LOGIC;
82     bdi_read   : OUT STD_LOGIC;
83     bdi_size   : IN STD_LOGIC_VECTOR(1 DOWNTO 0);
84     bdi_valid_bytes : IN STD_LOGIC_VECTOR(3 DOWNTO 0);
85     bdi_pad_loc : IN STD_LOGIC_VECTOR(3 DOWNTO 0);
86     bdi_nodata : IN STD_LOGIC;
87     exp_tag_ready : IN STD_LOGIC;
88     bdo_ready  : IN STD_LOGIC;
89     bdo_write  : OUT STD_LOGIC;
90     bdo       : OUT STD_LOGIC_VECTOR(31 DOWNTO 0);
91     bdo_size  : OUT STD_LOGIC_VECTOR(2 DOWNTO 0);
92     bdo_nsec  : OUT STD_LOGIC;
93     tag_ready : IN STD_LOGIC;
94     tag_write : OUT STD_LOGIC;
95     tag       : OUT STD_LOGIC_VECTOR(127 DOWNTO 0);
96     msg_auth_done : OUT STD_LOGIC;
97     msg_auth_valid : OUT std_logic
98 );
99 END COMPONENT;
100
101 --SIGNAL DECLARATIONS
102 SIGNAL esig_IN : STD_LOGIC := '0'; --PUF enable SIGNAL
103 SIGNAL res : STD_LOGIC := '0';
104 SIGNAL challenge : STD_LOGIC_VECTOR(63 DOWNTO 0);
105 SIGNAL seed1 : STD_LOGIC_VECTOR(11 DOWNTO 0) := x"001"; --TODO: into NVM
106 SIGNAL chall : STD_LOGIC_VECTOR(39 DOWNTO 0) := (OTHERS => '0'); --TODO: into NVM
107 SIGNAL setup : STD_LOGIC := '0';
108 SIGNAL seed2 : STD_LOGIC_VECTOR(11 DOWNTO 0) := (OTHERS => '0');
109 SIGNAL chal2 : STD_LOGIC_VECTOR(39 DOWNTO 0) := (OTHERS => '0');
110 SIGNAL pufresp : STD_LOGIC_VECTOR(1279 DOWNTO 0) := (OTHERS => '0');
111 SIGNAL c1 : STD_LOGIC_VECTOR(1279 DOWNTO 0) := (OTHERS => '0');
112 SIGNAL pdi : STD_LOGIC_VECTOR(127 DOWNTO 0) := (OTHERS => '0');
113 SIGNAL nce2 : STD_LOGIC_VECTOR(126 DOWNTO 0) := (OTHERS => '0');
114 SIGNAL t1 : STD_LOGIC_VECTOR(127 DOWNTO 0) := (OTHERS => '0');
115 SIGNAL t2 : STD_LOGIC_VECTOR(127 DOWNTO 0) := (OTHERS => '0');
116 SIGNAL bchrnd : STD_LOGIC_VECTOR(138 DOWNTO 0) := (OTHERS => '0');
117 SIGNAL rep_res : STD_LOGIC_VECTOR(254 DOWNTO 0) := (OTHERS => '0');
118 SIGNAL hd_rep : STD_LOGIC_VECTOR(1019 DOWNTO 0) := (OTHERS => '0');
119 SIGNAL bch_cw : STD_LOGIC_VECTOR(115 DOWNTO 0) := (OTHERS => '0');
120 SIGNAL dev_key : STD_LOGIC_VECTOR(127 DOWNTO 0) := (OTHERS => '0');
121 SIGNAL ctrl_puf_resp : STD_LOGIC := '0';
122 SIGNAL ctrl_rst_puf : STD_LOGIC := '0';
123 SIGNAL ctrl_rst_rep : STD_LOGIC := '0';
124 SIGNAL ctrl_index : STD_LOGIC_VECTOR(11 DOWNTO 0) := (OTHERS => '0');
125 SIGNAL ctrl_index2 : STD_LOGIC_VECTOR(7 DOWNTO 0) := (OTHERS => '0');
126 SIGNAL ctrl_cnt : STD_LOGIC_VECTOR(7 DOWNTO 0) := (OTHERS => '0');
127 SIGNAL ctrl_rst_bch : STD_LOGIC := '0';
128 SIGNAL ctrl_rst_ketje : STD_LOGIC := '0';
129 SIGNAL rst_bch : STD_LOGIC := '0';
130 SIGNAL din_bch : STD_LOGIC := '0';
131 SIGNAL dout_bch : STD_LOGIC;
132 SIGNAL ctrl_rst_lfsr : STD_LOGIC := '0';
133 SIGNAL ctrl_lfsr : STD_LOGIC := '0';
134 SIGNAL ctrl_comp_t2 : STD_LOGIC := '0';
135 SIGNAL ctrl_checkandupd : STD_LOGIC := '0';
136 SIGNAL lfsr : STD_LOGIC_VECTOR(11 DOWNTO 0);
137 SIGNAL ctrl_ketje_mode : STD_LOGIC_VECTOR(1 DOWNTO 0) := (OTHERS => '0');
138 SIGNAL npub_reg : STD_LOGIC_VECTOR(127 DOWNTO 0) := (OTHERS => '0');
139 SIGNAL key_reg : STD_LOGIC_VECTOR(127 DOWNTO 0) := (OTHERS => '0');
140 SIGNAL ad_reg : STD_LOGIC_VECTOR(127 DOWNTO 0) := (OTHERS => '0');
141 SIGNAL rst_ketje : STD_LOGIC := '0';
142 SIGNAL npub : STD_LOGIC_VECTOR(127 DOWNTO 0) := (OTHERS => '0');
143 SIGNAL key : STD_LOGIC_VECTOR(127 DOWNTO 0) := (OTHERS => '0');
144 SIGNAL bdi : STD_LOGIC_VECTOR(31 DOWNTO 0) := (OTHERS => '0');
145 SIGNAL key_ready : STD_LOGIC := '0';
146 SIGNAL key_needs_update : STD_LOGIC := '0';
147 SIGNAL npub_ready : STD_LOGIC := '0';
148 SIGNAL bdi_ready : STD_LOGIC := '0';

```

## Appendix C. Source Code Listings

```
149 SIGNAL bdi_ad      : STD_LOGIC := '0';
150 SIGNAL bdi_nsec    : STD_LOGIC := '0';
151 SIGNAL bdi_eot     : STD_LOGIC := '0';
152 SIGNAL bdi_eoi     : STD_LOGIC := '0';
153 SIGNAL bdo         : STD_LOGIC_VECTOR(31 DOWNTO 0);
154 SIGNAL tag_write   : STD_LOGIC;
155 SIGNAL tag         : STD_LOGIC_VECTOR(127 DOWNTO 0);
156
157 --UNUSED SIGNAL DECLARATIONS (will be synthesized out)
158 SIGNAL rst_puf     : STD_LOGIC := '0'; --PUF reset signal
159 --OMITTED: vdin_bch_unused, nsec, rdkey, exp_tag, len_a, len_d, rdkey_ready, nsec_ready, bdi_proc, bdi_pad,
        bdi_decrypt, bdi_size, bdi_valid_bytes, bdi_pad_loc, bdi_nodata, exp_tag_ready, bdo_ready, tag_ready,
        key_updated, rdkey_read, npub_read, nsec_read, bdi_read, bdo_write, bdo_size, bdo_nsec, msg_auth_done,
        msg_auth_vali,
160
161 --STATE DECLARATIONS
162 TYPE puf_state_type IS (idle,chall,exec,recv);
163 SIGNAL puf_state : puf_state_type := idle;
164 TYPE rep_state_type IS (idle,exec,set);
165 SIGNAL rep_state : rep_state_type := idle;
166 TYPE bch_state_type IS (idle,restart,exec,get,set);
167 SIGNAL bch_state : bch_state_type := idle;
168 TYPE resp_state_type IS (idle,get_seed2,get_pufresp1,get_bchrnd,get_chal2,get_nce2,get_pufresp2,wtaeadenc,
        checkandupd);
169 SIGNAL resp_state : resp_state_type := idle;
170 TYPE ketje_state_type IS (idle,ldkey,ldnce,initstate,ldad,wtad,comptag,ldmsg,wtmsg,1stmsg);
171 SIGNAL ketje_state : ketje_state_type := idle;
172
173 BEGIN
174 DAPUF_0: DAPUF PORT MAP (
175     clk => clk,
176     rst_n => rst_puf,
177     idata => challenge,
178     esig => esig_in,
179     Answer => res
180 );
181 BCH_ENCODER: bch255_139_31enc PORT MAP (
182     clk => clk,
183     reset => rst_bch,
184     din => din_bch,
185     vdin => vdin_bch_unused,
186     dout => dout_bch
187 );
188 KETJE: ketjeSr PORT MAP (
189     clk => clk,
190     rst => rst_ketje,
191     npub => npub,
192     nsec => nsec,
193     key => key,
194     rdkey => rdkey,
195     bdi => bdi,
196     exp_tag => exp_tag,
197     len_a => len_a,
198     len_d => len_d,
199     key_ready => key_ready,
200     key_updated => key_updated,
201     key_needs_update => key_needs_update,
202     rdkey_ready => rdkey_ready,
203     rdkey_read => rdkey_read,
204     npub_ready => npub_ready,
205     npub_read => npub_read,
206     nsec_ready => nsec_ready,
207     nsec_read => nsec_read,
208     bdi_ready => bdi_ready,
209     bdi_proc => bdi_proc,
210     bdi_ad => bdi_ad,
211     bdi_nsec => bdi_nsec,
212     bdi_pad => bdi_pad,
213     bdi_decrypt => bdi_decrypt,
214     bdi_eot => bdi_eot,
215     bdi_eoi => bdi_eoi,
216     bdi_read => bdi_read,
217     bdi_size => bdi_size,
218     bdi_valid_bytes => bdi_valid_bytes,
219     bdi_pad_loc => bdi_pad_loc,
220     bdi_nodata => bdi_nodata,
221     exp_tag_ready => exp_tag_ready,
222     bdo_ready => bdo_ready,
223     bdo_write => bdo_write,
224     bdo => bdo,
225     bdo_size => bdo_size,
226     bdo_nsec => bdo_nsec,
227     tag_ready => tag_ready,
228     tag_write => tag_write,
229     tag => tag,
230     msg_auth_done => msg_auth_done,
231     msg_auth_valid => msg_auth_valid
232 );
233
234 pdo81 <= nce2(31 DOWNTO 0);
235 pdo82 <= nce2(63 DOWNTO 32);
236 pdo83 <= nce2(95 DOWNTO 64);
237 pdo84 <= '0' & nce2(126 DOWNTO 96);
238 pdo85 <= t1(31 DOWNTO 0);
239 pdo86 <= t1(63 DOWNTO 32);
240 pdo87 <= t1(95 DOWNTO 64);
241 pdo88 <= t1(127 DOWNTO 96);
```

```

242
243 pdi <= pdi4 & pdi3 & pdi2 & pdi1;
244
245 lfsr_proc : PROCESS(clk, ctrl_rst_lfsr)
246 BEGIN
247   IF (ctrl_rst_lfsr = '1') THEN
248     IF (ctrl_lfsr = '1') THEN
249       lfsr <= seed1(11 DOWNT0 1) & '1';
250     ELSE
251       lfsr <= x"001";
252     END IF;
253   ELSIF RISING_EDGE(clk) THEN
254     lfsr(0) <= lfsr(11);
255     lfsr(1) <= lfsr(0);
256     lfsr(2) <= lfsr(1);
257     lfsr(3) <= lfsr(2) XOR lfsr(11);
258     lfsr(4) <= lfsr(3) XOR lfsr(11);
259     lfsr(5) <= lfsr(4);
260     lfsr(6) <= lfsr(5);
261     lfsr(7) <= lfsr(6) XOR lfsr(11);
262     lfsr(8) <= lfsr(7);
263     lfsr(9) <= lfsr(8);
264     lfsr(10) <= lfsr(9);
265     lfsr(11) <= lfsr(10);
266   END IF;
267 END PROCESS; --p(x) = 1001100100001
268
269 resp_proc : PROCESS(clk)
270 BEGIN
271   IF RISING_EDGE(clk) THEN
272     CASE resp_state IS
273     WHEN idle =>
274       ctrl_rst_ket_je <= '0';
275       IF (pdi5 = x"facade01") AND (setup = '0') THEN
276         chall <= pdi1 & pdi2(7 DOWNT0 0);
277         resp_state <= get_seed2;
278         ctrl_index <= x"000";
279         ctrl_rst_puf <= '1';
280         pdo89 <= x"facade01"; --data not ready
281       ELSIF (pdi5 = x"facade02") THEN
282         pdo90 <= (OTHERS => '0');
283         pdo91 <= (OTHERS => '0');
284         pdo92 <= (OTHERS => '0');
285         -- pdo93 to pdo126 OMITTED FOR CLARITY
286         pdol27 <= (OTHERS => '0');
287         pdol28 <= (OTHERS => '0');
288         pdol29 <= (OTHERS => '0');
289         resp_state <= get_seed2;
290         ctrl_index <= x"000";
291         ctrl_rst_puf <= '1';
292         pdo89 <= x"facade02"; --data not ready
293       END IF;
294     WHEN get_seed2 =>
295       IF (ctrl_index = x"00c") THEN
296         ctrl_rst_puf <= '0';
297         ctrl_rst_lfsr <= '1';
298         ctrl_lfsr <='1';
299         --challenge <= chall(39 DOWNT0 36) [ & chall(35 DOWNT0 33) & lfsr(11) & '0']* EXAMPLE
300         challenge <= chall(39 DOWNT0 36) & chall(35 DOWNT0 33) & lfsr(11) & '0' & chall(32 DOWNT0 30) & lfsr
(10) & '0' & chall(29 DOWNT0 27) & lfsr(9) & '0' & chall(26 DOWNT0 24) & lfsr(8) & '0' & chall(23
DOWNT0 21) & lfsr(7) & '0' & chall(20 DOWNT0 18) & lfsr(6) & '0' & chall(17 DOWNT0 15) & lfsr(5)
& '0' & chall(14 DOWNT0 12) & lfsr(4) & '0' & chall(11 DOWNT0 9) & lfsr(3) & '0' & chall(8
DOWNT0 6) & lfsr(2) & '0' & chall(5 DOWNT0 3) & lfsr(1) & '0' & chall(2 DOWNT0 0) & lfsr(0) &
'0';
301       END IF;
302       IF (ctrl_index = x"00c") THEN
303         resp_state <= get_pufrespl;
304         ctrl_index <= x"000";
305         seed1 <= seed2;
306         ctrl_lfsr <='0';
307       ELSIF (ctrl_puf_resp = '1') THEN
308         --challenge <= chall(39 DOWNT0 36) [ & chall(35 DOWNT0 33) & lfsr(11) & '0']* OMITTED
309         ctrl_rst_lfsr <= '0';
310         seed2(TO_INTEGER(UNSIGNED(ctrl_index))) <= res;
311         ctrl_index <= STD_LOGIC_VECTOR(UNSIGNED(ctrl_index) + 1);
312       END IF;
313     WHEN get_pufrespl =>
314       IF (ctrl_index = x"000") THEN
315         ctrl_rst_lfsr <= '1';
316         --challenge <= chall(39 DOWNT0 36) [ & chall(35 DOWNT0 33) & '0' & lfsr(11)]* OMITTED
317       END IF;
318       IF (ctrl_index = x"4fb") THEN
319         IF (pdi5 = x"facade01") AND (setup = '0') THEN
320           resp_state <= idle;
321           setup <= '1';
322           pdo90 <= pufresp(31 DOWNT0 0);
323           pdo91 <= pufresp(63 DOWNT0 32);
324           pdo92 <= pufresp(95 DOWNT0 64);
325           -- pdo93 to pdo126 OMITTED FOR CLARITY
326           pdol27 <= pufresp(1215 DOWNT0 1184);
327           pdol28 <= pufresp(1247 DOWNT0 1216);
328           pdol29 <= pufresp(1279 DOWNT0 1248);
329           pdo89 <= x"accede01"; --data ready
330         ELSE
331           resp_state <= get_bchrnd;
332           ctrl_rst_rep <= '1'; --start repetition code in rep_proc
333           ctrl_index <= x"000";

```

## Appendix C. Source Code Listings

```
334     END IF;
335     ELSIF (ctrl_puf_resp = '1') THEN
336         --challenge <= chall(39 DOWNT0 36) [ & chall(35 DOWNT0 33) & '0' & lfsr(11)]* OMITTED
337         ctrl_rst_lfsr <= '0';
338         pufresp(TO_INTEGER(UNSIGNED(ctrl_index))) <= res;
339         ctrl_index <= STD_LOGIC_VECTOR(UNSIGNED(ctrl_index) + 1);
340     END IF;
341     WHEN get_bchrnd =>
342         IF (ctrl_index = x"000") THEN
343             ctrl_rst_lfsr <= '1';
344             ctrl_rst_rep <= '0';
345             ctrl_lfsr <='1';
346             --challenge <= chall(39 DOWNT0 36) [ & chall(35 DOWNT0 33) & lfsr(11) & '0']* OMITTED
347         END IF;
348         IF (ctrl_index = x"08b") THEN
349             resp_state <= get_chal2;
350             ctrl_rst_bch <= '1'; --start bch code in bch_proc
351             ctrl_ket_je_mode <= "01";
352             ctrl_index <= x"000";
353             ctrl_lfsr <='0';
354         ELSIF (ctrl_puf_resp = '1') THEN
355             --challenge <= chall(39 DOWNT0 36) [ & chall(35 DOWNT0 33) & lfsr(11) & '0']* OMITTED
356             ctrl_rst_lfsr <= '0';
357             bchrnd(TO_INTEGER(UNSIGNED(ctrl_index))) <= res;
358             ctrl_index <= STD_LOGIC_VECTOR(UNSIGNED(ctrl_index) + 1);
359         END IF;
360     WHEN get_chal2 =>
361         IF (ctrl_index = x"028") THEN
362             resp_state <= get_nce2;
363             ctrl_index <= x"000";
364             ctrl_lfsr <='0';
365         ELSIF (ctrl_puf_resp = '1') THEN
366             --challenge <= chall(39 DOWNT0 36) [ & chall(35 DOWNT0 33) & lfsr(11) & '0']* OMITTED
367             ctrl_rst_bch <= '0';
368             chal2(TO_INTEGER(UNSIGNED(ctrl_index))) <= res;
369             ctrl_index <= STD_LOGIC_VECTOR(UNSIGNED(ctrl_index) + 1);
370         END IF;
371     WHEN get_nce2 =>
372         IF (ctrl_index = x"07f") THEN
373             resp_state <= get_pufresp2;
374             ctrl_rst_ket_je <= '1'; --start computing dev-key
375             ctrl_index <= x"000";
376             ctrl_lfsr <='0';
377         ELSIF (ctrl_puf_resp = '1') THEN
378             --challenge <= chall(39 DOWNT0 36) [ & chall(35 DOWNT0 33) & lfsr(11) & '0']* OMITTED
379             nce2(TO_INTEGER(UNSIGNED(ctrl_index))) <= res;
380             ctrl_index <= STD_LOGIC_VECTOR(UNSIGNED(ctrl_index) + 1);
381         END IF;
382     WHEN get_pufresp2 =>
383         IF (ctrl_index = x"000") THEN
384             ctrl_rst_lfsr <= '1';
385             --challenge <= chal2(39 DOWNT0 36) [ & chal2(35 DOWNT0 33) & '0' & lfsr(11)]* OMITTED
386         END IF;
387         IF (ctrl_index = x"4fb") THEN
388             resp_state <= wtaeadenc;
389             ctrl_index <= x"000";
390             ctrl_rst_ket_je <= '1'; --start computing C^1,T^1
391             ctrl_ket_je_mode <= "10";
392         ELSIF (ctrl_puf_resp = '1') THEN
393             --challenge <= chal2(39 DOWNT0 36) [ & chal2(35 DOWNT0 33) & '0' & lfsr(11)]* OMITTED
394             ctrl_rst_lfsr <= '0';
395             ctrl_rst_ket_je <= '0';
396             pufresp(TO_INTEGER(UNSIGNED(ctrl_index))) <= res;
397             ctrl_index <= STD_LOGIC_VECTOR(UNSIGNED(ctrl_index) + 1);
398         END IF;
399     WHEN wtaeadenc =>
400         IF (ctrl_comp_t2 = '1') THEN
401             ctrl_rst_ket_je <= '1'; --start computing T^2
402             ctrl_ket_je_mode <= "11";
403             resp_state <= checkandupd;
404             pdo89 <= x"facade09";
405         ELSE
406             ctrl_rst_ket_je <= '0';
407         END IF;
408     WHEN checkandupd =>
409         IF (ctrl_checkandupd = '1') THEN
410             pdo89 <= x"accede02"; --data ready
411         ELSE
412             ctrl_rst_ket_je <= '0';
413         END IF;
414         IF (pdi5 = x"accede02") AND (ctrl_checkandupd = '1') THEN
415             IF (pdi = t2) THEN
416                 chall <= chal2;
417                 pdo89 <= x"accede03"; --finished AND accepted
418             END IF;
419             resp_state <= idle;
420         END IF;
421     WHEN OTHERS =>
422         ctrl_rst_ket_je <= '0';
423     END CASE;
424 END IF;
425 END PROCESS;
426
427 puf_proc : PROCESS(clk)
428 BEGIN
429     IF (ctrl_rst_puf = '1') THEN
430         puf_state <= chall;
```

```

431     ELSIF RISING_EDGE(clk) THEN
432     CASE puf_state IS
433     WHEN chall =>
434         esig_in <= '1';
435         puf_state <= exec;
436     WHEN exec =>
437         esig_in <= '0';
438         ctrl_puf_resp <= '1';
439         puf_state <= recv;
440     WHEN recv =>
441         ctrl_puf_resp <= '0';
442         puf_state <= chall;
443     WHEN OTHERS =>
444     END CASE;
445     END IF;
446 END PROCESS;
447
448 rep_proc : PROCESS(clk)
449 BEGIN
450     IF (ctrl_rst_rep = '1') THEN
451         rep_state <= exec;
452     ELSIF RISING_EDGE(clk) THEN
453     CASE rep_state IS
454     WHEN exec =>
455         FOR i IN 0 TO 254 LOOP
456             rep_res(i) <= pufresp(i*5);
457             hd_rep(i*4) <= pufresp(i*5) XOR pufresp(i*5+1);
458             hd_rep(i*4+1) <= pufresp(i*5) XOR pufresp(i*5+2);
459             hd_rep(i*4+2) <= pufresp(i*5) XOR pufresp(i*5+3);
460             hd_rep(i*4+3) <= pufresp(i*5) XOR pufresp(i*5+4);
461         END LOOP;
462         rep_state <= set;
463     WHEN set =>
464         pdo1 <= hd_rep(31 DOWNT0 0);
465         pdo2 <= hd_rep(63 DOWNT0 32);
466         pdo3 <= hd_rep(95 DOWNT0 64);
467         -- pdo4 to pdo29 OMITTED FOR CLARITY
468         pdo30 <= hd_rep(959 DOWNT0 928);
469         pdo31 <= hd_rep(991 DOWNT0 960);
470         pdo32 <= "0000" & hd_rep(1019 DOWNT0 992);
471         rep_state <= idle;
472     WHEN OTHERS =>
473     END CASE;
474     END IF;
475 END PROCESS;
476
477 bch_proc : PROCESS(clk)
478 BEGIN
479     IF (ctrl_rst_bch = '1') THEN
480         bch_state <= restart;
481         ctrl_index2 <= x"00";
482     ELSIF RISING_EDGE(clk) THEN
483     CASE bch_state IS
484     WHEN restart =>
485         rst_bch <= '1';
486         bch_state <= exec;
487     WHEN exec =>
488         IF (ctrl_index2 = x"8c") THEN
489             bch_state <= get;
490             ctrl_index2 <= x"00";
491         ELSE
492             rst_bch <= '0';
493             din_bch <= bchrnd(TO_INTEGER(UNSIGNED(ctrl_index2)));
494             ctrl_index2 <= STD_LOGIC_VECTOR(UNSIGNED(ctrl_index2) + 1);
495         END IF;
496     WHEN get =>
497         IF (ctrl_index2 = x"74") THEN
498             bch_state <= set;
499             ctrl_index2 <= x"00";
500         ELSE
501             bch_cw(TO_INTEGER(UNSIGNED(ctrl_index2))) <= dout_bch;
502             ctrl_index2 <= STD_LOGIC_VECTOR(UNSIGNED(ctrl_index2) + 1);
503         END IF;
504     WHEN set =>
505         pdo33 <= bch_cw(31 DOWNT0 0) XOR rep_res(31 DOWNT0 0);
506         pdo34 <= bch_cw(63 DOWNT0 32) XOR rep_res(63 DOWNT0 32);
507         pdo35 <= bch_cw(95 DOWNT0 64) XOR rep_res(95 DOWNT0 64);
508         pdo36 <= (bchrnd(11 DOWNT0 0) XOR rep_res(127 DOWNT0 116)) & (bch_cw(115 DOWNT0 96) XOR rep_res(115
509             DOWNT0 96));
510         pdo37 <= bchrnd(43 DOWNT0 12) XOR rep_res(159 DOWNT0 128);
511         pdo38 <= bchrnd(75 DOWNT0 44) XOR rep_res(191 DOWNT0 160);
512         pdo39 <= bchrnd(107 DOWNT0 76) XOR rep_res(223 DOWNT0 192);
513         pdo40 <= '0' & (bchrnd(138 DOWNT0 108) XOR rep_res(254 DOWNT0 224));
514         bch_state <= idle;
515     WHEN OTHERS =>
516     END CASE;
517     END IF;
518 END PROCESS;
519
520 ketje_mode_proc : PROCESS(ctrl_ketje_mode)
521 BEGIN
522     IF (ctrl_ketje_mode = "01") THEN --keygen
523         key_reg <= '0' & rep_res(254 DOWNT0 128);
524         npub_reg <= '0' & nce2;
525         ad_reg <= rep_res(127 DOWNT0 0);
526     ELSIF (ctrl_ketje_mode = "10") THEN --enc
527         key_reg <= dev_key;

```

## Appendix C. Source Code Listings

```
527     npub_reg <= pdi;
528     ad_reg <= '0' & nce2;
529     ELSIF (ctrl_ketje_mode = "11") THEN --authenticator
530         key_reg <= dev_key;
531         npub_reg <= pdi;
532         ad_reg <= '1' & nce2;
533     END IF;
534 END PROCESS;
535
536 ketje_proc : PROCESS (clk)
537 BEGIN
538     IF (ctrl_rst_ketje = '1') THEN
539         ketje_state <= ldkey;
540         rst_ketje <= '1';
541         ctrl_cnt <= x"00";
542         ctrl_checkandupd <= '0';
543         ctrl_comp_t2 <= '0';
544     ELSIF RISING_EDGE (clk) THEN
545         CASE ketje_state IS
546             WHEN ldkey =>
547                 rst_ketje <= '0';
548                 key <= key_reg;
549                 key_needs_update <= '1';
550                 key_ready <= '1';
551                 ketje_state <= ldnce;
552             WHEN ldnce =>
553                 key_needs_update <= '0';
554                 key_ready <= '0';
555                 npub <= npub_reg;
556                 npub_ready <= '1';
557                 ketje_state <= initstate;
558             WHEN initstate =>
559                 npub_ready <= '0';
560                 IF (ctrl_cnt = x"0c") THEN --so total of 14 clk_periods
561                     ctrl_cnt <= x"00";
562                     ketje_state <= ldad;
563                 ELSE
564                     ctrl_cnt <= STD_LOGIC_VECTOR (UNSIGNED (ctrl_cnt) + 1);
565                 END IF;
566             WHEN ldad =>
567                 bdi <= ad_reg (TO_INTEGER (UNSIGNED (ctrl_cnt)) * 32 + 31 DOWNTO TO_INTEGER (UNSIGNED (ctrl_cnt)) * 32);
568                 bdi_ready <= '1';
569                 bdi_ad <= '1';
570                 IF (ctrl_cnt = x"03") AND (ctrl_ketje_mode = "10") THEN
571                     bdi_eot <= '1';
572                 ELSIF (ctrl_cnt = x"03") THEN
573                     bdi_eoi <= '1';
574                     bdi_eot <= '1';
575                 END IF;
576                 ctrl_cnt <= STD_LOGIC_VECTOR (UNSIGNED (ctrl_cnt) + 1);
577                 ketje_state <= wtad;
578             WHEN wtad =>
579                 bdi <= x"00000000";
580                 bdi_ready <= '0';
581                 bdi_ad <= '0';
582                 bdi_eot <= '0';
583                 bdi_eoi <= '0';
584                 IF (ctrl_cnt = x"04") AND (ctrl_ketje_mode = "10") THEN
585                     ketje_state <= ldmsg;
586                     ctrl_cnt <= x"00";
587                 ELSIF (ctrl_cnt = x"04") THEN
588                     ketje_state <= comptag;
589                     ctrl_cnt <= x"00";
590                 ELSE
591                     ketje_state <= ldad;
592                 END IF;
593             WHEN ldmsg =>
594                 bdi <= pufresp (TO_INTEGER (UNSIGNED (ctrl_cnt)) * 32 + 31 DOWNTO TO_INTEGER (UNSIGNED (ctrl_cnt)) * 32);
595                 bdi_ready <= '1';
596                 IF (ctrl_cnt = x"27") THEN
597                     bdi_eot <= '1';
598                 END IF;
599                 ctrl_cnt <= STD_LOGIC_VECTOR (UNSIGNED (ctrl_cnt) + 1);
600                 ketje_state <= wtmsg;
601             WHEN wtmsg =>
602                 bdi <= x"00000000";
603                 bdi_ready <= '0';
604                 bdi_eot <= '0';
605                 bdi_eoi <= '0';
606                 IF (ctrl_cnt = x"28") then
607                     ketje_state <= lstmsg;
608                     c1 (TO_INTEGER (UNSIGNED (ctrl_cnt)) * 32 - 33 DOWNTO TO_INTEGER (UNSIGNED (ctrl_cnt)) * 32 - 64) <= bdo;
609                     ctrl_cnt <= x"00";
610                 ELSIF (ctrl_cnt /= x"00" AND (ctrl_cnt /= x"01") THEN
611                     c1 (TO_INTEGER (UNSIGNED (ctrl_cnt)) * 32 - 33 DOWNTO TO_INTEGER (UNSIGNED (ctrl_cnt)) * 32 - 64) <= bdo;
612                 ELSE
613                     ketje_state <= ldmsg;
614                 ELSE
615                     ketje_state <= ldmsg;
616                 END IF;
617             WHEN lstmsg =>
618                 IF (ctrl_cnt = x"01") THEN
619                     c1 (1279 DOWNTO 1248) <= bdo;
620                     ketje_state <= comptag;
621                     ctrl_cnt <= x"00";
622                     pdo41 <= c1 (31 DOWNTO 0);
623                     pdo42 <= c1 (63 DOWNTO 32);
624                     pdo43 <= c1 (95 DOWNTO 64);
```



```

624         -- pdo44 to pdo76 OMITTED FOR CLARITY
625         pdo77 <= c1(1183 DOWNT0 1152);
626         pdo78 <= c1(1215 DOWNT0 1184);
627         pdo79 <= c1(1247 DOWNT0 1216);
628         pdo80 <= bdo;
629     ELSE
630         ctrl_cnt <= STD_LOGIC_VECTOR(UNSIGNED(ctrl_cnt) + 1);
631     END IF;
632     WHEN comptag =>
633     IF (tag_write = '1') THEN
634     IF (ctrl_ketje_mode = "01") THEN --keygen
635         dev_key <= tag;
636         ketje_state <= idle;
637     ELSIF (ctrl_ketje_mode = "10") THEN --enc
638         t1 <= tag;
639         ctrl_comp_t2 <= '1';
640         ketje_state <= idle;
641     ELSIF (ctrl_ketje_mode = "11") THEN --authenticator
642         t2 <= tag;
643         ketje_state <= idle;
644         ctrl_checkandupd <= '1';
645     END IF;
646     END IF;
647     WHEN OTHERS =>
648     END CASE;
649     END IF;
650 END PROCESS;
651 end Behavioral;

```

### C.2.3 3-1 DAPUF

```

1  /*****
2  // Author: J.G. (Gerben) Geltink // g.geltink@gmail.com
3  // Module: 3-1 DAPUF // dapuf.v
4  // This module describes the device DAPUF in the Concealing Ketje Protocol as presented by the
5  // guiding MSc thesis: Geltink, J. G. (2016). "Concealing Ketje: A Lightweight PUF-based
6  // Authentication Protocol".
7  //
8  // Copyright (c) 2015 Sakiyama, Machida, Iwamoto All Rights Reserved.
9  // Adapted by J.G. (Gerben) Geltink, Copyright (c) 2016 under MIT license
10 /*****/
11
12
13 /***** 3-1 DAPUF Module begin *****/
14 module DAPUF(clk, rst_n, idata, esig, Answer);
15
16 input        clk; // Clock signal
17 input        rst_n; // Reset signal
18 input [63:0] idata; // 64-bit challenge
19 input        esig; // Input signal
20 output       Answer; //1-bit response
21
22 /***** Wire/Register Definition begin *****/
23 //reg [63:0] idata;
24 reg Answer_reg;
25
26 wire a0,a1,a2,//// a3 to a64 OMITTED FOR CLARITY
27 wire b0,b1,b2,//// b3 to b64 OMITTED FOR CLARITY
28 wire c0,c1,c2,//// c3 to c64 OMITTED FOR CLARITY
29 wire d0,d1,d2,//// d3 to d64 OMITTED FOR CLARITY
30 wire e0,e1,e2,//// e3 to e64 OMITTED FOR CLARITY
31 wire f0,f1,f2,//// f3 to f64 OMITTED FOR CLARITY
32 wire res_a,res_b,res_c,res_d,res_e,res_f;
33 /***** Wire/Register Definition begin *****/
34
35 /***** Generate Input Signal begin *****/
36 //assign idata = idata;
37
38 FDCE #(
39     .INIT(1'b0) // Initial value of register (1'b0 or 1'b1)
40 ) sig_reg_a (
41     .Q(a0), // Data output
42     .C(clk), // Clock input
43     .CE(1'b1), // Clock enable input
44     .CLR(1'b0), // Asynchronous clear input
45     .D(esig) // Data input
46 );
47
48 FDCE #(
49     .INIT(1'b0) // Initial value of register (1'b0 or 1'b1)
50 ) sig_reg_b (
51     .Q(e0), // Data output
52     .C(clk), // Clock input
53     .CE(1'b1), // Clock enable input
54     .CLR(1'b0), // Asynchronous clear input
55     .D(esig) // Data input
56 );

```

## Appendix C. Source Code Listings

```
57 /***** Generate Input Signal end *****/
58
59 /***** First Selector Chain begin *****/
60 MUXF7 MUX_000(.0(a1), .IO(a0), .I1(a0), .S(idata[0])); // synthesis attribute keep of a1 is true;
61 MUXF7 MUX_001(.0(b1), .IO(c0), .I1(c0), .S(idata[0])); // synthesis attribute keep of b1 is true;
62 MUXF7 MUX_002(.0(a2), .IO(a1), .I1(b1), .S(idata[1])); // synthesis attribute keep of a2 is true;
63 MUXF7 MUX_003(.0(b2), .IO(b1), .I1(a1), .S(idata[1])); // synthesis attribute keep of b2 is true;
64 /// MUX_005 to MUX_123 OMITTED FOR CLARITY
65 MUXF7 MUX_124(.0(a63), .IO(a62), .I1(b62), .S(idata[62])); // synthesis attribute keep of a63 is true;
66 MUXF7 MUX_125(.0(b63), .IO(b62), .I1(a62), .S(idata[62])); // synthesis attribute keep of b63 is true;
67 MUXF7 MUX_126(.0(a64), .IO(a63), .I1(b63), .S(idata[63])); // synthesis attribute keep of a64 is true;
68 MUXF7 MUX_127(.0(b64), .IO(b63), .I1(a63), .S(idata[63])); // synthesis attribute keep of b64 is true;
69 /***** First Selector Chain end *****/
70
71 /***** Second Selector Chain begin *****/
72 MUXF7 MUX_128(.0(c1), .IO(a0), .I1(a0), .S(idata[0])); // synthesis attribute keep of c1 is true;
73 MUXF7 MUX_129(.0(d1), .IO(c0), .I1(c0), .S(idata[0])); // synthesis attribute keep of d1 is true;
74 MUXF7 MUX_130(.0(c2), .IO(c1), .I1(d1), .S(idata[1])); // synthesis attribute keep of c2 is true;
75 MUXF7 MUX_131(.0(d2), .IO(d1), .I1(c1), .S(idata[1])); // synthesis attribute keep of d2 is true;
76 /// MUX_132 to MUX_251 OMITTED FOR CLARITY
77 MUXF7 MUX_252(.0(c63), .IO(c62), .I1(d62), .S(idata[62])); // synthesis attribute keep of c63 is true;
78 MUXF7 MUX_253(.0(d63), .IO(d62), .I1(c62), .S(idata[62])); // synthesis attribute keep of d63 is true;
79 MUXF7 MUX_254(.0(c64), .IO(c63), .I1(d63), .S(idata[63])); // synthesis attribute keep of c64 is true;
80 MUXF7 MUX_255(.0(d64), .IO(d63), .I1(c63), .S(idata[63])); // synthesis attribute keep of d64 is true;
81 /***** Second Selector Chain end *****/
82
83 /***** Third Selector Chain begin *****/
84 MUXF7 MUX_256(.0(e1), .IO(a0), .I1(a0), .S(idata[0])); // synthesis attribute keep of e1 is true;
85 MUXF7 MUX_257(.0(f1), .IO(c0), .I1(c0), .S(idata[0])); // synthesis attribute keep of f1 is true;
86 MUXF7 MUX_258(.0(e2), .IO(e1), .I1(f1), .S(idata[1])); // synthesis attribute keep of e2 is true;
87 MUXF7 MUX_259(.0(f2), .IO(f1), .I1(e1), .S(idata[1])); // synthesis attribute keep of f2 is true;
88 /// MUX_260 to MUX_379 OMITTED FOR CLARITY
89 MUXF7 MUX_380(.0(e63), .IO(e62), .I1(f62), .S(idata[62])); // synthesis attribute keep of e63 is true;
90 MUXF7 MUX_381(.0(f63), .IO(f62), .I1(e62), .S(idata[62])); // synthesis attribute keep of f63 is true;
91 MUXF7 MUX_382(.0(e64), .IO(e63), .I1(f63), .S(idata[63])); // synthesis attribute keep of e64 is true;
92 MUXF7 MUX_383(.0(f64), .IO(f63), .I1(e63), .S(idata[63])); // synthesis attribute keep of f64 is true;
93 /***** Third Selector Chain end *****/
94
95 /***** Generate Response begin *****/
96 SRL SRL_0(.S(a64), .R(c64), .Q(res_a)); // synthesis attribute keep of res_a is true;
97 SRL SRL_1(.S(c64), .R(e64), .Q(res_b)); // synthesis attribute keep of res_b is true;
98 SRL SRL_2(.S(e64), .R(a64), .Q(res_c)); // synthesis attribute keep of res_c is true;
99 SRL SRL_3(.S(b64), .R(d64), .Q(res_d)); // synthesis attribute keep of res_d is true;
100 SRL SRL_4(.S(d64), .R(f64), .Q(res_e)); // synthesis attribute keep of res_e is true;
101 SRL SRL_5(.S(f64), .R(b64), .Q(res_f)); // synthesis attribute keep of res_f is true;
102
103 assign Answer = Answer_reg;
104
105 always @(posedge clk or negedge rst_n) begin
106     if (~rst_n) begin
107         //rst_n was unnecessary => changed by JGG
108         Answer_reg <= res_a^res_b^res_c^res_d^res_e^res_f; //1'b0; // Reset
109     end
110     else begin
111         Answer_reg <= res_a^res_b^res_c^res_d^res_e^res_f;
112     end
113 end
114 /***** Response Generating Part end *****/
115 endmodule
116 /***** 3-1 DAPUF Module end *****/
117
118 /***** SR Latch Module begin *****/
119 module SRL(S, R, Q);
120     input S,R;
121     output Q;
122     wire QB;
123
124     NAND2 NAND_0(.IO(S), .I1(QB), .O(Q)); // synthesis attribute keep of Q is true;
125     NAND2 NAND_1(.IO(R), .I1(Q), .O(QB)); // synthesis attribute keep of QB is true;
126 endmodule
127
128 /***** SR Latch module end *****/
```

## C.2.4 Constraints

```

1  #*****#
2  # Author:   J.G. (Gerben) Geltink # g.geltink@gmail.com
3  # Module:   Xilinx Design Constr # constr.xdc
4  # This module describes the design constraints of the device DAPUF in the Concealing Ketje
5  # Protocol as presented by the guiding MSc thesis: Geltink, J. G. (2016). "Concealing Ketje: A
6  # Lightweight PUF-based Authentication Protocol".
7  #
8  # Copyright (c) 2016 J.G. Geltink under MIT license
9  #*****#
10
11 #***** Start registers begin *****#
12 set_property BEL BFF [get_cells CKP_DEV_CORE_0/DAPUF_0/sig_reg_a]
13 set_property LOC SLICE_X56Y149 [get_cells CKP_DEV_CORE_0/DAPUF_0/sig_reg_a]
14 set_property BEL AFF [get_cells CKP_DEV_CORE_0/DAPUF_0/sig_reg_b]
15 set_property LOC SLICE_X56Y149 [get_cells CKP_DEV_CORE_0/DAPUF_0/sig_reg_b]
16 #***** Start registers end *****#
17
18 #***** First Selector Chain begin *****#
19 set_property BEL F7BMUX [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_000]
20 set_property LOC SLICE_X54Y148 [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_000]
21 set_property BEL F7BMUX [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_001]
22 set_property LOC SLICE_X55Y148 [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_001]
23 set_property BEL F7BMUX [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_002]
24 set_property LOC SLICE_X54Y147 [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_002]
25 set_property BEL F7BMUX [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_003]
26 set_property LOC SLICE_X55Y147 [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_003]
27 ### MUX_004 to MUX_123 OMITTED FOR CLARITY
28 set_property BEL F7BMUX [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_124]
29 set_property LOC SLICE_X54Y86 [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_124]
30 set_property BEL F7BMUX [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_125]
31 set_property LOC SLICE_X55Y86 [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_125]
32 set_property BEL F7BMUX [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_126]
33 set_property LOC SLICE_X54Y85 [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_126]
34 set_property BEL F7BMUX [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_127]
35 set_property LOC SLICE_X55Y85 [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_127]
36 #***** First Selector Chain end *****#
37
38 #***** Second Selector Chain begin *****#
39 set_property BEL F7BMUX [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_128]
40 set_property LOC SLICE_X56Y148 [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_128]
41 set_property BEL F7BMUX [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_129]
42 set_property LOC SLICE_X57Y148 [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_129]
43 set_property BEL F7BMUX [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_130]
44 set_property LOC SLICE_X56Y147 [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_130]
45 set_property BEL F7BMUX [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_131]
46 set_property LOC SLICE_X57Y147 [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_131]
47 ### MUX_132 to MUX_251 OMITTED FOR CLARITY
48 set_property BEL F7BMUX [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_252]
49 set_property LOC SLICE_X56Y86 [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_252]
50 set_property BEL F7BMUX [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_253]
51 set_property LOC SLICE_X57Y86 [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_253]
52 set_property BEL F7BMUX [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_254]
53 set_property LOC SLICE_X56Y85 [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_254]
54 set_property BEL F7BMUX [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_255]
55 set_property LOC SLICE_X57Y85 [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_255]
56 #***** Second Selector Chain end *****#
57
58 #***** Third Selector Chain begin *****#
59 set_property BEL F7BMUX [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_256]
60 set_property LOC SLICE_X58Y148 [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_256]
61 set_property BEL F7BMUX [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_257]
62 set_property LOC SLICE_X59Y148 [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_257]
63 set_property BEL F7BMUX [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_258]
64 set_property LOC SLICE_X58Y147 [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_258]
65 set_property BEL F7BMUX [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_259]
66 set_property LOC SLICE_X59Y147 [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_259]
67 ### MUX_260 to MUX_379 OMITTED FOR CLARITY
68 set_property BEL F7BMUX [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_380]
69 set_property LOC SLICE_X58Y86 [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_380]
70 set_property BEL F7BMUX [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_381]
71 set_property LOC SLICE_X59Y86 [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_381]
72 set_property BEL F7BMUX [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_382]
73 set_property LOC SLICE_X58Y85 [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_382]
74 set_property BEL F7BMUX [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_383]
75 set_property LOC SLICE_X59Y85 [get_cells CKP_DEV_CORE_0/DAPUF_0/MUX_383]
76 #***** Third Selector Chain end *****#
77
78
79 #***** Generate Response begin *****#
80 set_property BEL C6LUT [get_cells CKP_DEV_CORE_0/DAPUF_0/SRL_5/NAND_0]
81 set_property LOC SLICE_X59Y82 [get_cells CKP_DEV_CORE_0/DAPUF_0/SRL_5/NAND_0]
82 set_property BEL C6LUT [get_cells CKP_DEV_CORE_0/DAPUF_0/SRL_0/NAND_1]
83 set_property LOC SLICE_X56Y84 [get_cells CKP_DEV_CORE_0/DAPUF_0/SRL_0/NAND_1]
84 set_property BEL C6LUT [get_cells CKP_DEV_CORE_0/DAPUF_0/SRL_1/NAND_1]
85 set_property LOC SLICE_X58Y83 [get_cells CKP_DEV_CORE_0/DAPUF_0/SRL_1/NAND_1]
86 set_property BEL C6LUT [get_cells CKP_DEV_CORE_0/DAPUF_0/SRL_0/NAND_0]
87 set_property LOC SLICE_X54Y84 [get_cells CKP_DEV_CORE_0/DAPUF_0/SRL_0/NAND_0]
88 set_property BEL C6LUT [get_cells CKP_DEV_CORE_0/DAPUF_0/SRL_2/NAND_1]
89 set_property LOC SLICE_X54Y82 [get_cells CKP_DEV_CORE_0/DAPUF_0/SRL_2/NAND_1]
90 set_property BEL C6LUT [get_cells CKP_DEV_CORE_0/DAPUF_0/SRL_1/NAND_0]
91 set_property LOC SLICE_X56Y83 [get_cells CKP_DEV_CORE_0/DAPUF_0/SRL_1/NAND_0]

```

## Appendix C. Source Code Listings

```
92 set_property BEL C6LUT [get_cells CKP_DEV_CORE_0/DAPUF_0/SRL_3/NAND_1]
93 set_property LOC SLICE_X57Y84 [get_cells CKP_DEV_CORE_0/DAPUF_0/SRL_3/NAND_1]
94 set_property BEL C6LUT [get_cells CKP_DEV_CORE_0/DAPUF_0/SRL_2/NAND_0]
95 set_property LOC SLICE_X58Y82 [get_cells CKP_DEV_CORE_0/DAPUF_0/SRL_2/NAND_0]
96 set_property BEL C6LUT [get_cells CKP_DEV_CORE_0/DAPUF_0/SRL_4/NAND_1]
97 set_property LOC SLICE_X59Y83 [get_cells CKP_DEV_CORE_0/DAPUF_0/SRL_4/NAND_1]
98 set_property BEL C6LUT [get_cells CKP_DEV_CORE_0/DAPUF_0/SRL_3/NAND_0]
99 set_property LOC SLICE_X55Y84 [get_cells CKP_DEV_CORE_0/DAPUF_0/SRL_3/NAND_0]
100 set_property BEL C6LUT [get_cells CKP_DEV_CORE_0/DAPUF_0/SRL_5/NAND_1]
101 set_property LOC SLICE_X55Y82 [get_cells CKP_DEV_CORE_0/DAPUF_0/SRL_5/NAND_1]
102 set_property BEL C6LUT [get_cells CKP_DEV_CORE_0/DAPUF_0/SRL_4/NAND_0]
103 set_property LOC SLICE_X57Y83 [get_cells CKP_DEV_CORE_0/DAPUF_0/SRL_4/NAND_0]
104 #***** Generate Response end *****#
```

### C.2.5 BCH Encoder

```
1 -----
2 -- Author: J.G. (Gerben) Geltink -- g.geltink@gmail.com
3 -- Module: BCH encoder -- bch.vhd
4 -- This module describes the device BCH encoder of the Concealing Ketje Protocol as presented by
5 -- the guiding MSc thesis: Geltink, J. G. (2016). "Concealing Ketje: A Lightweight PUF-based
6 -- Authentication Protocol".
7 --
8 -- Copyright (c) 2016 J.G. Geltink under MIT license
9 -----
10
11 -- ring for encoder
12 LIBRARY ieee;
13 USE ieee.std_logic_1164.ALL;
14 USE WORK.const.ALL;
15
16 ENTITY ering IS
17 PORT (clk, r11, din: IN std_logic;
18       dout : OUT std_logic); --output serial data
19 END ering;
20
21 ARCHITECTURE eringa OF ering IS
22 SIGNAL rin, rout: std_logic_vector(0 TO nk-1) := (others => '0'); -- ring register
23 SIGNAL rin0: std_logic;
24 BEGIN
25   dout<= rout(nk-1);
26   rin0 <= (din XOR rout(nk-1)) AND r11;
27
28   rin(0)<= rin0;
29   rin(1) <= rout(0);
30   rin(2) <= rout(1);
31   rin(3) <= rout(2) XOR rin0;
32   rin(4) <= rout(3) XOR rin0;
33   rin(5) <= rout(4);
34   rin(6) <= rout(5);
35   rin(7) <= rout(6);
36   rin(8) <= rout(7) XOR rin0;
37   rin(9) <= rout(8) XOR rin0;
38   rin(10) <= rout(9);
39   rin(11) <= rout(10);
40   rin(12) <= rout(11);
41   rin(13) <= rout(12);
42   rin(14) <= rout(13);
43   rin(15) <= rout(14);
44   rin(16) <= rout(15);
45   rin(17) <= rout(16) XOR rin0;
46   rin(18) <= rout(17) XOR rin0;
47   rin(19) <= rout(18) XOR rin0;
48   rin(20) <= rout(19) XOR rin0;
49   -- rin(21) to rin(99) OMITTED FOR CLARITY
50   rin(100) <= rout(99);
51   rin(101) <= rout(100) XOR rin0;
52   rin(102) <= rout(101) XOR rin0;
53   rin(103) <= rout(102) XOR rin0;
54   rin(104) <= rout(103);
55   rin(105) <= rout(104) XOR rin0;
56   rin(106) <= rout(105) XOR rin0;
57   rin(107) <= rout(106) XOR rin0;
58   rin(108) <= rout(107) XOR rin0;
59   rin(109) <= rout(108);
60   rin(110) <= rout(109);
61   rin(111) <= rout(110) XOR rin0;
62   rin(112) <= rout(111);
63   rin(113) <= rout(112);
64   rin(114) <= rout(113) XOR rin0;
65   rin(115) <= rout(114);
66   -- Generator polynomial: 1001100011000000111101101000110000011111011011000110111000111010010111
67   -- 01100001010011110010101110110111011100100101
68   -- Number of XOR gates= 59
69
70 PROCESS BEGIN
71   WAIT UNTIL clk'EVENT AND clk='1';
72   rout<= rin;
```

```

73   END PROCESS;
74   END eringa;
75
76   -----
77   -- COUNTER MODULO n FOR ENCODER BCH CODE (n,k)
78   -- pe- parallel data in; rll-ring loop lock
79   LIBRARY ieee;
80   USE ieee.std_logic_1164.ALL;
81   USE WORK.const.ALL;
82
83   ENTITY ecount IS
84   PORT (clk, reset: IN std_logic;
85         vdin: OUT std_logic);
86   END ecount;
87
88   ARCHITECTURE ecounta OF ecount IS
89   SIGNAL cout: std_logic_vector(0 TO m-1); -- cout in GF(2^m); cout= L^count
90   SIGNAL vdinR, vdinS, vdinI: std_logic;
91   BEGIN
92   vdinR<= cout(0) AND NOT cout(1) AND NOT cout(2) AND NOT cout(3) AND NOT cout(4) AND cout(5) AND NOT cout(6) AND
      NOT cout(7);
93   -- reset vdin if cout==k-1
94   vdinS<= ( NOT cout(0) AND cout(1) AND cout(2) AND cout(3) AND NOT cout(4) AND NOT cout(5) AND NOT cout(6) AND
      cout(7)) OR reset;
95   -- vdinS=1 if cout==n-1
96   vdinI<= vdinI AND NOT reset;
97
98   PROCESS BEGIN
99   WAIT UNTIL clk'EVENT AND clk='1';
100  IF vdinR='1' THEN
101    vdinI<= '0';
102  ELSIF vdinS='1' THEN
103    vdinI<= '1';
104  END IF;
105  END PROCESS;
106
107  PROCESS BEGIN -- increment or reset cout in ring, cout=L^count
108  WAIT UNTIL clk'EVENT AND clk='1';
109  cout(0)<= cout(m-1) OR reset;
110  cout(1)<= cout(0) AND NOT reset;
111  cout(2)<= (cout(1) XOR cout(m-1)) AND NOT reset;
112  cout(3)<= (cout(2) XOR cout(m-1)) AND NOT reset;
113  cout(4)<= (cout(3) XOR cout(m-1)) AND NOT reset;
114  cout(5)<= cout(4) AND NOT reset;
115  cout(6)<= cout(5) AND NOT reset;
116  cout(7)<= cout(6) AND NOT reset;
117  END PROCESS; --p(x) = 100011101
118  END ecounta;
119
120   -----
121   -- ENCODER
122   LIBRARY ieee;
123   USE ieee.std_logic_1164.ALL;
124
125   ENTITY bch255_139_31enc IS
126   PORT (clk, reset, din: IN std_logic;
127         vdin, dout: OUT std_logic); --output serial data
128   END bch255_139_31enc; -- vdin - valid data in - to enable external data shifting
129
130   ARCHITECTURE enca OF bch255_139_31enc IS
131   SIGNAL vdinI, rin, rout, rll: std_logic;
132   -- rll-ring loop lock, pe-parallel enable din
133
134   COMPONENT ecount --counter encoder
135   PORT (clk, reset: IN std_logic; vdin: OUT std_logic);
136   END COMPONENT;
137   FOR ALL: ecount USE ENTITY WORK.ecount (ecounta);
138   COMPONENT ering --ring for encoder
139   PORT (clk, rll, din: IN std_logic; dout: OUT std_logic);
140   END COMPONENT;
141   FOR ALL: ering USE ENTITY WORK.ering (eringa);
142   BEGIN
143   cl: ecount
144   PORT MAP (clk, reset, vdinI);
145   rl: ering
146   PORT MAP (clk, rll, rin, rout);
147   rin<= din AND NOT reset;
148   rll<= vdinI AND NOT reset;
149   vdin<= vdinI;
150
151   PROCESS BEGIN
152   WAIT UNTIL clk'EVENT AND clk='1';
153   dout<= (NOT vdinI AND rout) OR (vdinI AND rin);
154   END PROCESS;
155   END enca;

```

